

# **PFM Studies of Polarization Dynamics in Ferroelectric Capacitors**

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**Oak Ridge National Laboratory**  
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# Outline

- ◆ **Introduction**

*Ferroelectric switching: theory and experiment*

- ◆ **Bias Dependent Measurements in PFM**

*Variability of switching parameters at the nanoscale*

- ◆ **Time Dependent Measurements in PFM**

*Applicability to fast switching processes*

- ◆ **Domain Switching Kinetics in Thin Film Capacitors**

*Polycrystalline vs epitaxial*

- ◆ **Capacitor Scaling Effect**

*Nucleation vs wall motion*

- ◆ **Conclusion**

## Ferroelectric Memories

The image is a promotional collage for Fujitsu's FRAM technology. It features a white humanoid robot holding a red block with the letter 'F', surrounded by large wooden blocks spelling 'E', 'R', 'A', 'M', and 'M'. To the right, a globe shows application areas: Metering, Automotive, Computing, and Industrial. A yellow arrow points from the globe to a cluster of RAMTRON FRAM IC packages. Below the globe are three close-up images: a DIP package, a surface-mount package, and a die micrograph showing the internal memory array.

## FeRAM - a dream semiconductor memory:

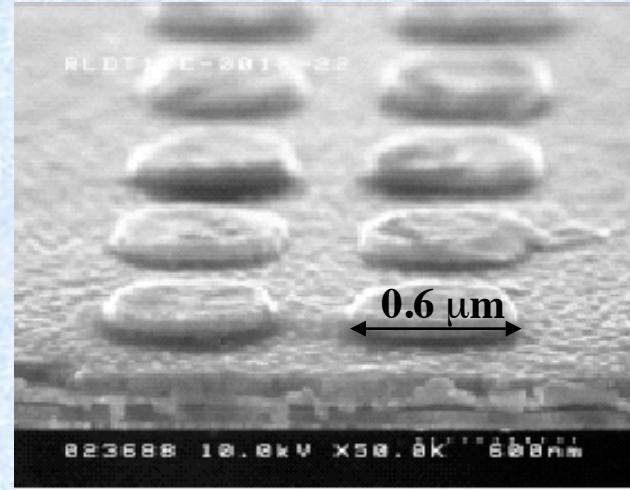
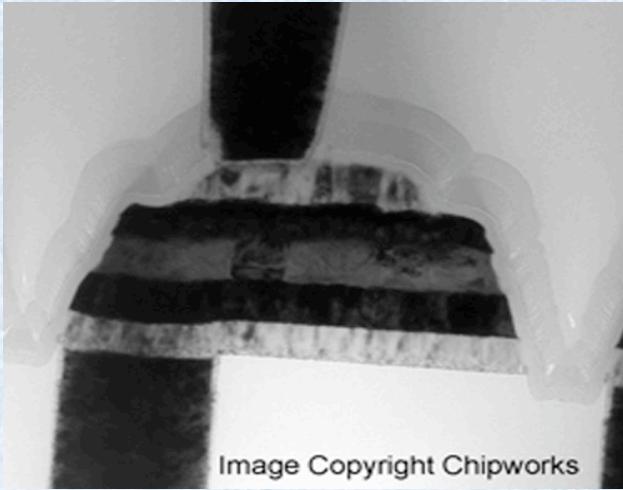
- High-density (as DRAM)
  - High-speed (as SRAM)
  - Nonvolatile (as Flash)

Over 30 million products using FRAM have already been shipped, including metering, RFID and smart-card devices (source: Ramtron, 2007).



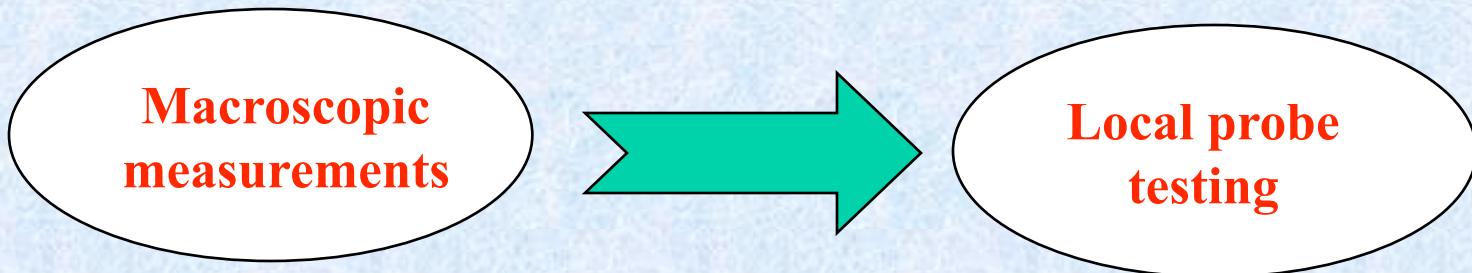
# Scaling of Ferroelectric Memories

PZT FeRAM cells



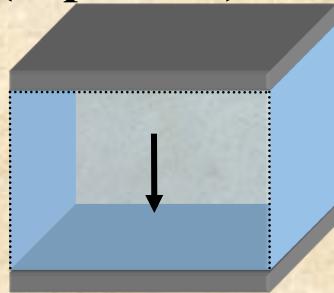
## Size effects become critical:

- Intrinsic limit for stable polarization
- Extrinsic effect on a stable domain and mechanism of switching
- Size limit for an operational device

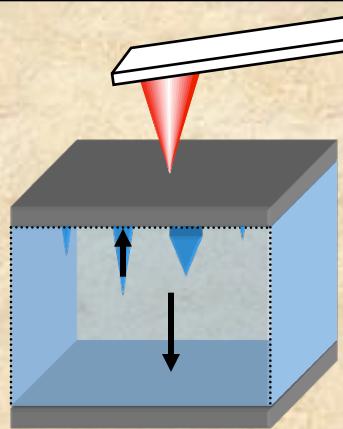


# Mechanism of Ferroelectric Switching in PFM

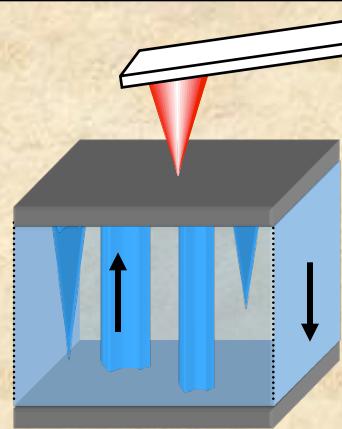
**Integral switching  
(capacitor)**



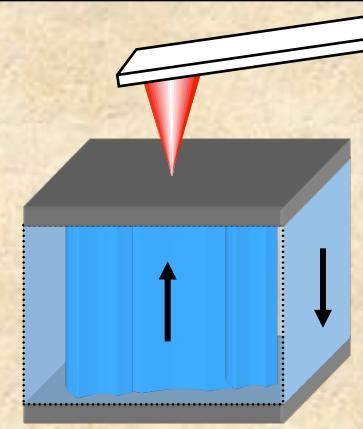
**initial state**



**nucleation**

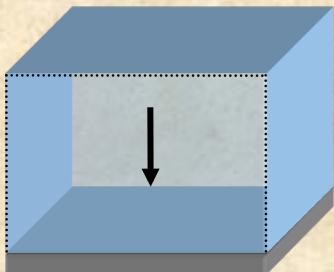


**forward growth**

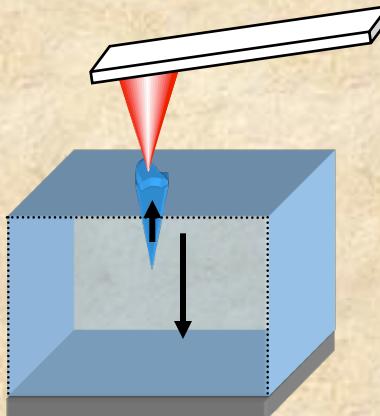


**lateral expansion**

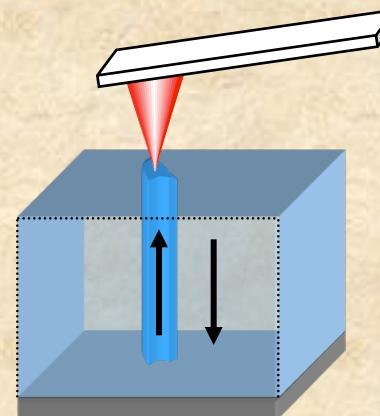
**Local switching  
(tip-induced)**



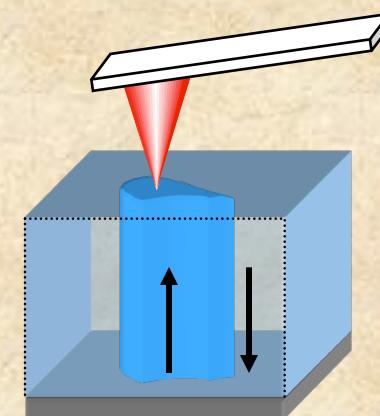
**initial state**



**nucleation**



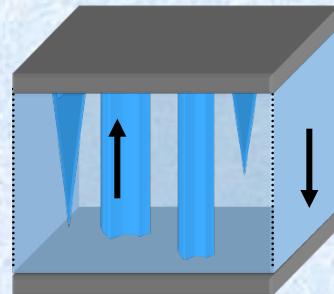
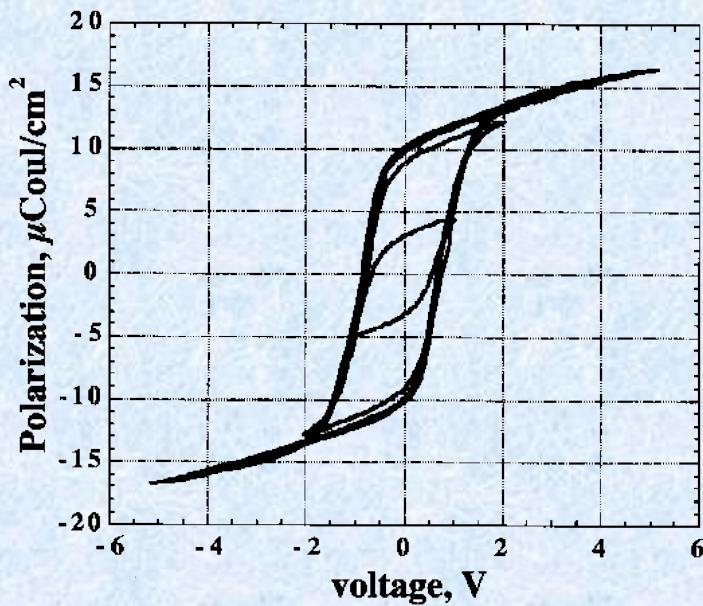
**forward growth**



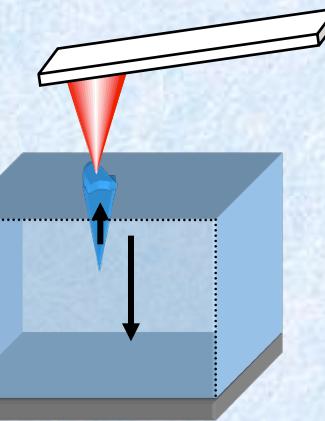
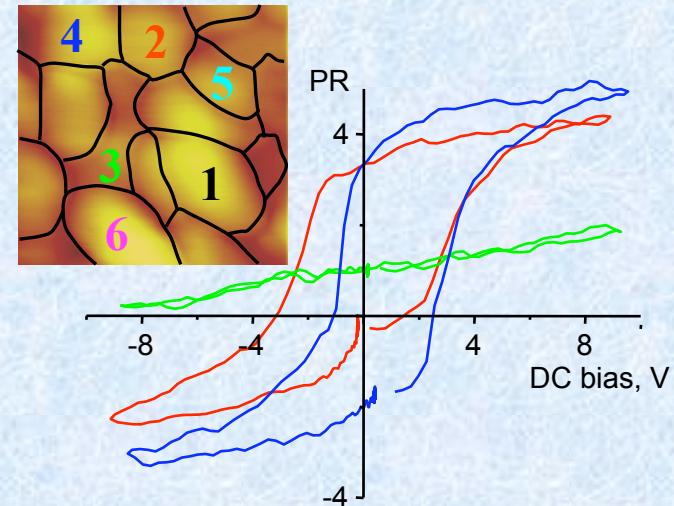
**lateral expansion**

# Hysteresis Loop: Global Switching vs Local

Polarization Hysteresis Loops



PFM Hysteresis Loops

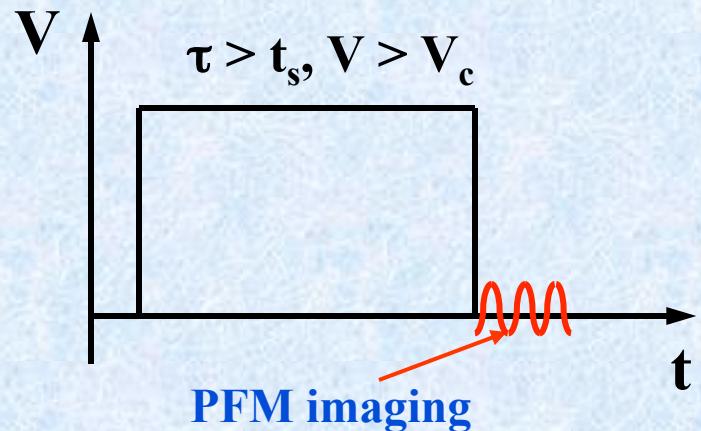


$$PR = d_{\text{eff}} \{V_0 - 2V_w\}$$

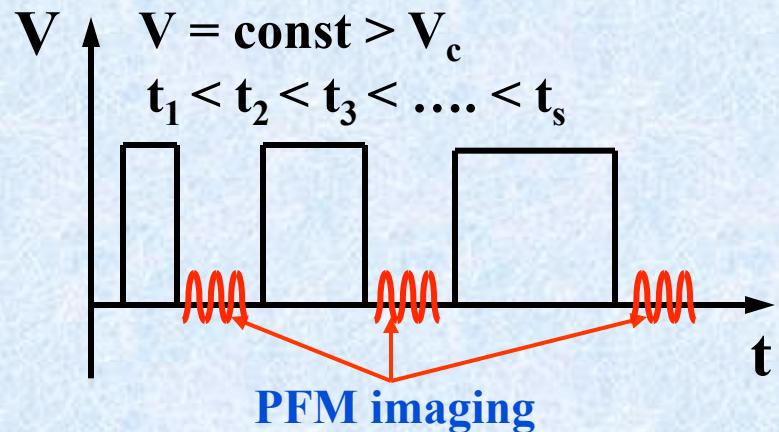
Kalinin et al, APL (2004)

# Pulse Trains for PFM Switching Studies

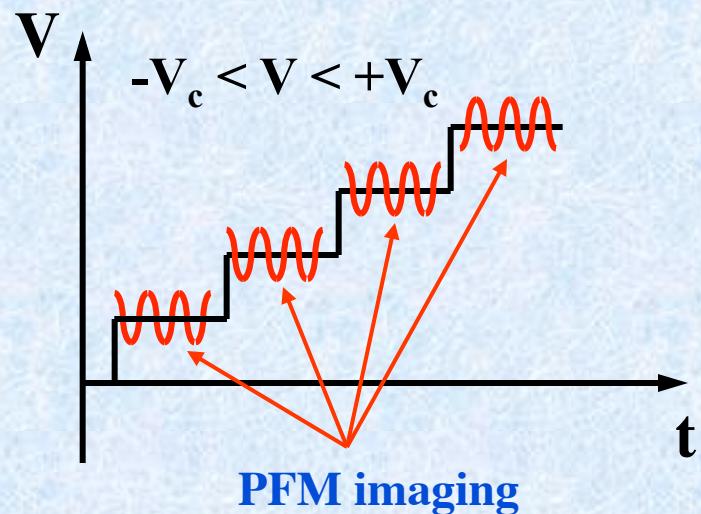
## 1. Conventional (switch-and-image) testing



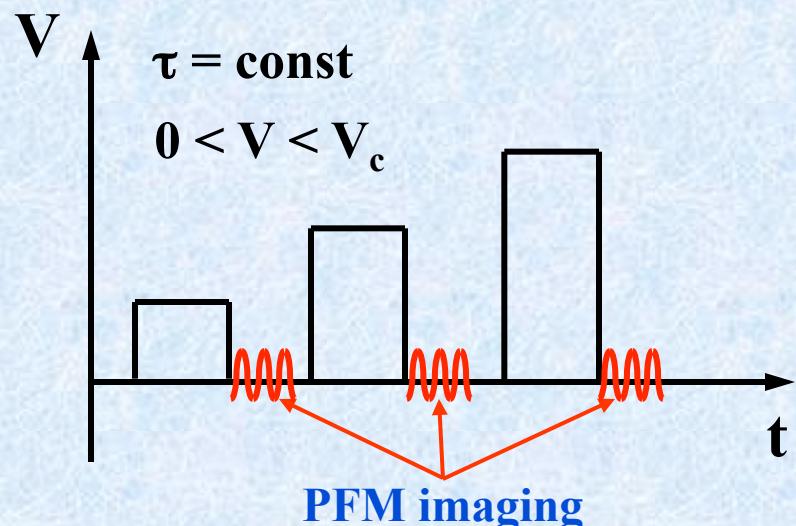
## 2. Stroboscopic (time dependent) testing



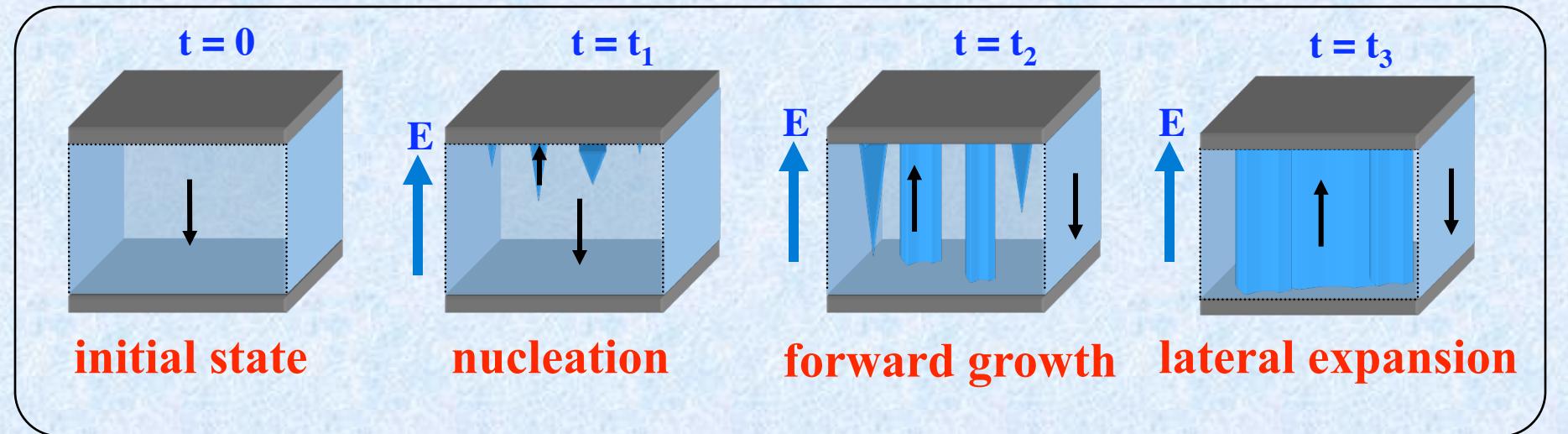
## 3. Spectroscopic (step bias) testing



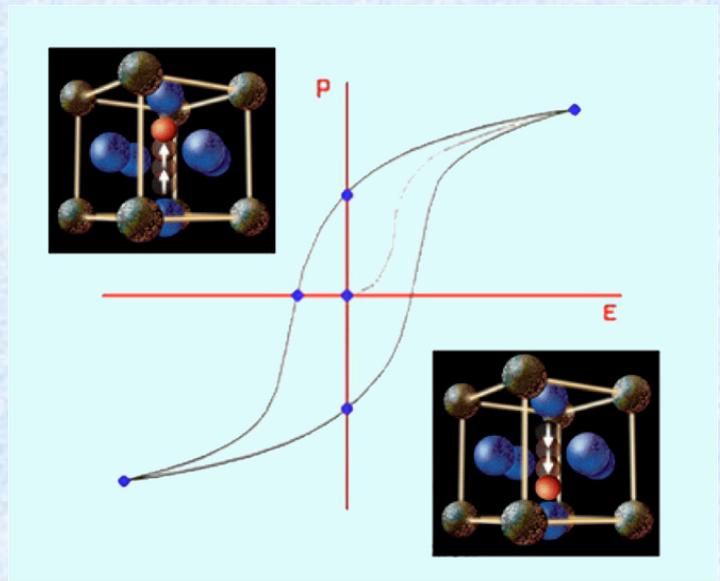
## 4. Spectroscopic (pulsed bias) testing



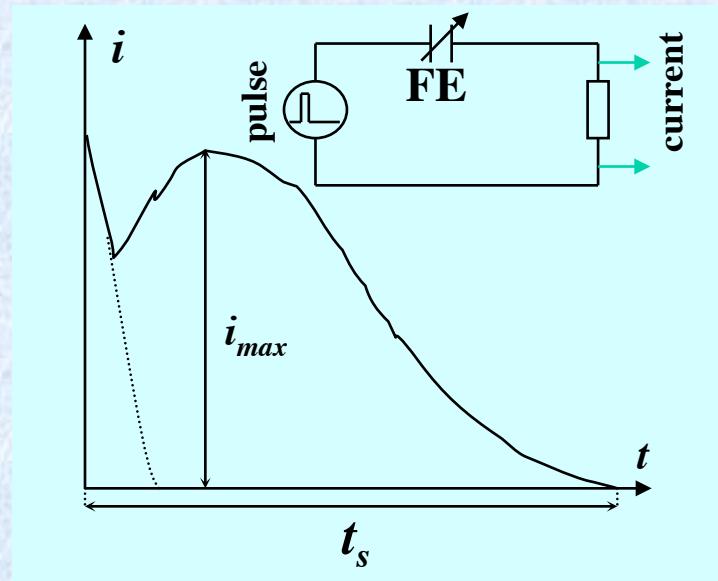
# Mechanism of Switching in Ferroelectrics



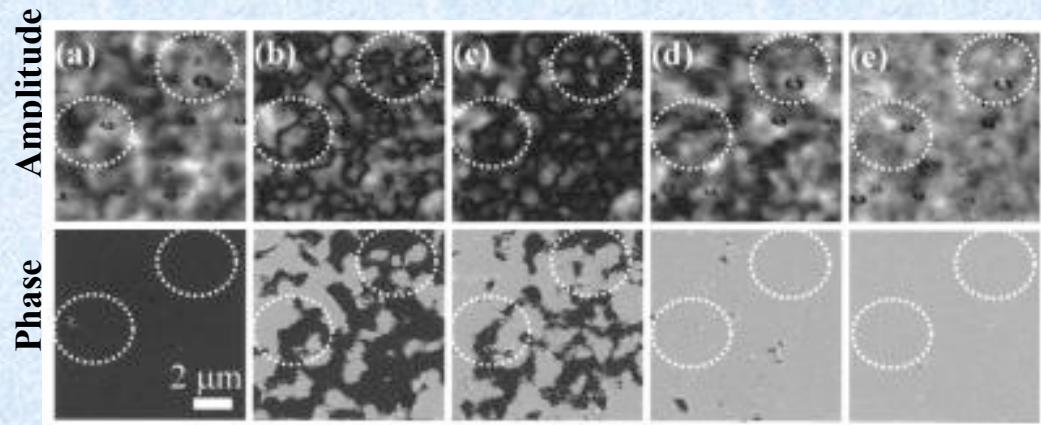
Bias dependence



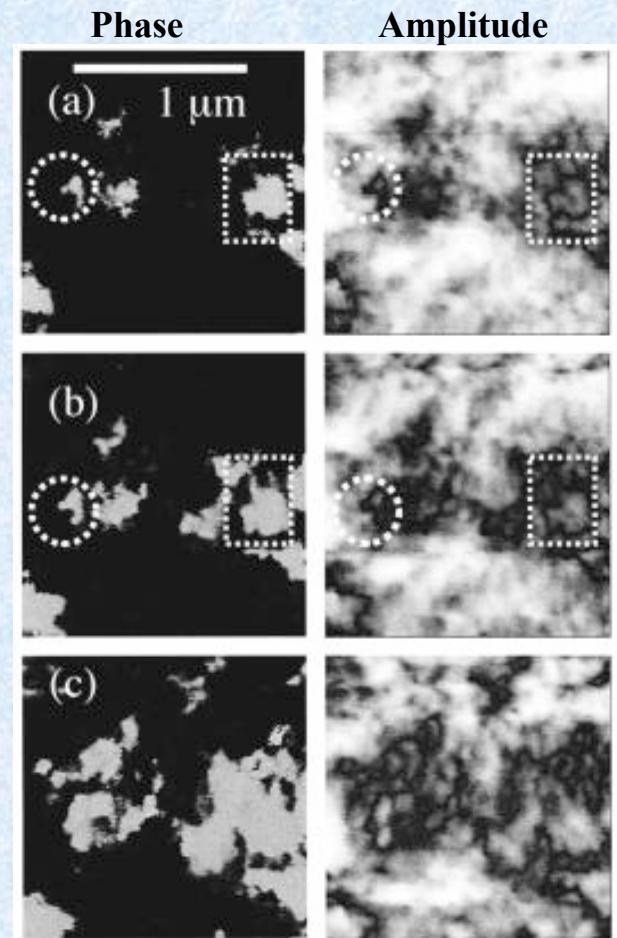
Time dependence



# Domain Evolution as a Function of Applied Bias



S. Hong and N. Setter, APL **81**, 3437 (2002)

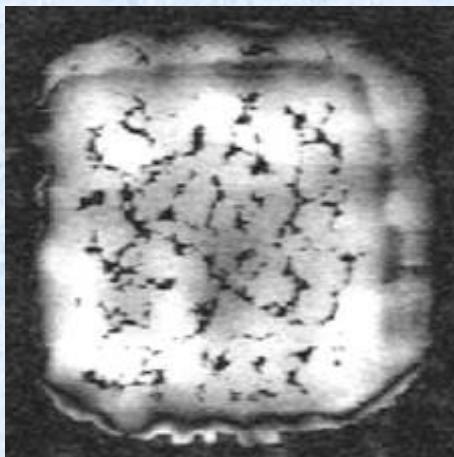


I. Stolichnov et al, APL **86**, 012902 (2005)

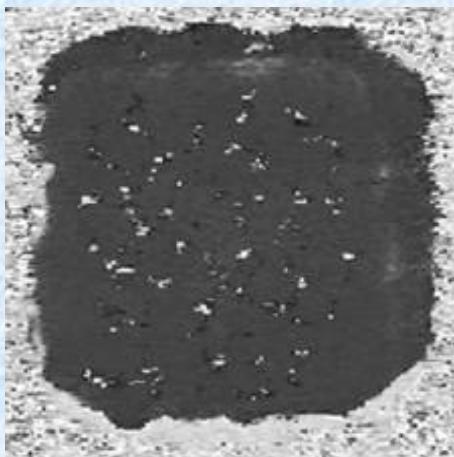
# Polarization as a function of applied DC bias

1.1 x1.1  $\mu\text{m}^2$  capacitor

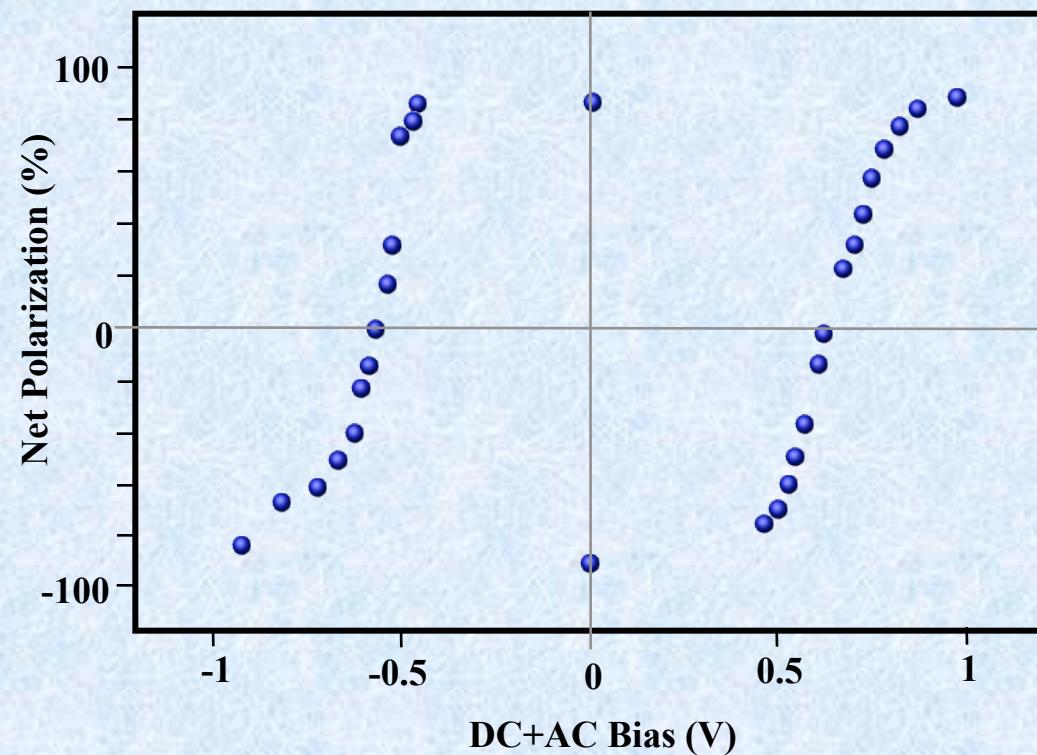
VPFM Amplitude



VPFM Phase



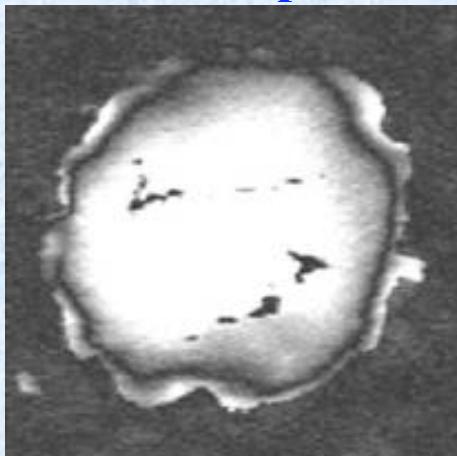
PFM imaging of ferroelectric capacitors provide direct microscopic evidence of the microscopic switching behavior.



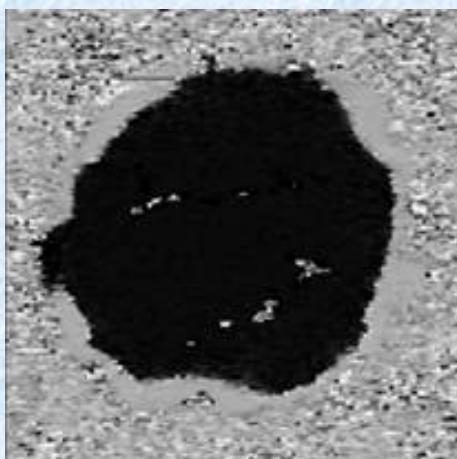
# Polarization as a function of applied DC bias

0.5 x 0.5  $\mu\text{m}^2$  capacitor

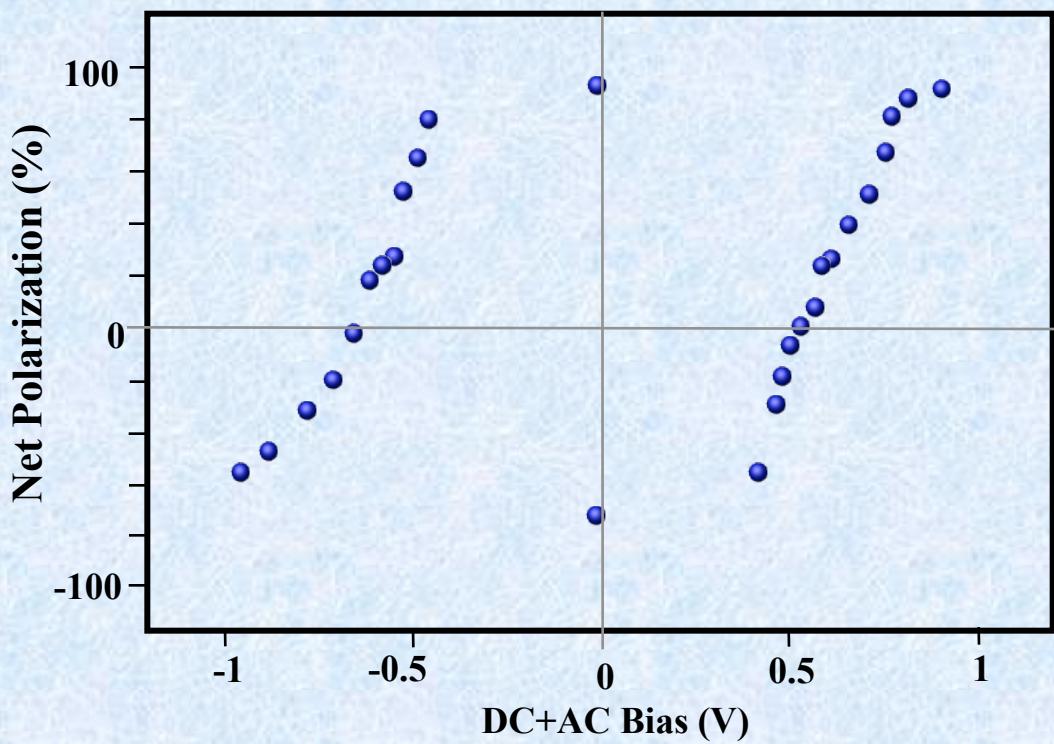
VPFM Amplitude



VPFM Phase



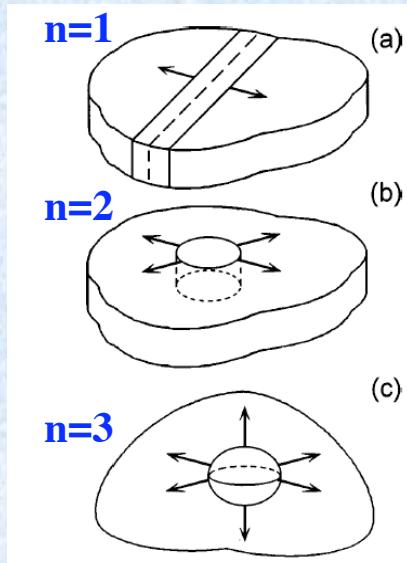
Electrode edge effect is observed: non-switched domains along the edge serve as seeds for switching. Reverse switching is almost exact re-trace of the forward switching.



# Switching Kinetics in Ferroelectrics

## Kolmogorov-Avrami-Ishibashi model

(nucleation in infinite medium)



Fraction of switched polarization:

$$f(t) = P(t)/P_{total}$$

$$f(t) = 1 - \exp[-(t/t_0)^n]$$

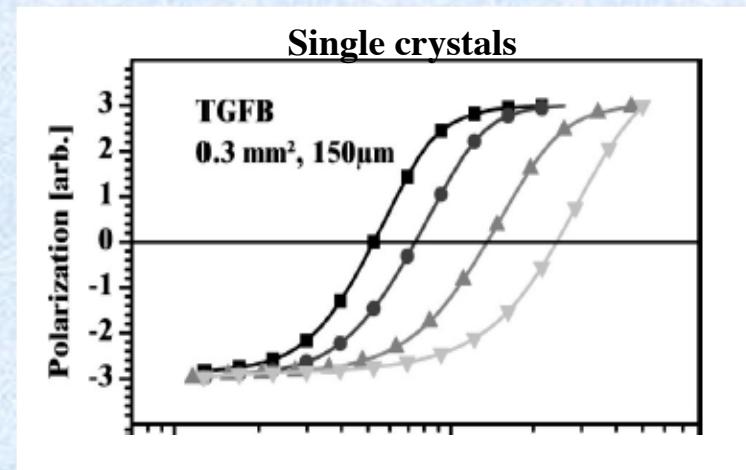
$t_0$  - characteristic switching time

$n$  - dimensionality of domain growth

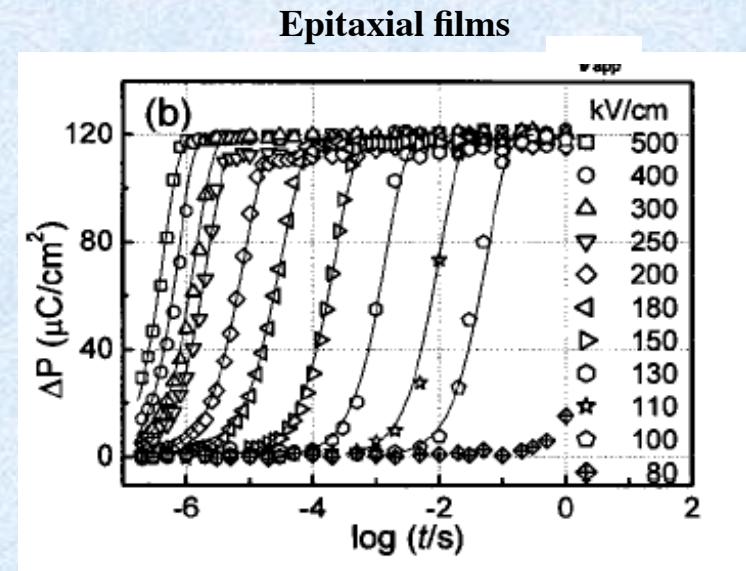
A. N. Kolmogorov, Izv. Akad. Nauk **3**, 355 (1937)

M. Avrami, J. Chem. Phys. **8**, 212 (1940)

H. Orihara *et al.*, J. Phys. Soc. Jpn. **63** 1031 (1994)



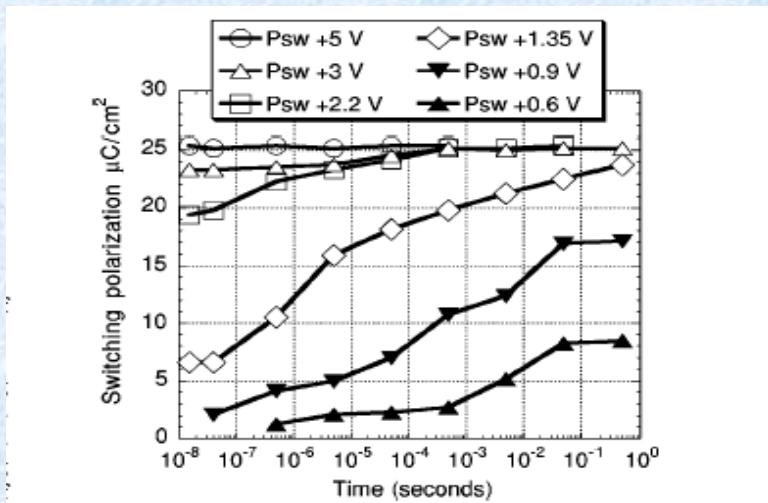
C. Pulvari and W. Kuebler, JAP **29**, 1742 (1958)



Y. W. So *et al.*, APL **86**, 92905 (2005)

# Switching in Polycrystalline Films

- Nucleation limited switching (NLS model)

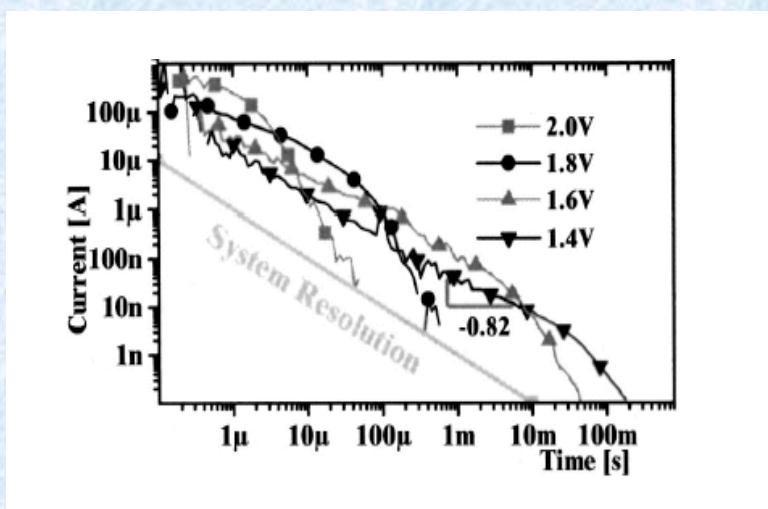


Nucleation limited switching mechanism  
(no effect of domain coalescence)

$$\frac{P(t)}{P_m} = 1 - \langle e^{-t/\tau} \rangle$$

Jung et al, Integrated Ferroelectrics 48, 59 (2002)  
Du and Chen, MRS Proc. 493, 311 (1998)  
Tagantsev et al, PR B 66, 214109 (2002)

- Curie–von Schweidler behavior



Ferroelectric switching is a result of polarization processes with a broad distribution of relaxation times:

$$i \sim t^{-\alpha}$$

Lohse et al, JAP 98, 2332 (2001)

# PFM Setup for Time-Dependent Switching Studies

Rise time: ~ 5-20 ns

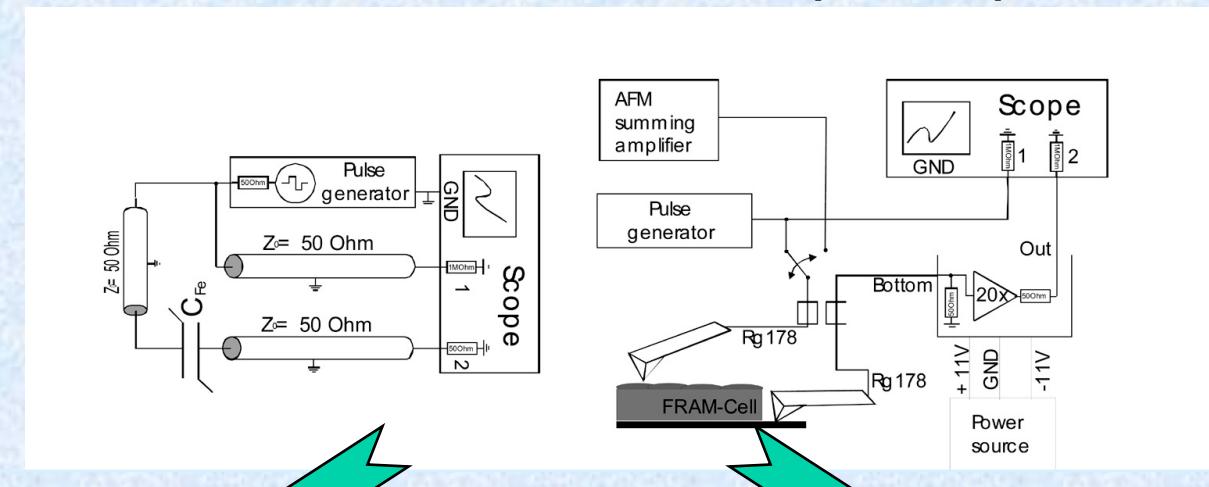
Pulse width: > 40 ns

Transient current 10  $\mu$ A

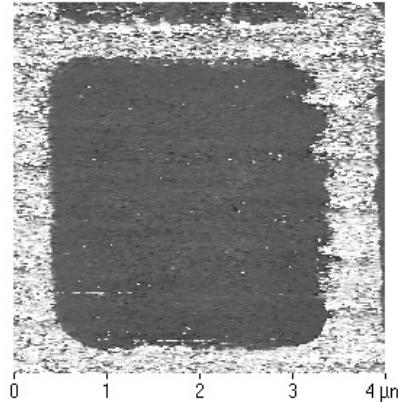
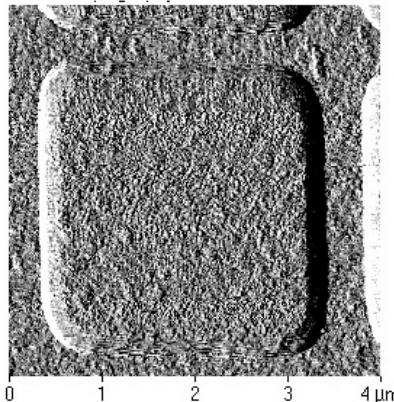
Min cap size: 1  $\mu$ m<sup>2</sup>

## Key parameters:

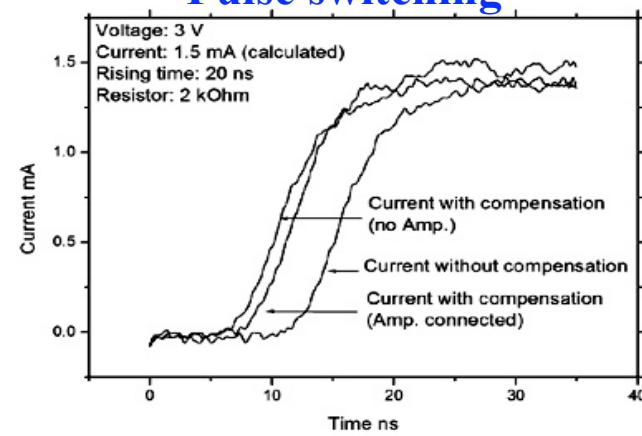
- Pulse rise time
- RC-constant
- Impedance matching



## PFM imaging

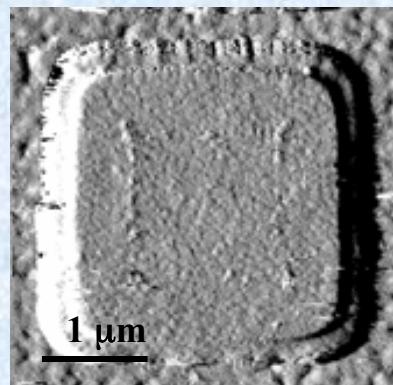


## Pulse switching

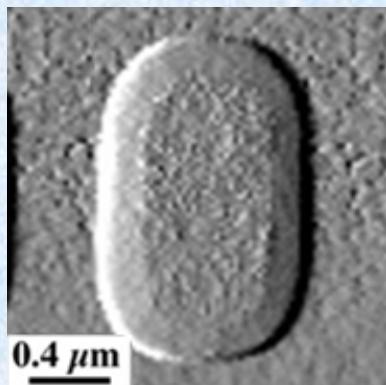


# PZT Capacitors for Switching Studies

**Poly-crystalline (111)  $\text{Pb}(\text{Zr}_{0.4}\text{Ti}_{0.6})\text{O}_3$**   
 $3 \times 3 \mu\text{m}^2$

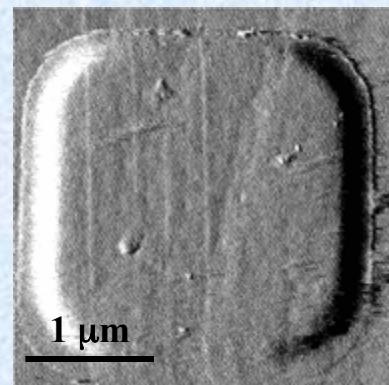


$1 \times 1.5 \mu\text{m}^2$

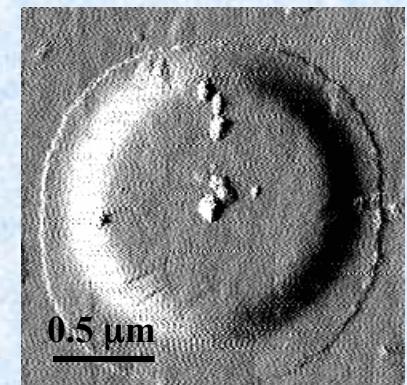


$\text{IrO}_2(50\text{nm})/\text{PZT}(180\text{nm})/\text{Pt}(175\text{nm})/\text{Ti}/\text{SiO}_2/\text{Si}$

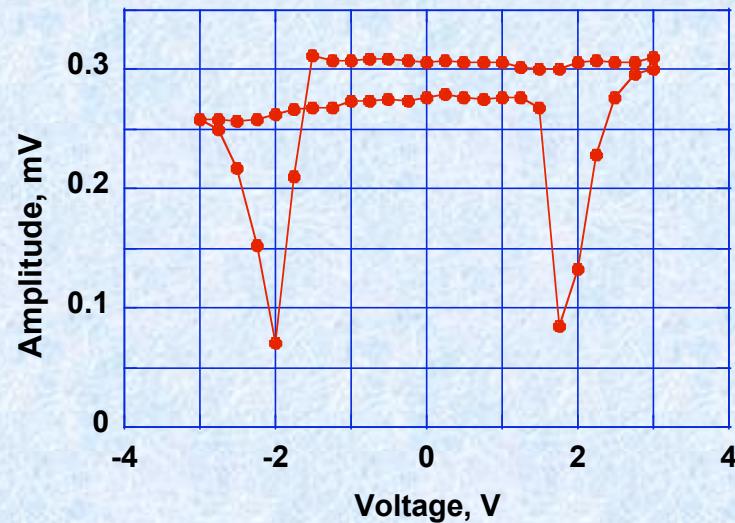
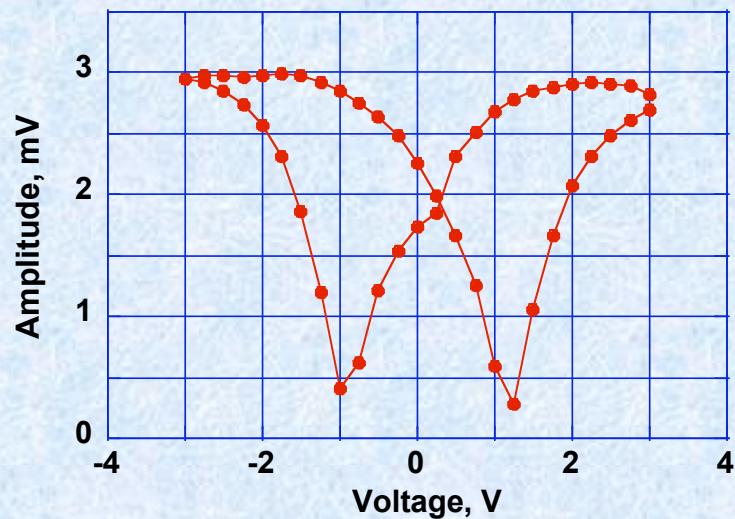
**Epitaxial (001)  $\text{Pb}(\text{Zr}_{0.2}\text{Ti}_{0.8})\text{O}_3$**   
 $2.5 \times 2.5 \mu\text{m}^2$



$1.1 \mu\text{m}$  diameter

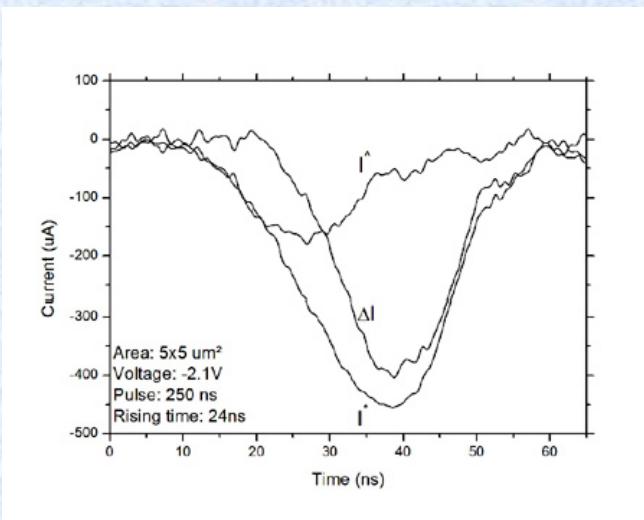


$\text{IrO}_2(50 \text{ nm})/\text{PZT}(50 \text{ nm})/\text{SRO}(20 \text{ nm})/\text{STO}$

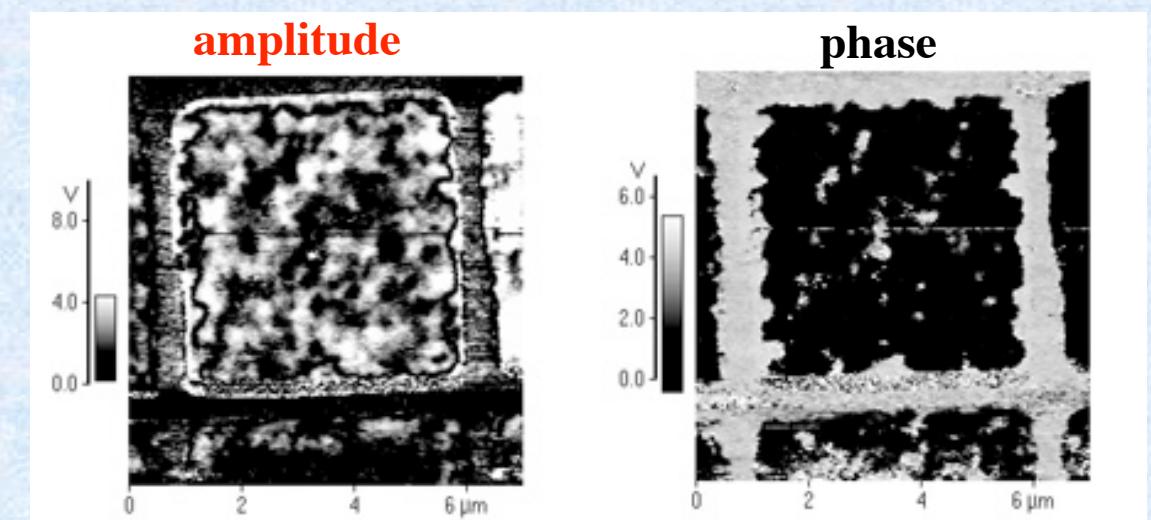


# Comparison of PFM and Switching Current Data

Pulse: 2.1 V, 250 ns



5x5  $\mu\text{m}^2$  capacitor



I(t) data suggest *complete* switching of the capacitor



But...

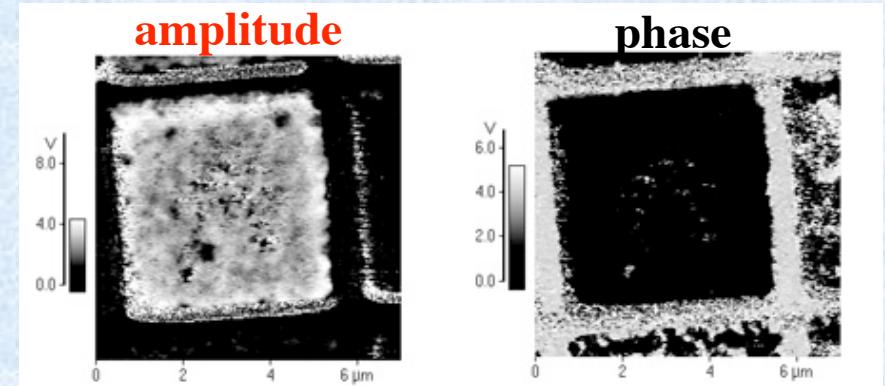
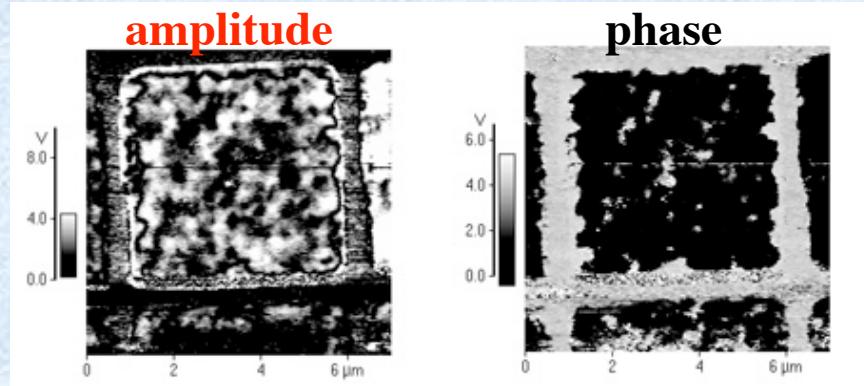
PFM images suggest *incomplete* switching

# Pulse Parameters Effect on PFM Image

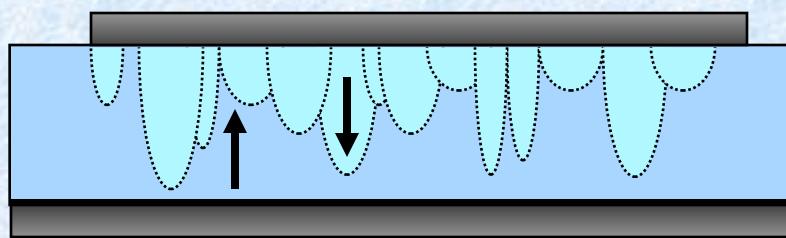
Pulse: 2.1 V, 250 ns

Pulse: 5 V, 1 s

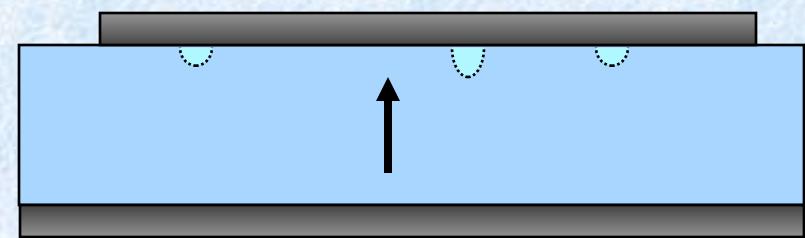
Piezoresponse images after pulse application



Schematics of domain pattern (side view)



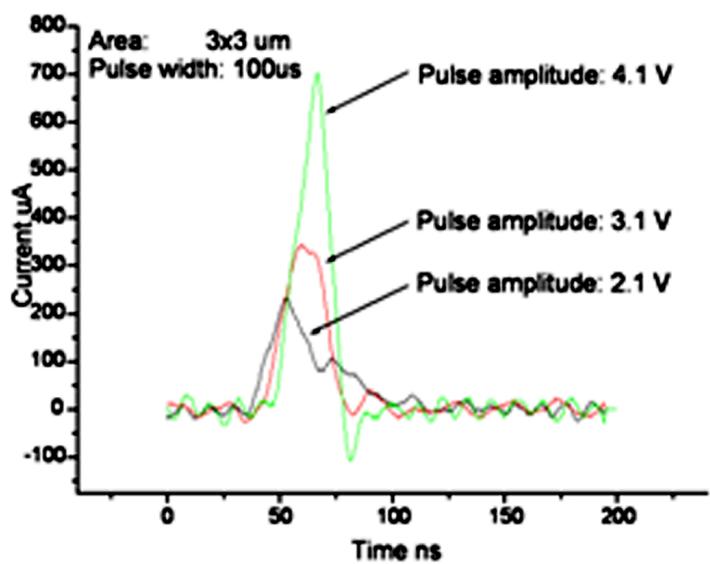
Partial switching



Complete switching

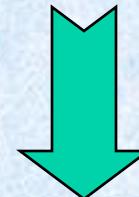
**Note:** Intermediate domain pattern corresponding to partial switching exists in a metastable state for a time period long enough for PFM imaging

# PFM for Fast Domain Switching Dynamics



Switching times in FE caps: from 50 ns to 1 ms

Acquisition of the PFM image: several minutes



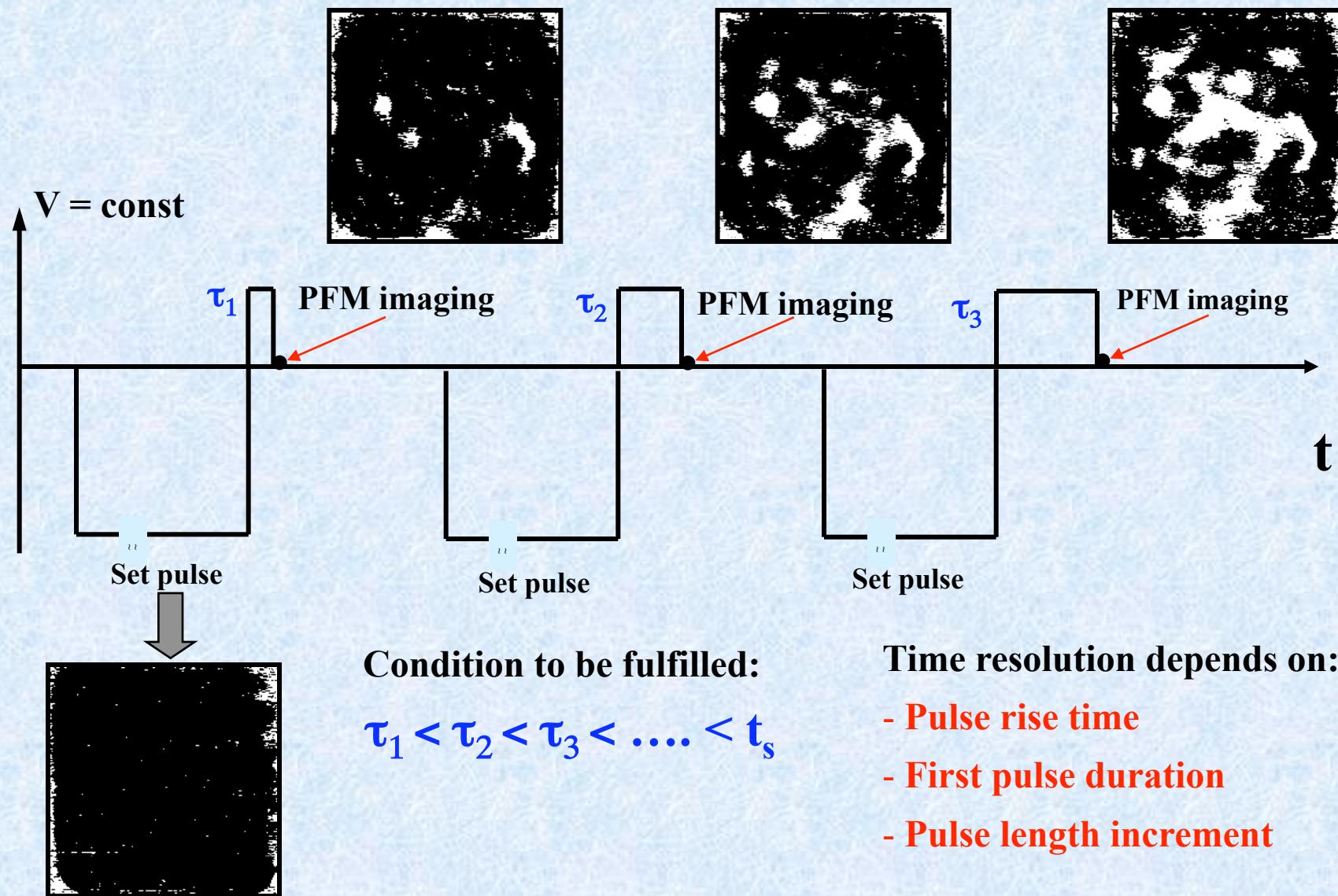
How can we use PFM to study fast switching processes?



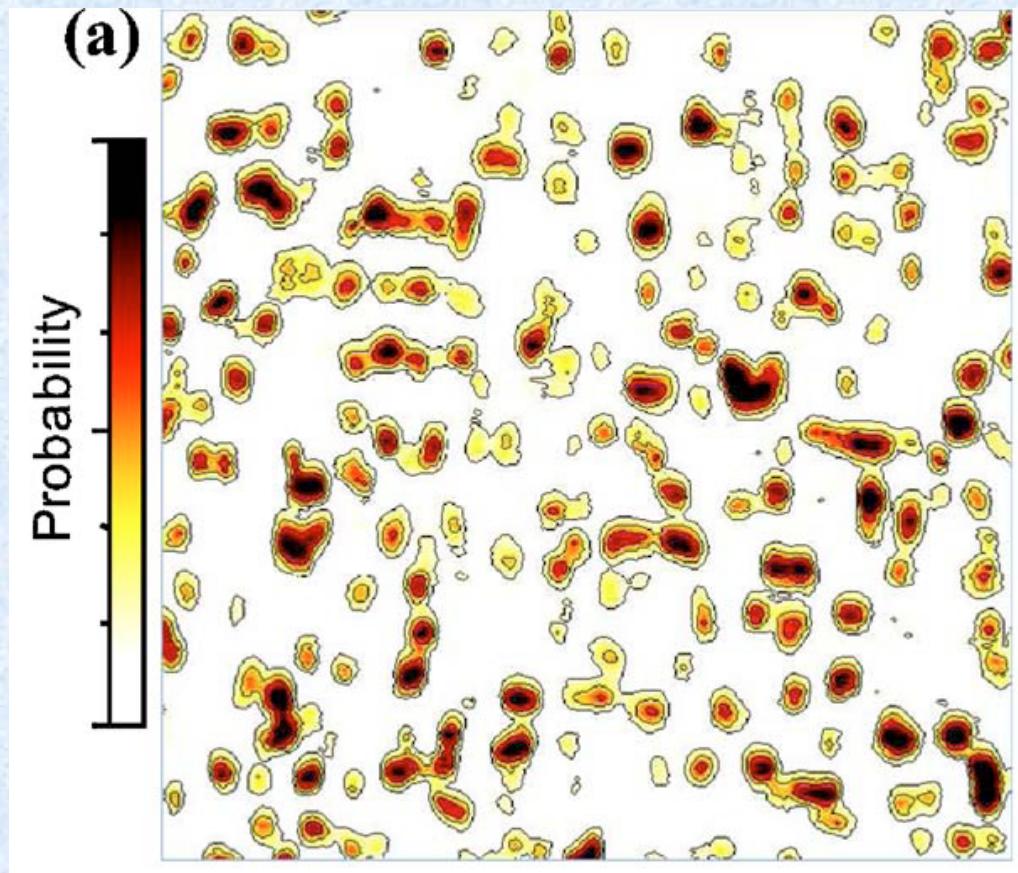
**STROBOSCOPIC PFM**

# PFM for Fast Domain Switching

Pulse train for stroboscopic PFM studies of domain kinetics:



# Heterogeneous Nucleation in Capacitors



The nucleation sites in capacitors can be visualized directly.

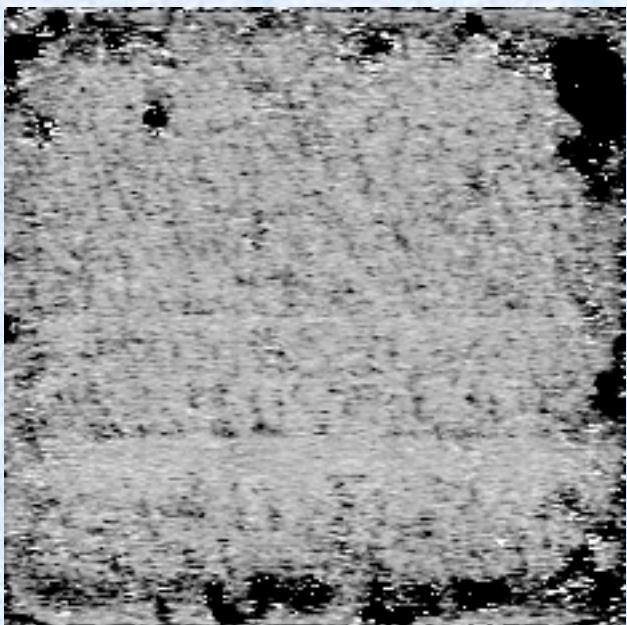
# Domain Switching in FeRAM Capacitors

Shortest pulse: 10 ns

Voltage range: <2.0 V

Coercive voltage: 1.1 V

**5x5  $\mu\text{m}^2$**



1.6V (~89 kV/cm)

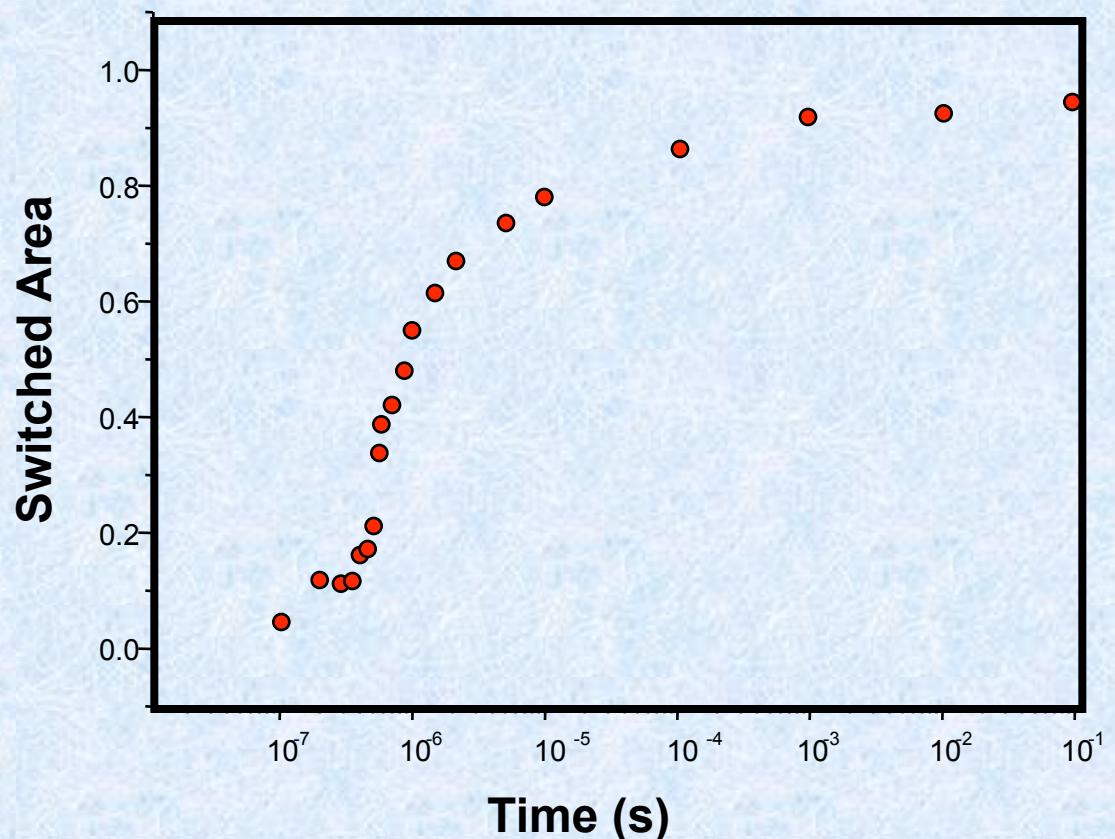
Note switching time variations  
within the capacitor.

Direct measurements of:

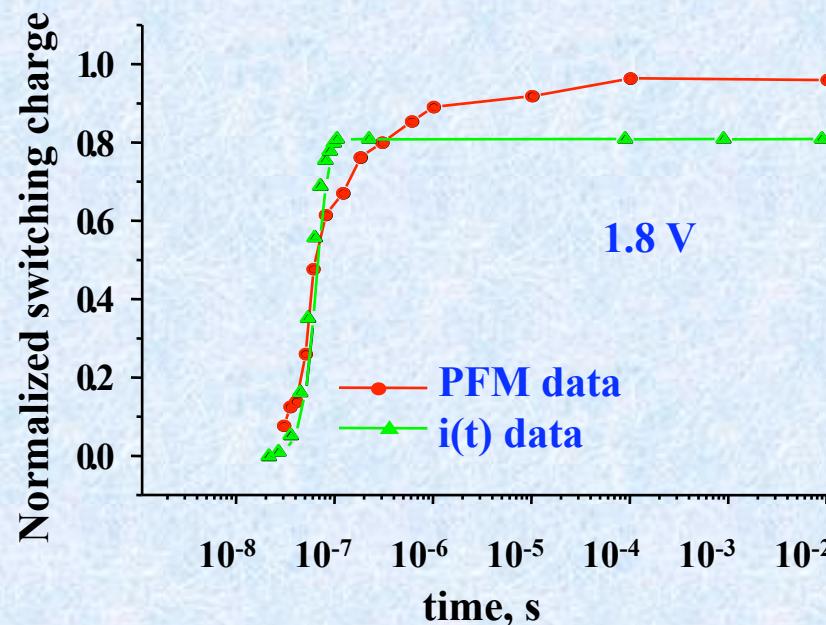
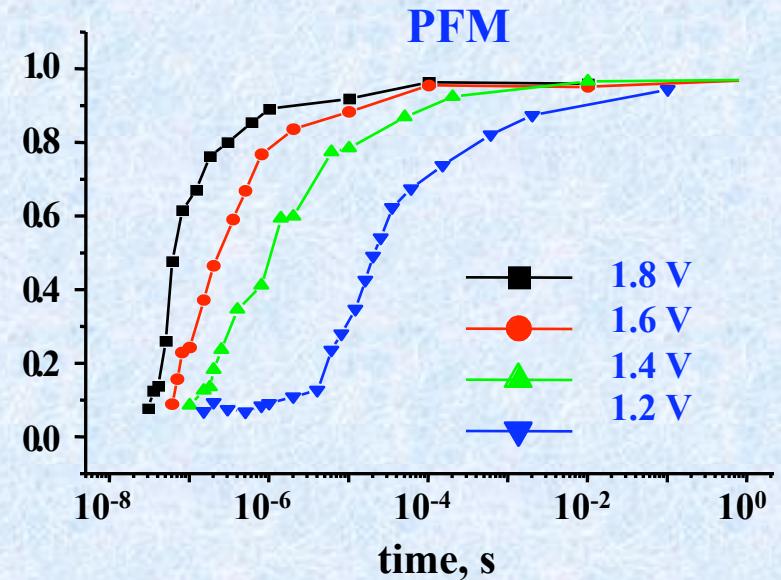
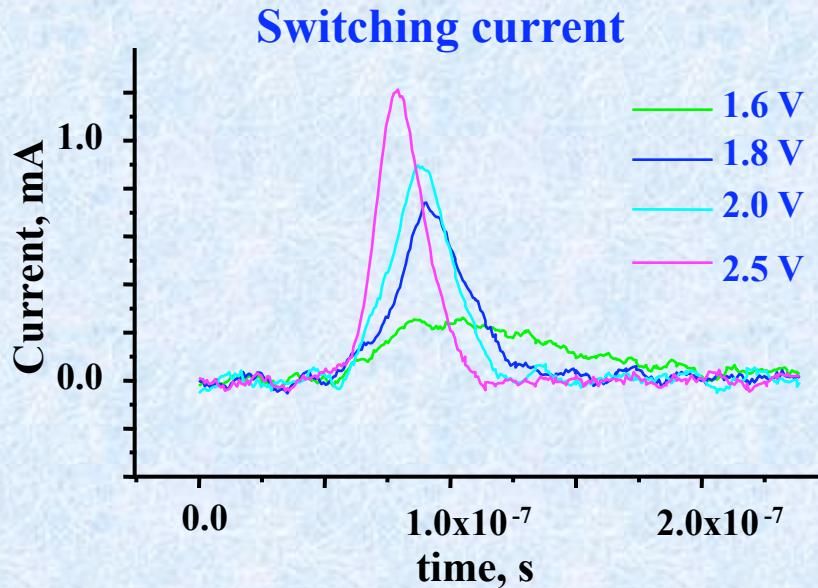
Nucleation rate

Forward growth velocity

Lateral growth velocity

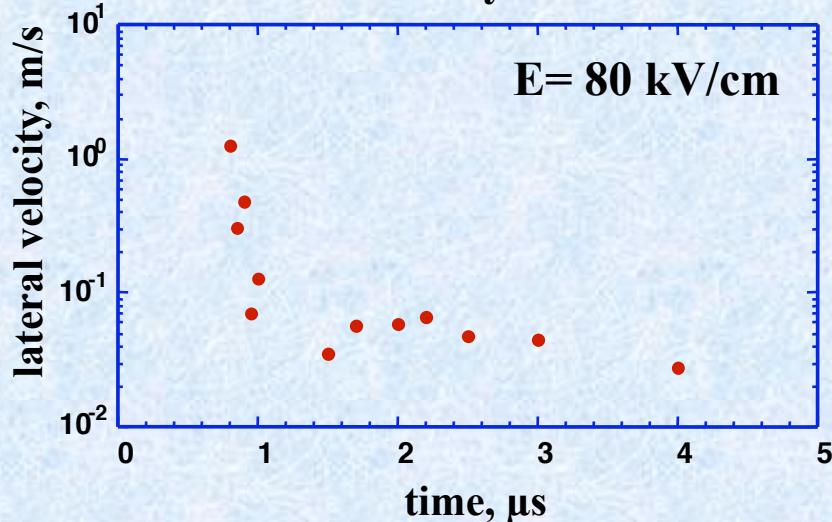


# PFM vs Switching Current



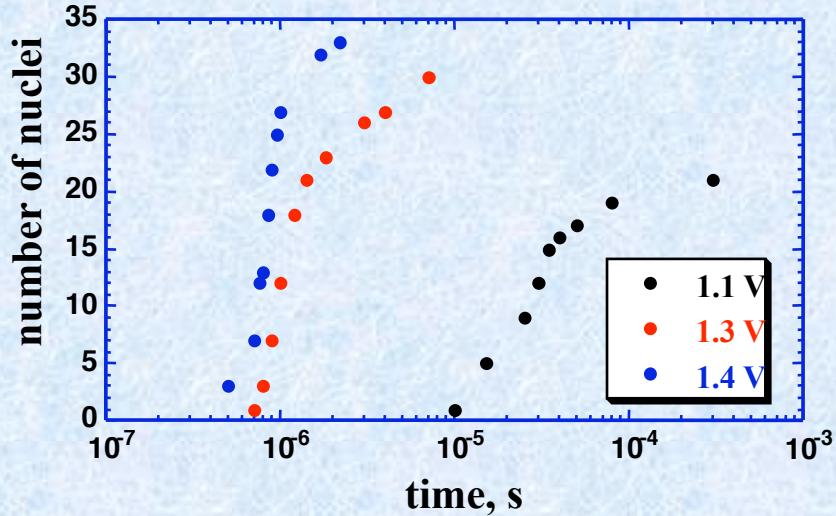
# Parameters of Domain Switching

Wall velocity vs time

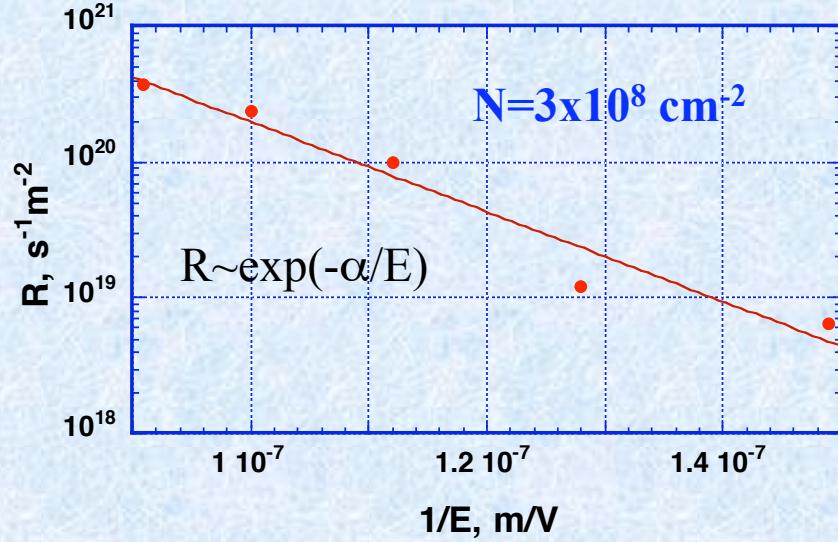


- Wall velocity varies by two orders of magnitude during switching
- Velocity decreases before domain merging with nearby domains
- Area fraction switched via nucleation increases with voltage

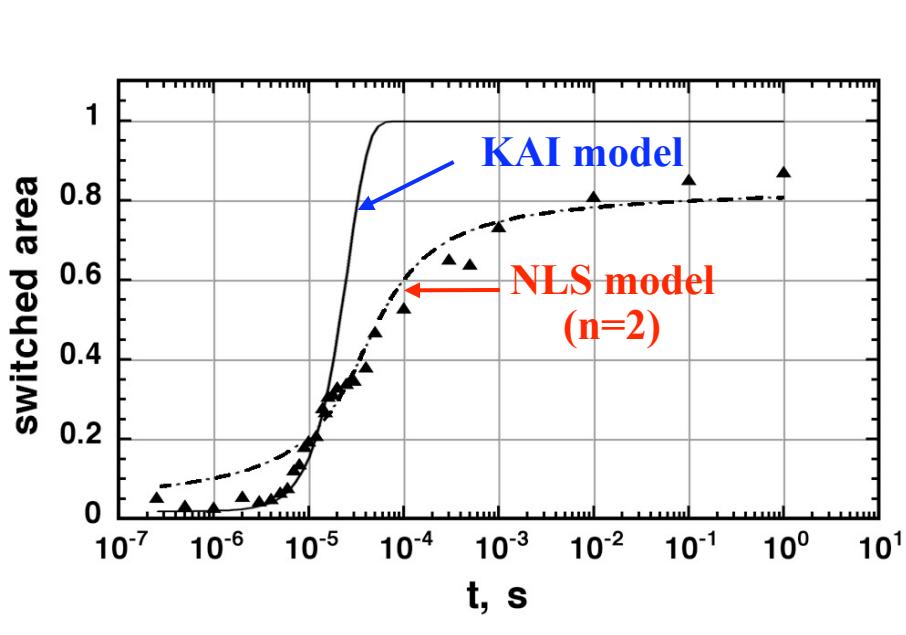
Nucleation rate vs time



Nucleation rate vs E



# Fitting Domain Switching Dynamics



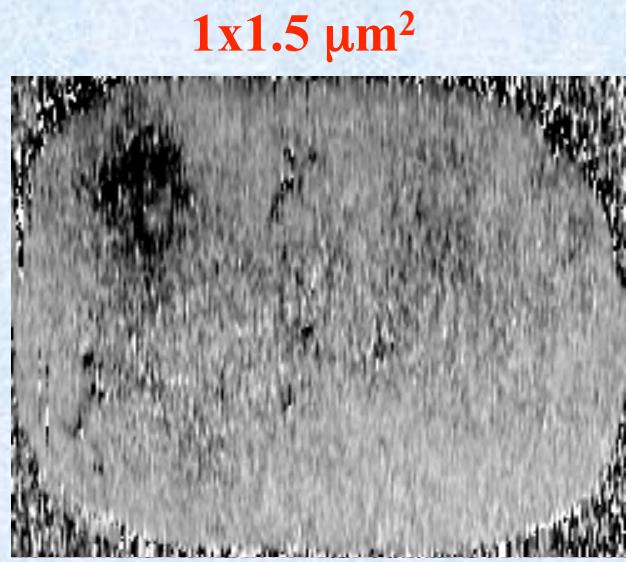
**NLS model: broad distribution of local switching times**

$$\Delta p(t) = 1 - \sum F(\log t_0) e^{-(t/t_0)^n}$$

Experimentally observed domain dynamics differs from the basic assumptions of the KAI model

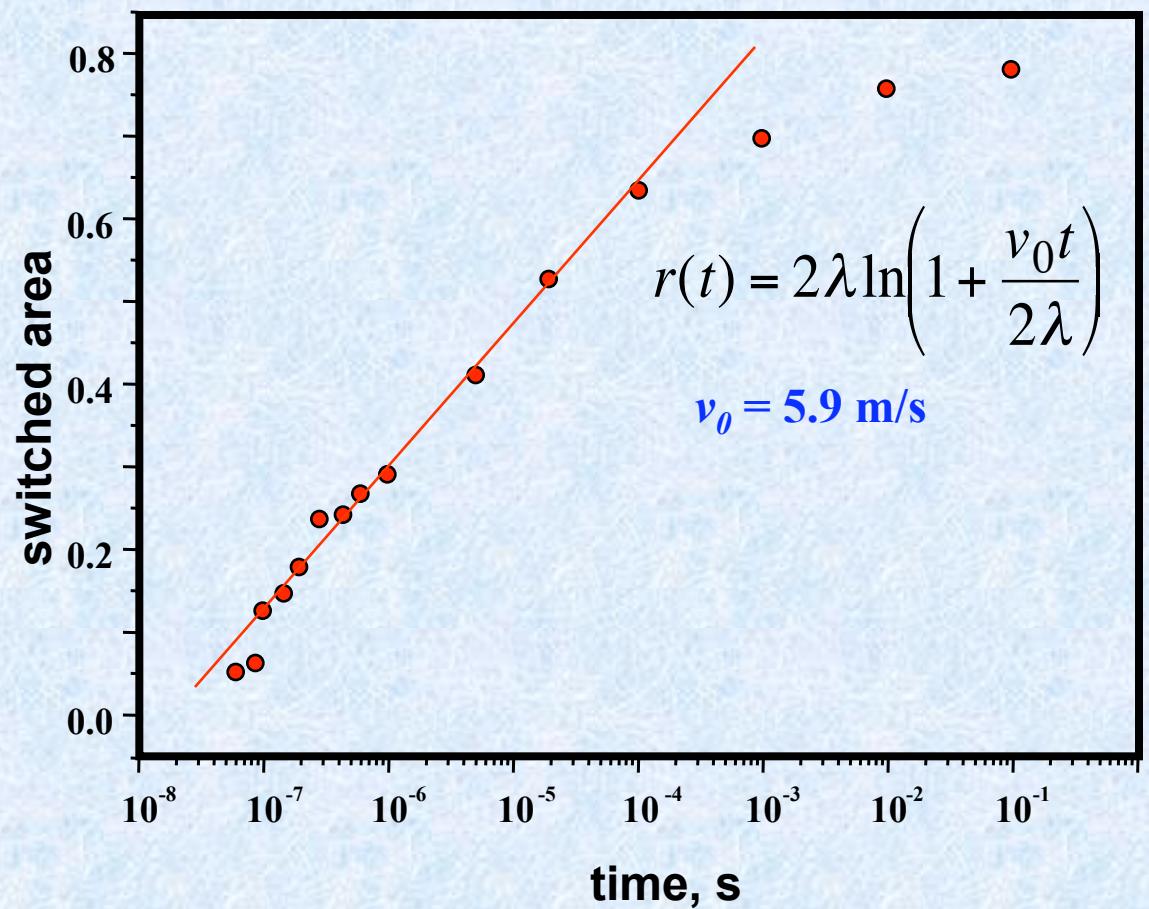
# Domain Switching in Small Capacitors

Capacitor scaling: change in the switching mechanism



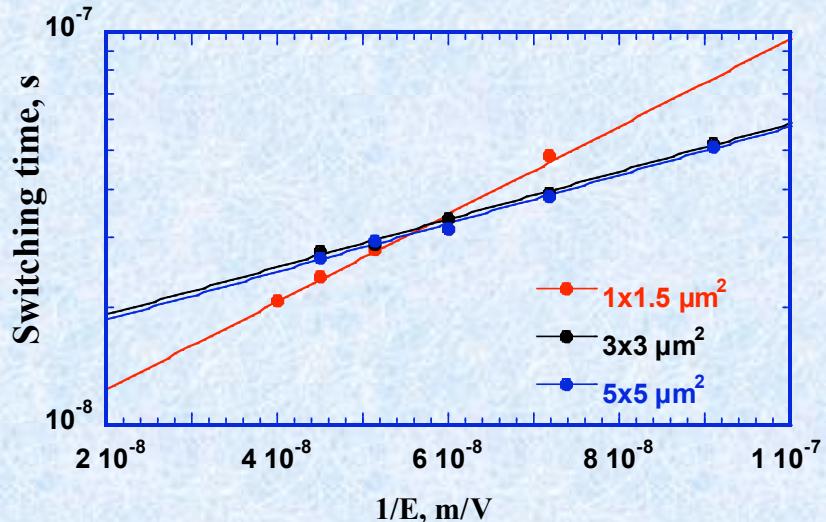
1.6V (1.45  $V_c$ )

- Nucleation is reduced
- Switching is via domain wall



# Capacitor Size Effect

Switching time vs E

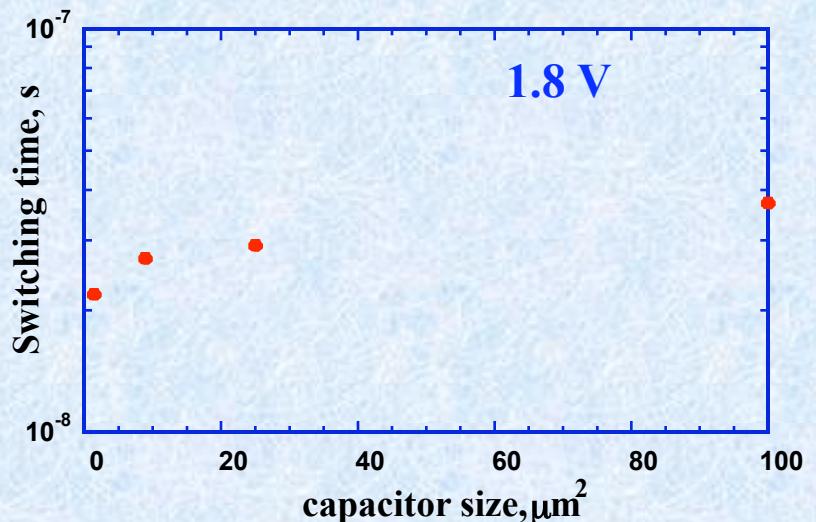


$5 \times 5 \mu\text{m}^2$  capacitor:  $\alpha = 1.4 \cdot 10^5 \text{ V/cm}$

$3 \times 3 \mu\text{m}^2$  capacitor:  $\alpha = 1.4 \cdot 10^5 \text{ V/cm}$

$1 \times 1.5 \mu\text{m}^2$  capacitor:  $\alpha = 2.6 \cdot 10^5 \text{ V/cm}$

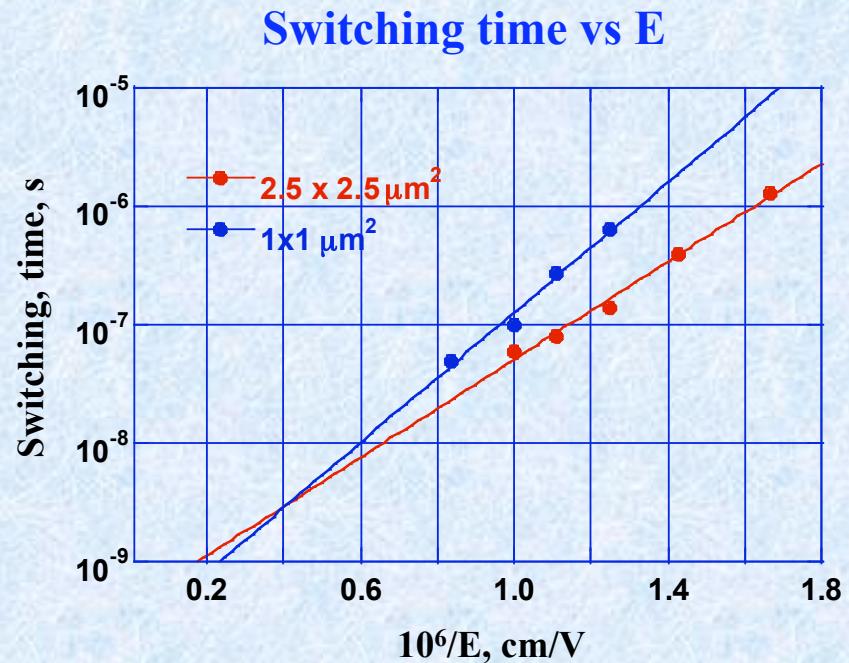
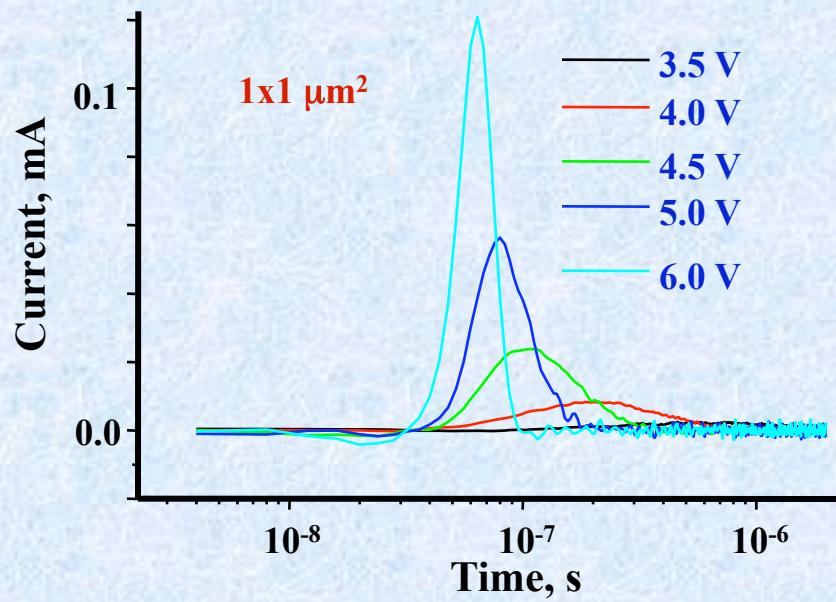
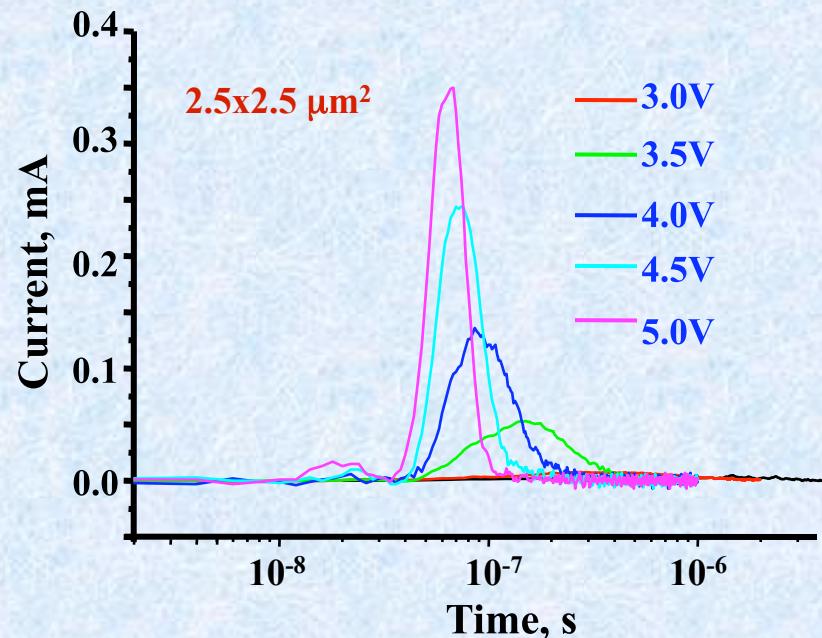
Switching time vs capacitor size



## Capacitor scaling:

- Decrease in a number of nuclei
- Larger contribution of wall motion to polarization reversal with decrease in capacitor size
- Both NLS and KAI model fail to describe the switching kinetics in small capacitors

# Switching Behavior of Epitaxial Capacitors



$$t_{sw} = t_0 \exp(\alpha / E)$$

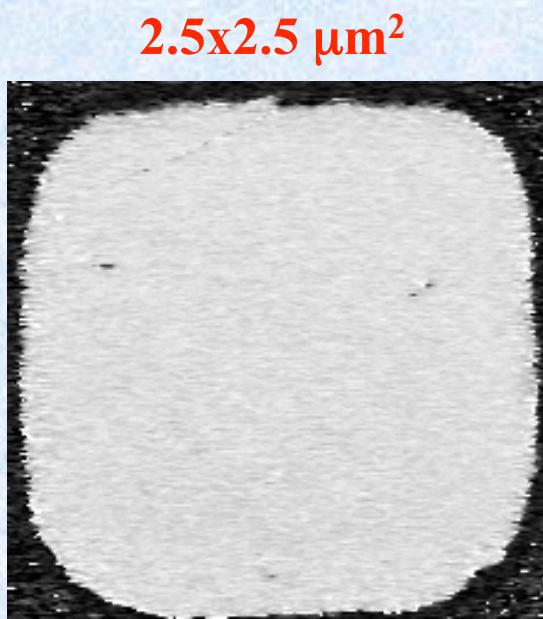
$2.5 \times 2.5 \mu\text{m}^2$  capacitor:  $\alpha = 4.8 \cdot 10^6 \text{ V/cm}$

$1 \times 1 \mu\text{m}^2$  capacitor:  $\alpha = 6.3 \cdot 10^6 \text{ V/cm}$

# Domain Switching in Epitaxial Capacitors

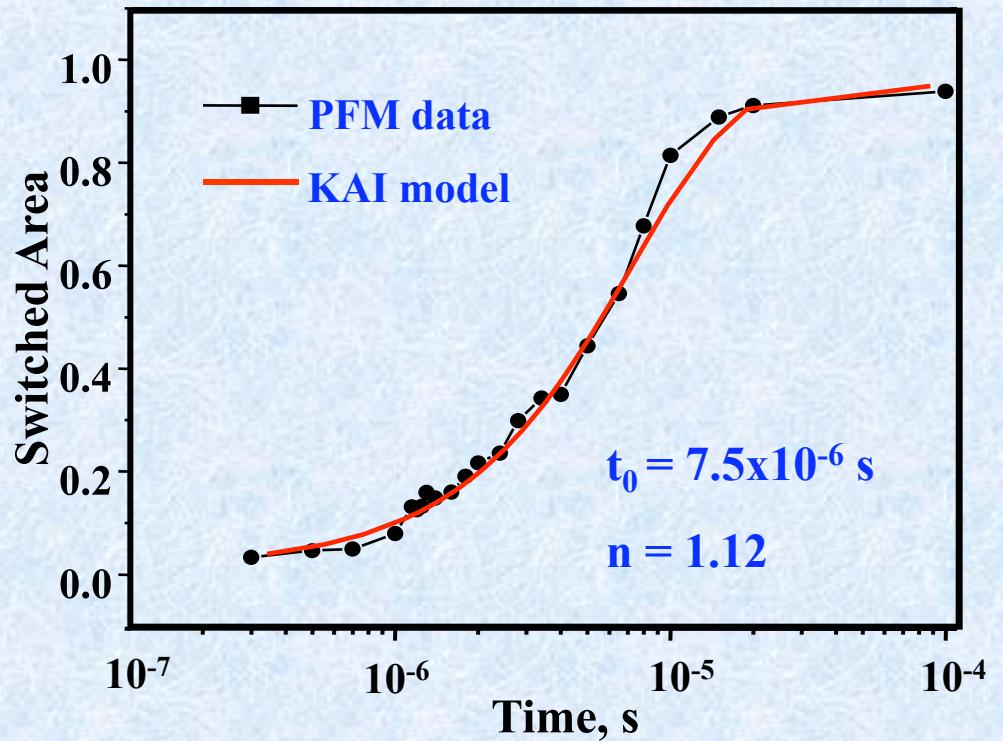
Coercive voltage: 2.0 V

$P_s = 90 \mu\text{C}/\text{cm}^2$



2.5V (1.38  $V_c$ )

- Smaller number of nucleation sites due to the improved film/electrode interface ( $N=8 \times 10^7 \text{ cm}^{-2}$ )
- Strong anisotropy of wall velocity



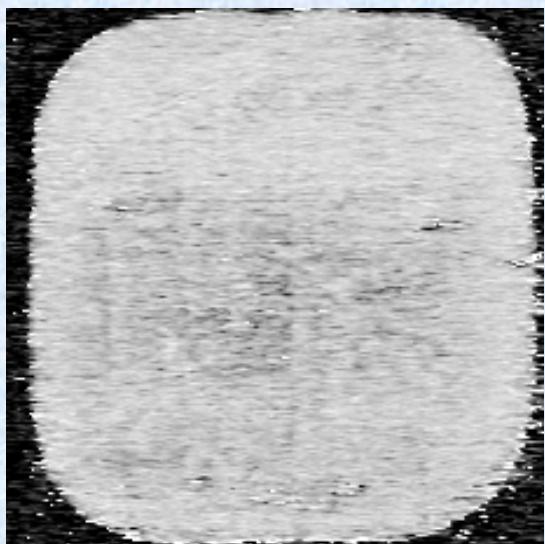
Sample courtesy M. Alexe

# Domain Switching in Epitaxial Capacitors

Coercive voltage: 2.0 V

$P_s = 90 \mu\text{C}/\text{cm}^2$

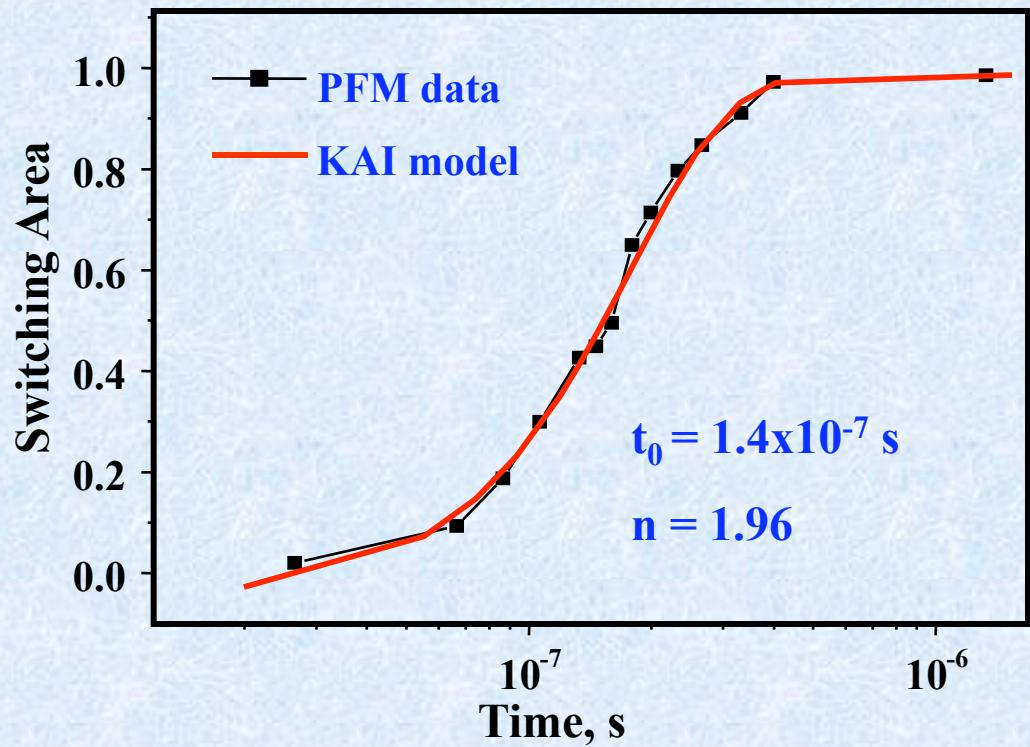
$2.5 \times 2.5 \mu\text{m}^2$



$3.5\text{V}$  ( $1.9 V_c$ )

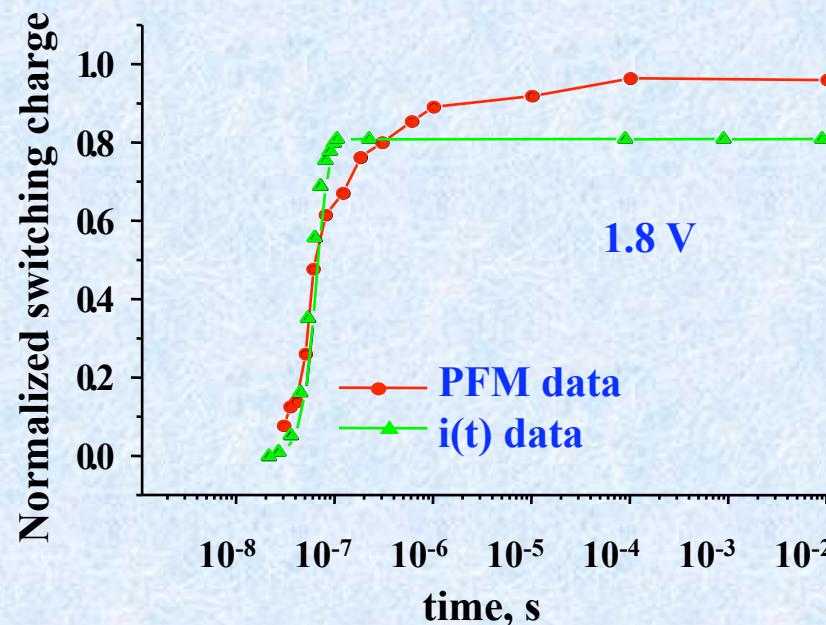
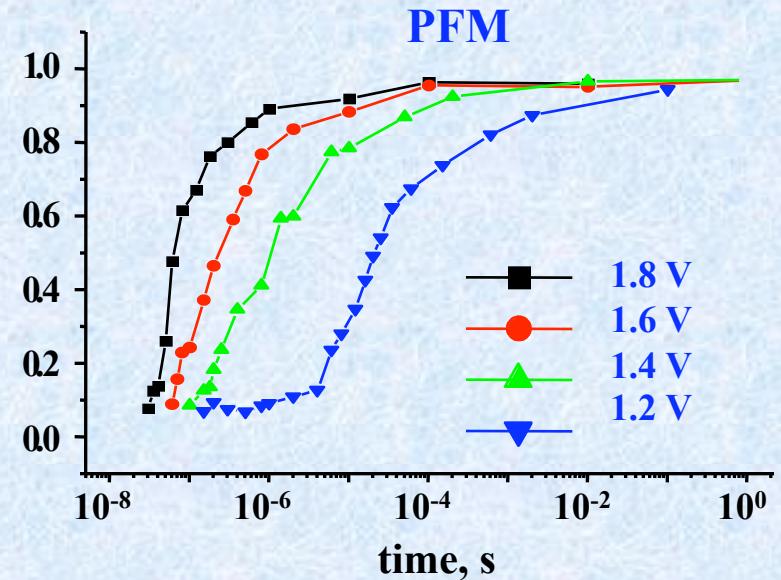
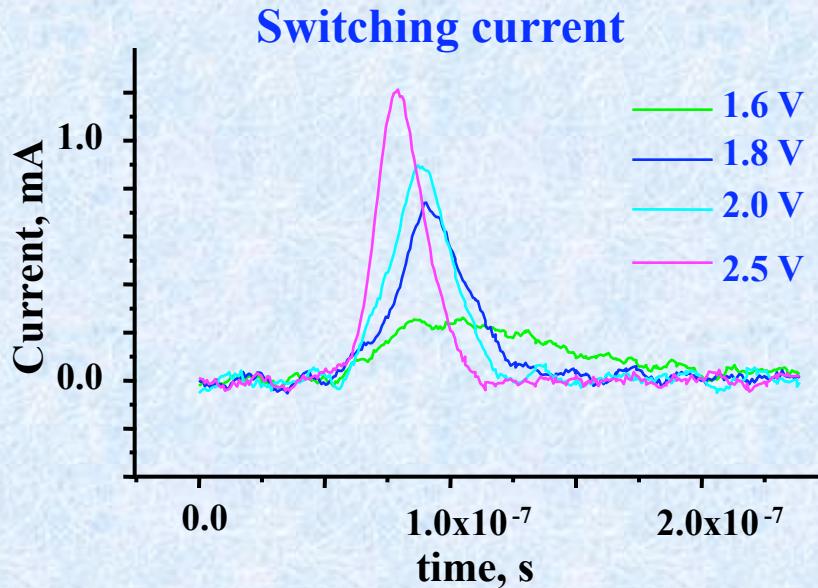
Nucleation density

$N = 7 \times 10^8 \text{ cm}^{-2}$

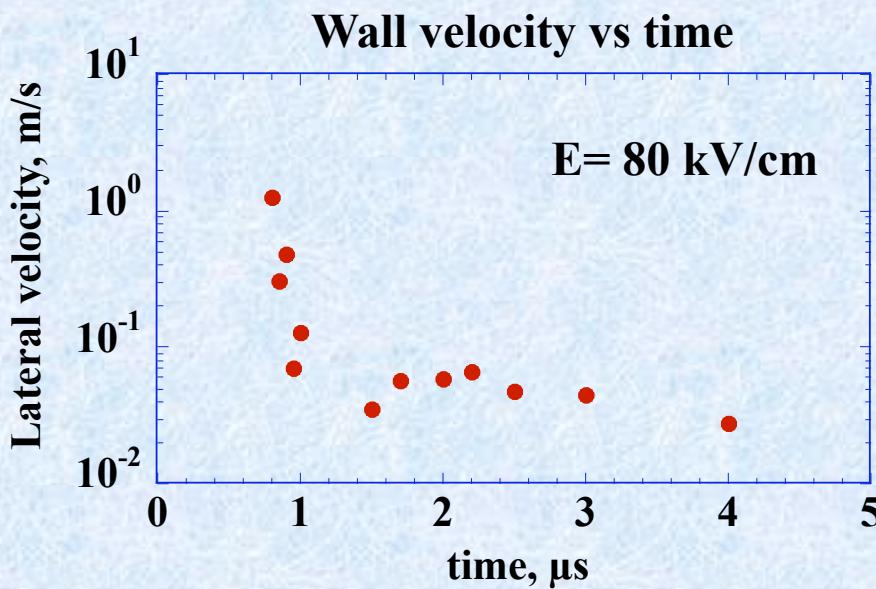
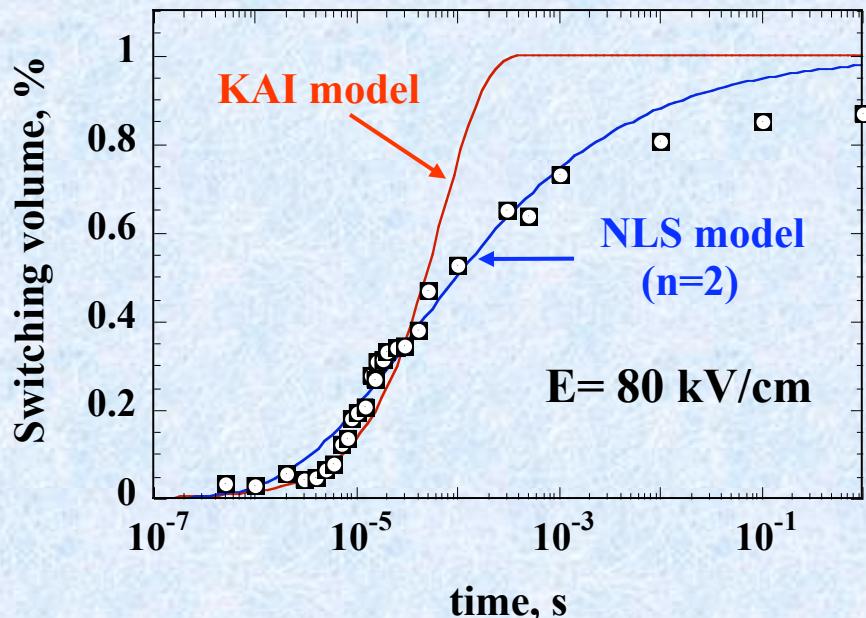


Sample courtesy M. Alexe

# PFM vs Switching Current



# Fitting Domain Switching Dynamics



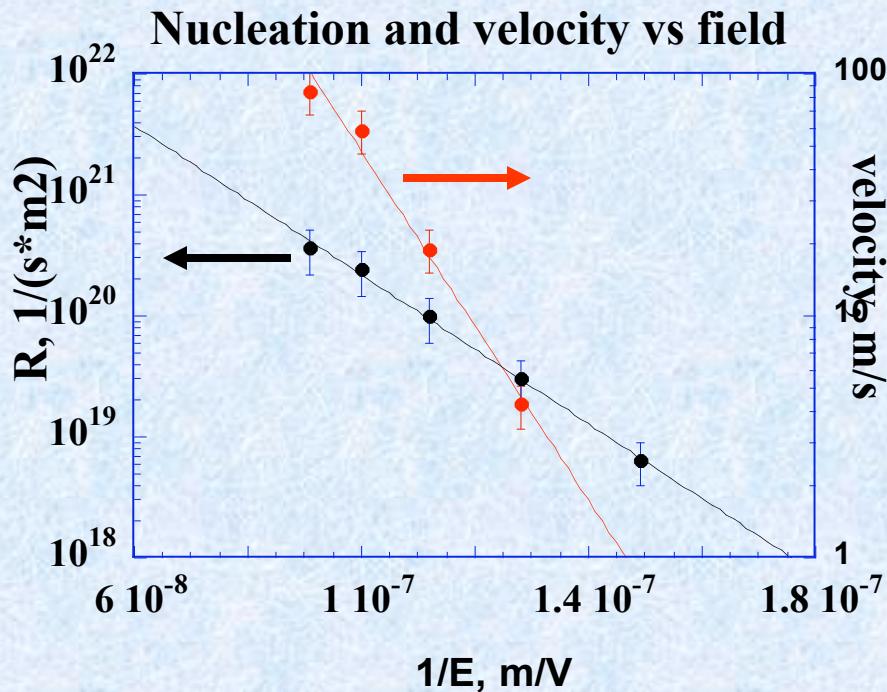
- Polycrystalline PZT films: broad distribution of local switching times

$$\Delta p(t) = 1 - \sum F(\log t_0) e^{-(t/t_0)^n}$$

Experimentally observed domain dynamics differs from the basic assumptions of the KAI model

- Wall velocity varies significantly during switching
- Area fraction switched via nucleation increases with voltage

# Parameters of Domain Switching Kinetics



A difference between  $\alpha_n$  and  $\alpha_w$  activation fields implies transition from wall-limited to nucleation limited switching: in high fields, nucleation becomes a rate-limiting parameter.

Two main mechanisms of switching in large capacitors:

- nucleation  $\alpha_n = 7.1 \cdot 10^7 \text{ V/cm}$
- wall motion  $\alpha_w = 8.3 \cdot 10^7 \text{ V/cm}$

- Nucleation rate

$$R = R_\infty \exp(-\alpha_n / E)$$

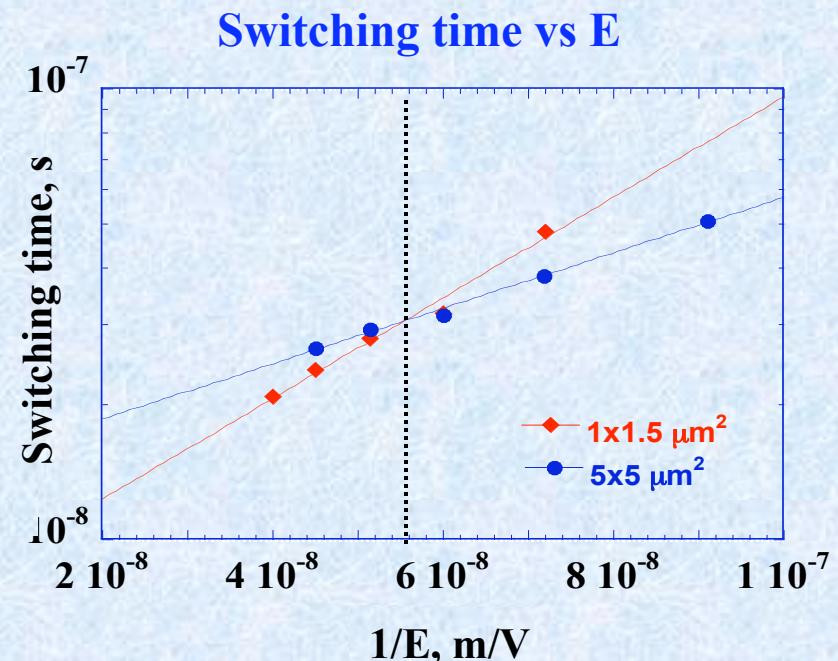
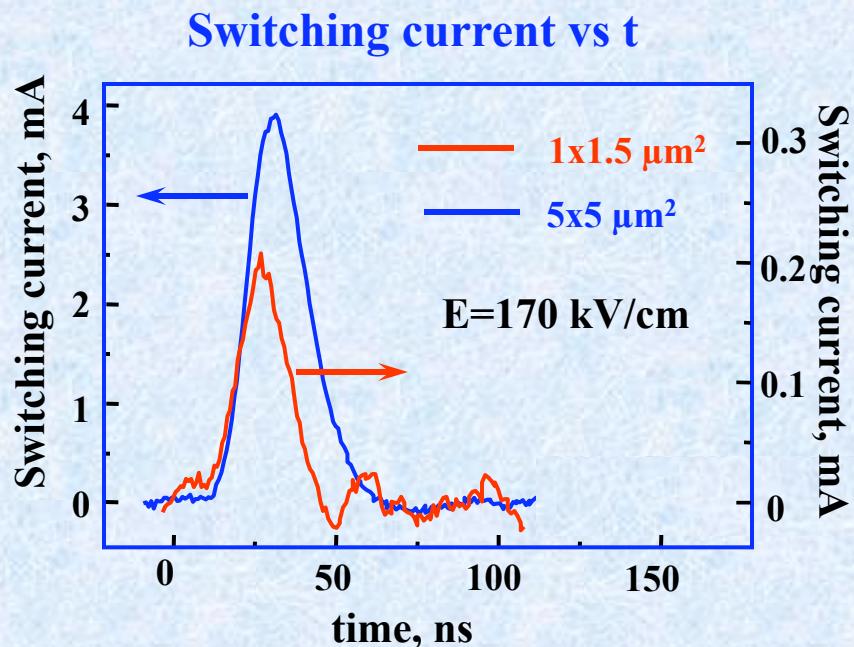
$$\alpha_n = 7.1 \cdot 10^7 \text{ V/cm}$$

- Wall velocity

$$v = v_\infty \exp(-\alpha_w / E)$$

$$\alpha_w = 8.3 \cdot 10^7 \text{ V/cm}$$

# Capacitor Scaling Effect on Switching



Small capacitors switch faster than large capacitors at high fields ( $> 150 \text{ kV/cm}$ ) but more slowly at low fields.

$5 \times 5 \mu\text{m}^2$  capacitor:  $\alpha = 1.4 \cdot 10^5 \text{ V/cm}$

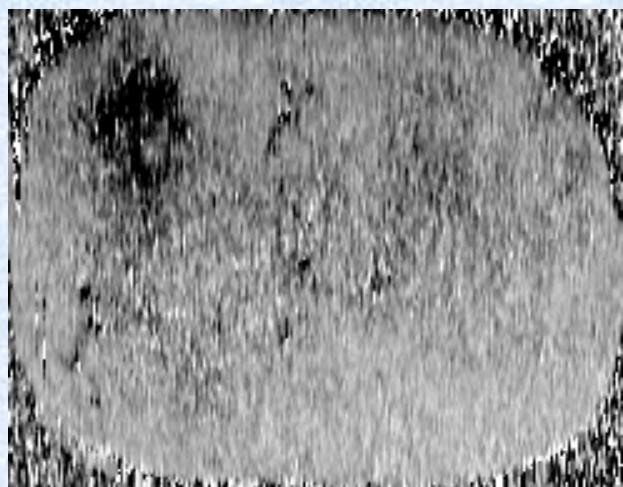
$3 \times 3 \mu\text{m}^2$  capacitor:  $\alpha = 1.4 \cdot 10^5 \text{ V/cm}$

$1 \times 1.5 \mu\text{m}^2$  capacitor:  $\alpha = 2.6 \cdot 10^5 \text{ V/cm}$

# Domain Switching in Small Capacitors

Capacitor scaling: change in the switching mechanism

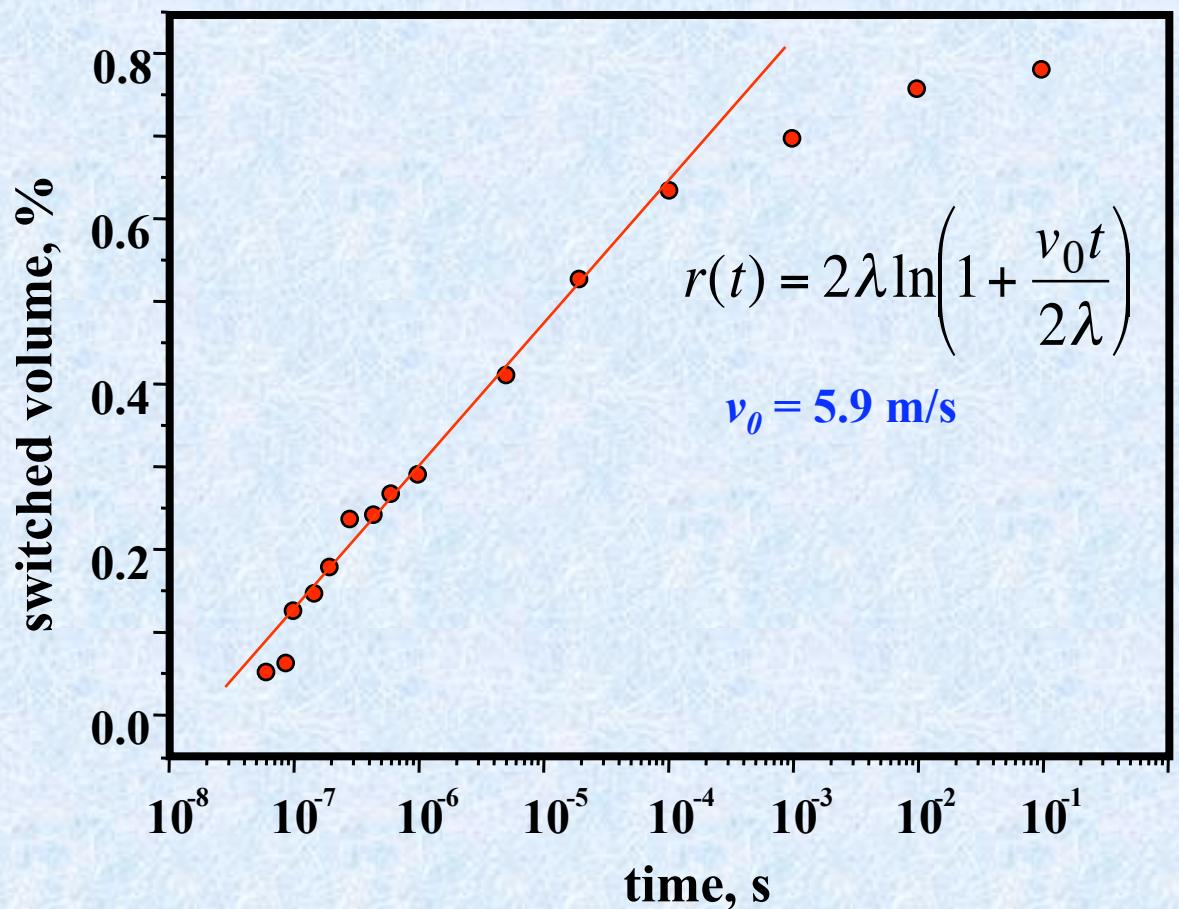
1x1.5  $\mu\text{m}^2$



1.6V ( $\sim 89$  kV/cm)

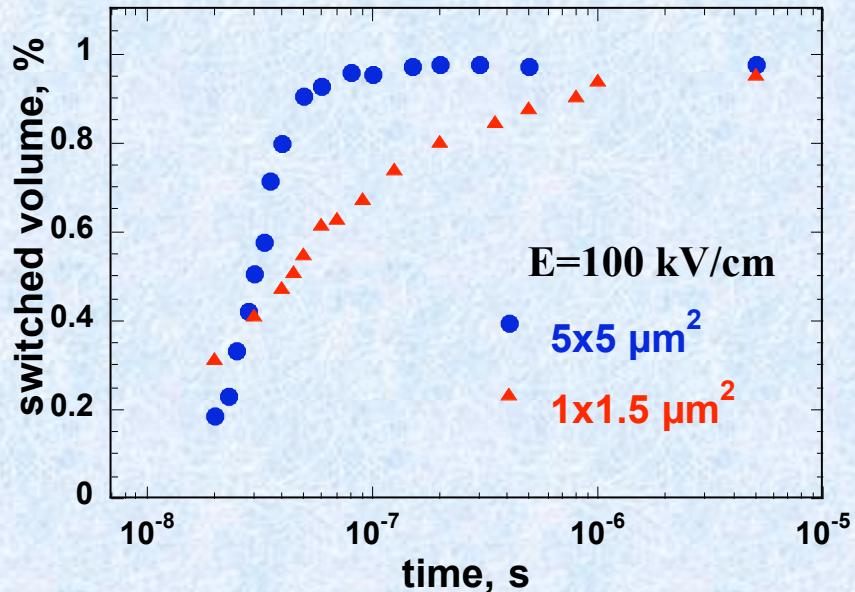
Capacitor scaling:

- Nucleation is reduced
- Switching is via domain wall
- Both NLS and KAI are not applicable



M. Dawber et al, APL 82, 436 (2003)

# Capacitor Scaling Effect on Switching Mechanism

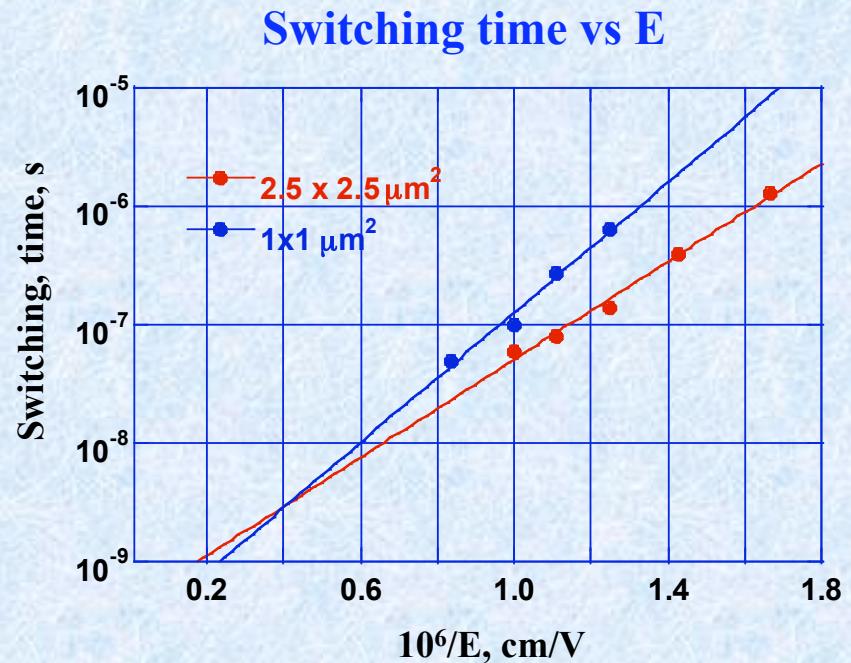
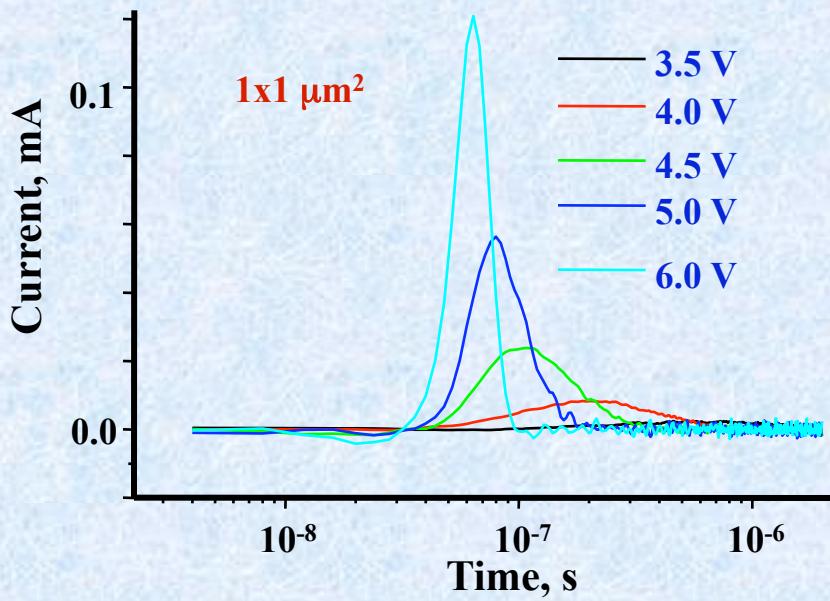
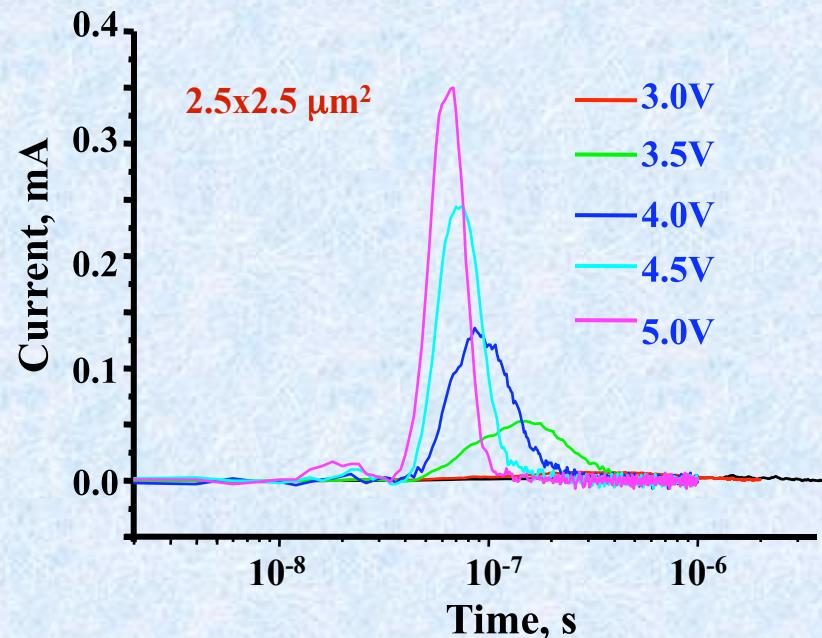


- Low fields ( $<150$  kV/cm): wall motion is a rate-limiting mechanism (small capacitors switch more slowly).
- High fields ( $>150$  kV/cm): nucleation is a rate-limiting mechanism (large capacitors switch more slowly)

Criterion for capacitor size effect on rate-limiting mechanism:

$$\frac{v_\infty}{NR_\infty} \exp\left(\frac{\alpha_n - \alpha_v}{E}\right) \ll A^{3/2}$$

# Switching Behavior of Epitaxial Capacitors

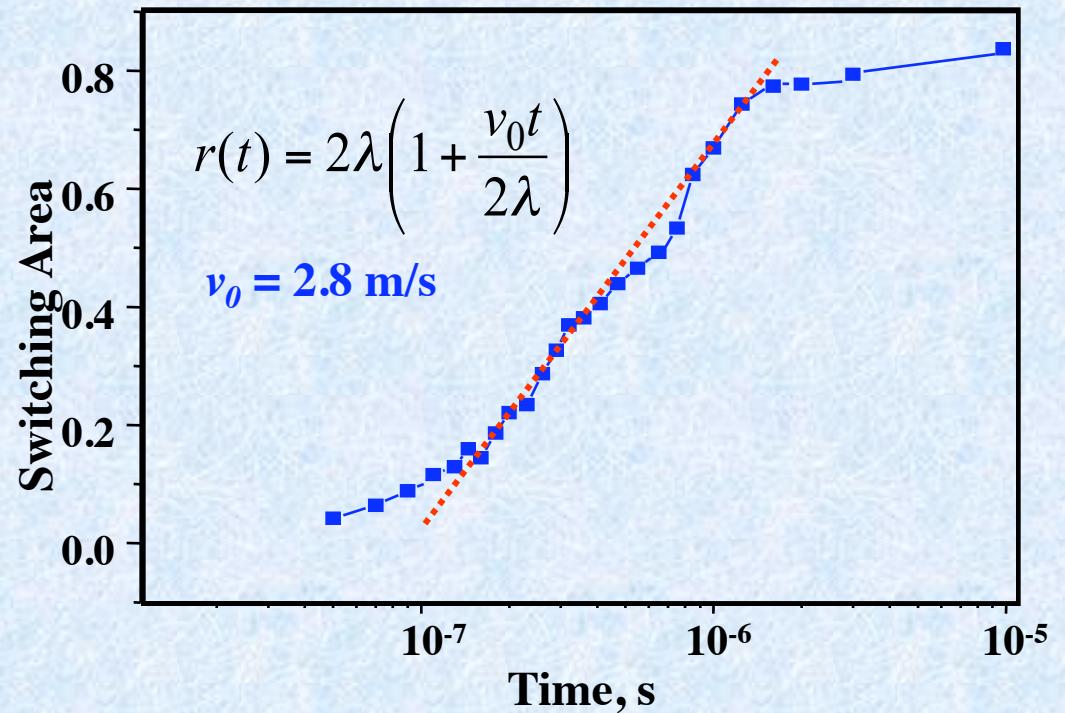
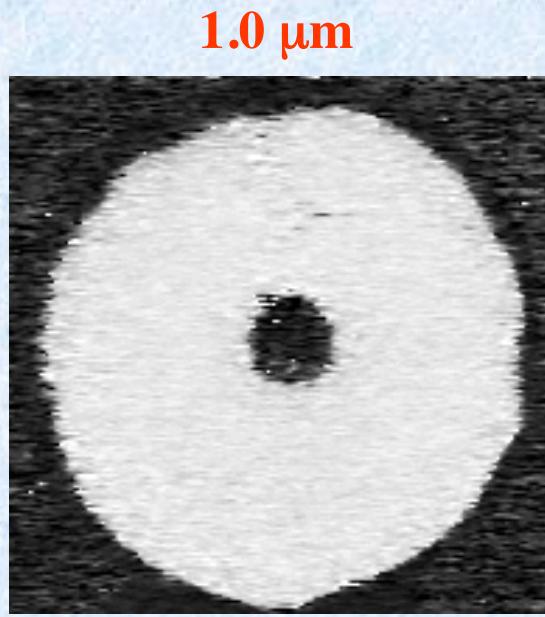


$$t_{sw} = t_0 \exp(\alpha / E)$$

$2.5 \times 2.5 \mu\text{m}^2$  capacitor:  $\alpha = 4.8 \cdot 10^6 \text{ V/cm}$

$1 \times 1 \mu\text{m}^2$  capacitor:  $\alpha = 6.3 \cdot 10^6 \text{ V/cm}$

# Domain Kinetics in Small Epitaxial Capacitors



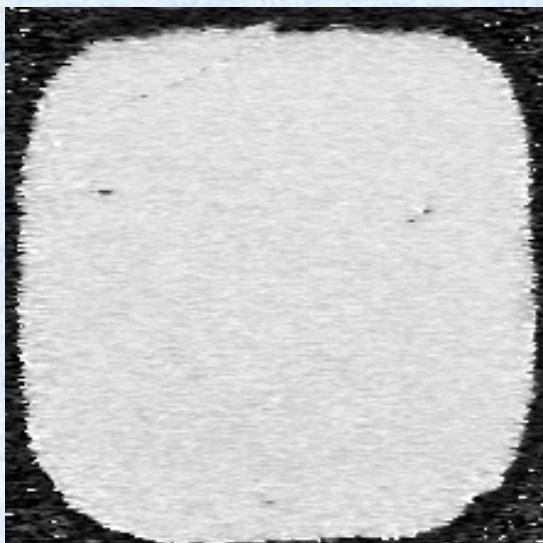
- Strong perimeter effect
- Reduced nucleation
- Pinned region in the center
- Dynamic vortex domain?

# Domain Kinetics in Epitaxial Capacitors

Coercive voltage: 2.0 V

$P_s = 90 \mu\text{C}/\text{cm}^2$

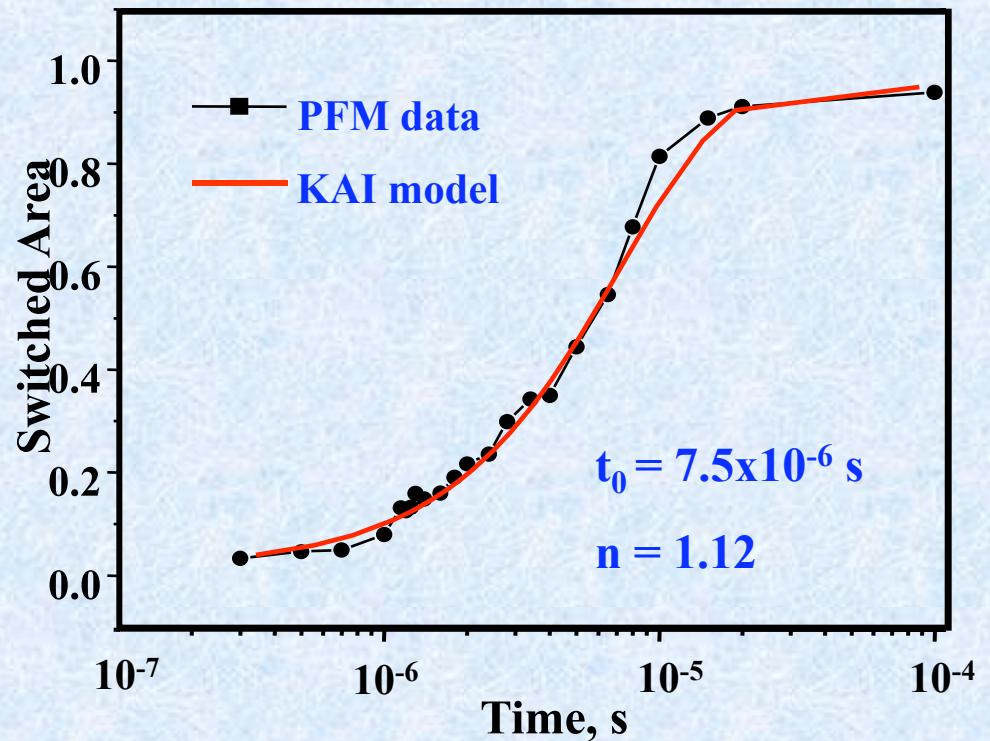
$2.5 \times 2.5 \mu\text{m}^2$



2.5V (1.38  $V_c$ )

- Smaller number of nucleation sites due to the improved film/electrode interface ( $N=8 \times 10^7 \text{ cm}^{-2}$ )
- Strong anisotropy of wall velocity

Kinetics of switching in low fields

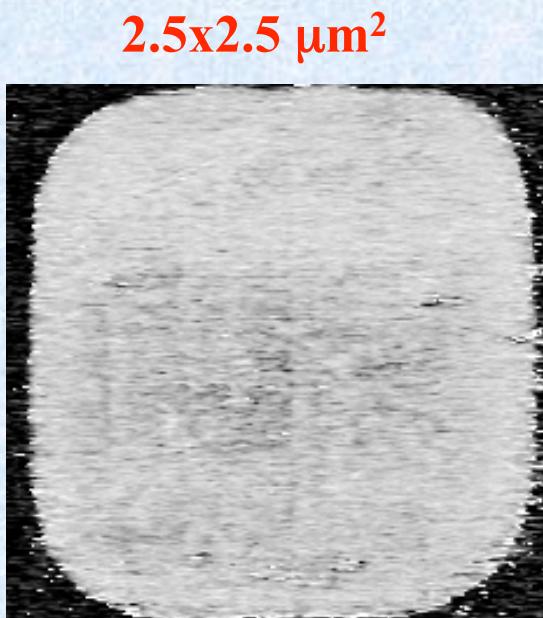


Sample courtesy M. Alexe

# Domain Kinetics in Epitaxial Capacitors

Coercive voltage: 2.0 V

$P_s = 90 \mu\text{C}/\text{cm}^2$

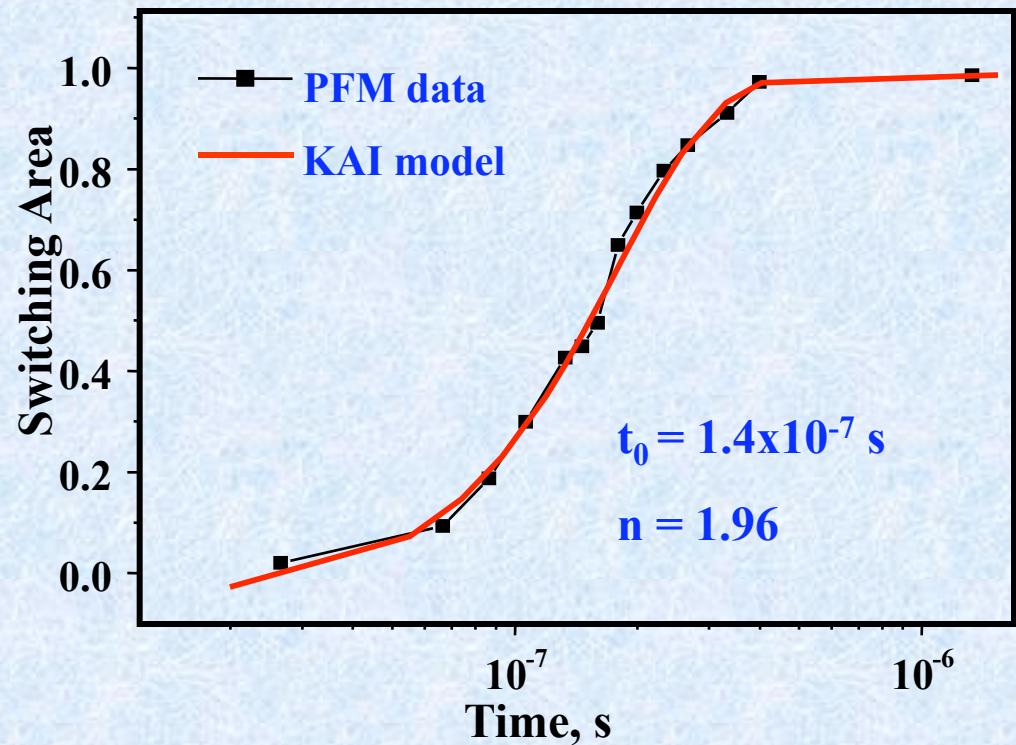


$3.5\text{V}$  ( $1.9 \text{ V}_c$ )

Nucleation density

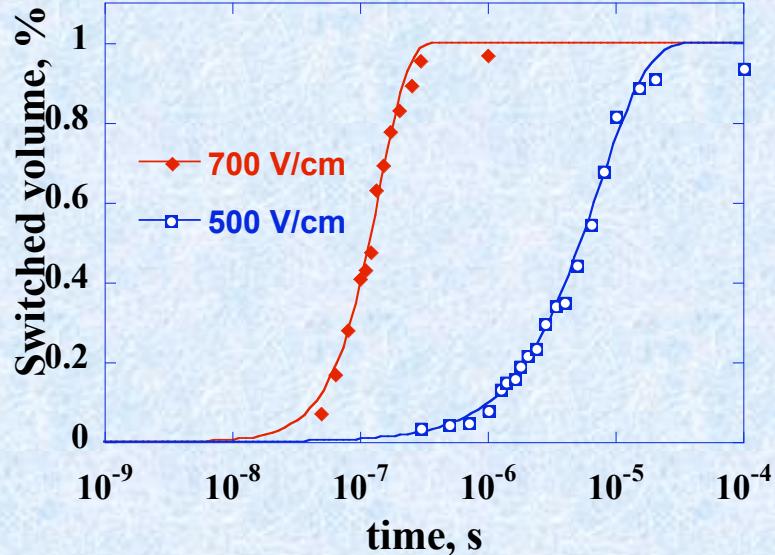
$N = 7 \times 10^8 \text{ cm}^{-2}$

Kinetics of switching in high fields



Sample courtesy M. Alexe

# Fitting Domain Switching Dynamics



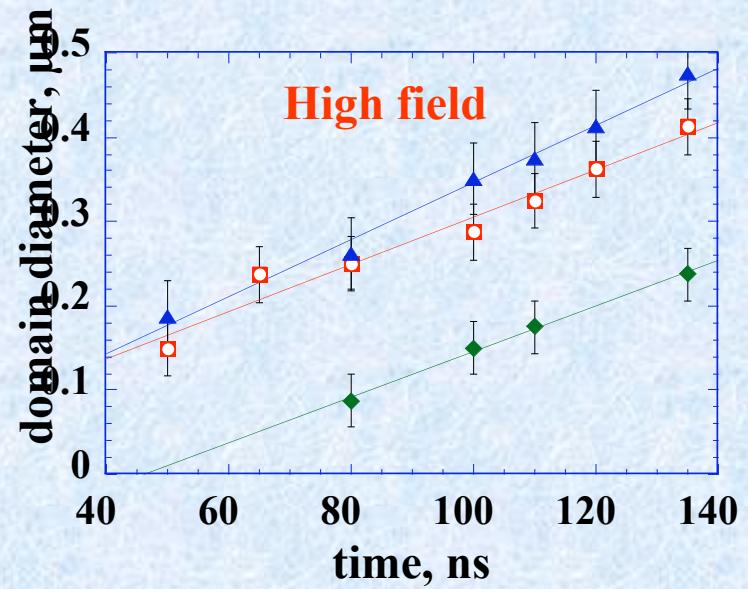
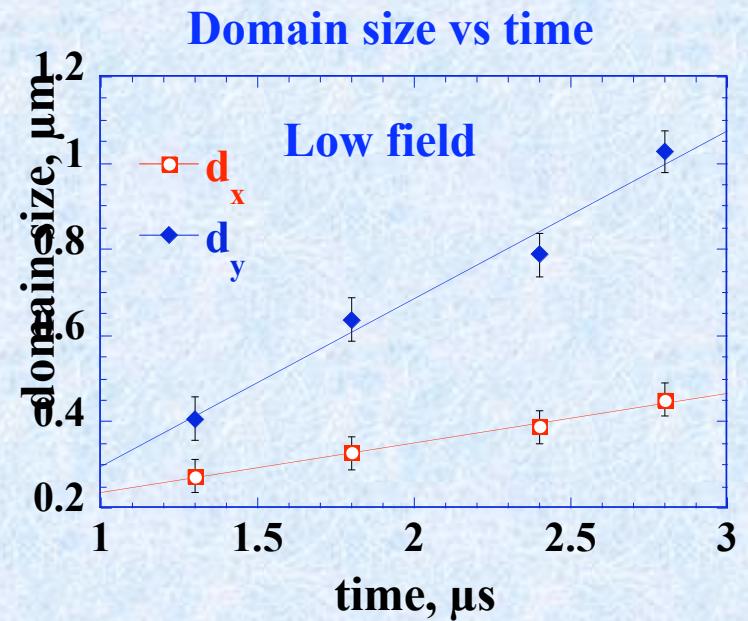
- Epitaxial PZT films: KAI model provides adequate fitting

$$f(t) = 1 - \exp[-(t/t_0)^n]$$

- Field-induced change in the switching mechanism is reflected in domain dimensionality change:

High fields:  $n = 1.96$

Low fields:  $n = 1.12$



# Anisotropy of Domain Wall Motion

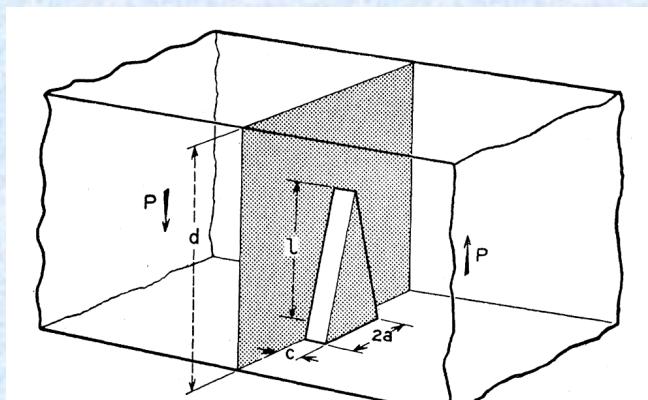
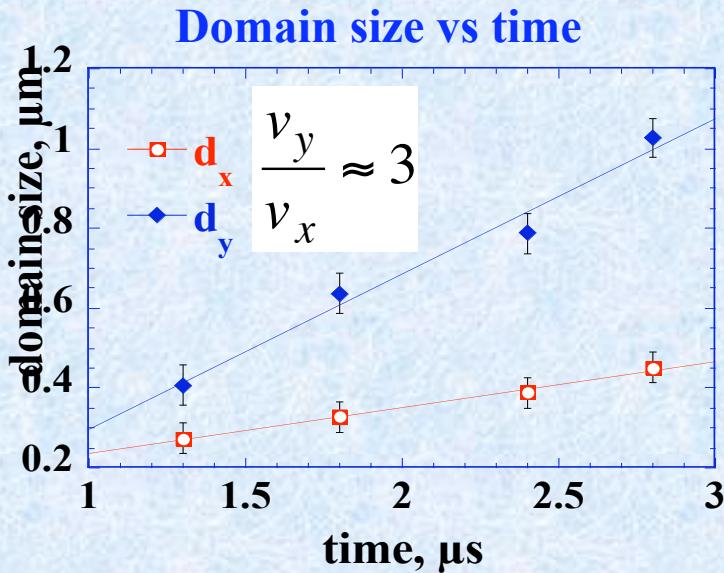


FIG. 1. Schematic drawing of a triangular step on a 180° domain wall. The applied electric field is parallel to the spontaneous polarization on the left side of the figure.

Miller & Weinreich, Phys. Rev. (1960)

**Activation type of wall motion yields**

$$v = v_\infty \exp\left(-\frac{\Delta U}{kT}\right)$$

Then  $\frac{v_y}{v_x} = \exp\left(-\frac{\Delta U_y - \Delta U_x}{kT}\right)$

where  $\Delta U_x, \Delta U_y$  activation energies in x, y directions

Since  $\Delta U = \frac{8b}{3\sqrt{3}} \frac{\sigma_p^{1/2} \sigma_w^{3/2}}{P_s E}$

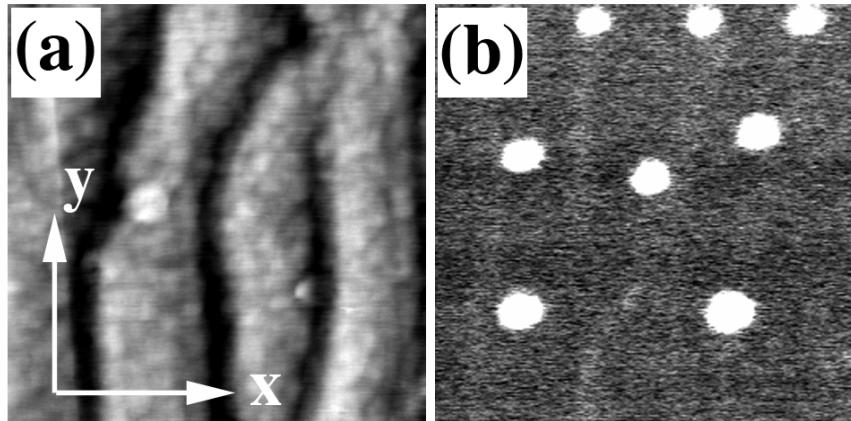
We have  $\frac{\Delta U_x}{\Delta U_y} = \left(\frac{\sigma_{wx}}{\sigma_{wy}}\right)^{3/2}$

$$\sigma_{wx} / \sigma_{wy} = 1.07$$

**Orientational variation of wall energy density by 7% will produce wall velocity anisotropy of factor 3**

# Effect of Microstructure on Domain Wall Motion

Topography and PFM of PZT film surface



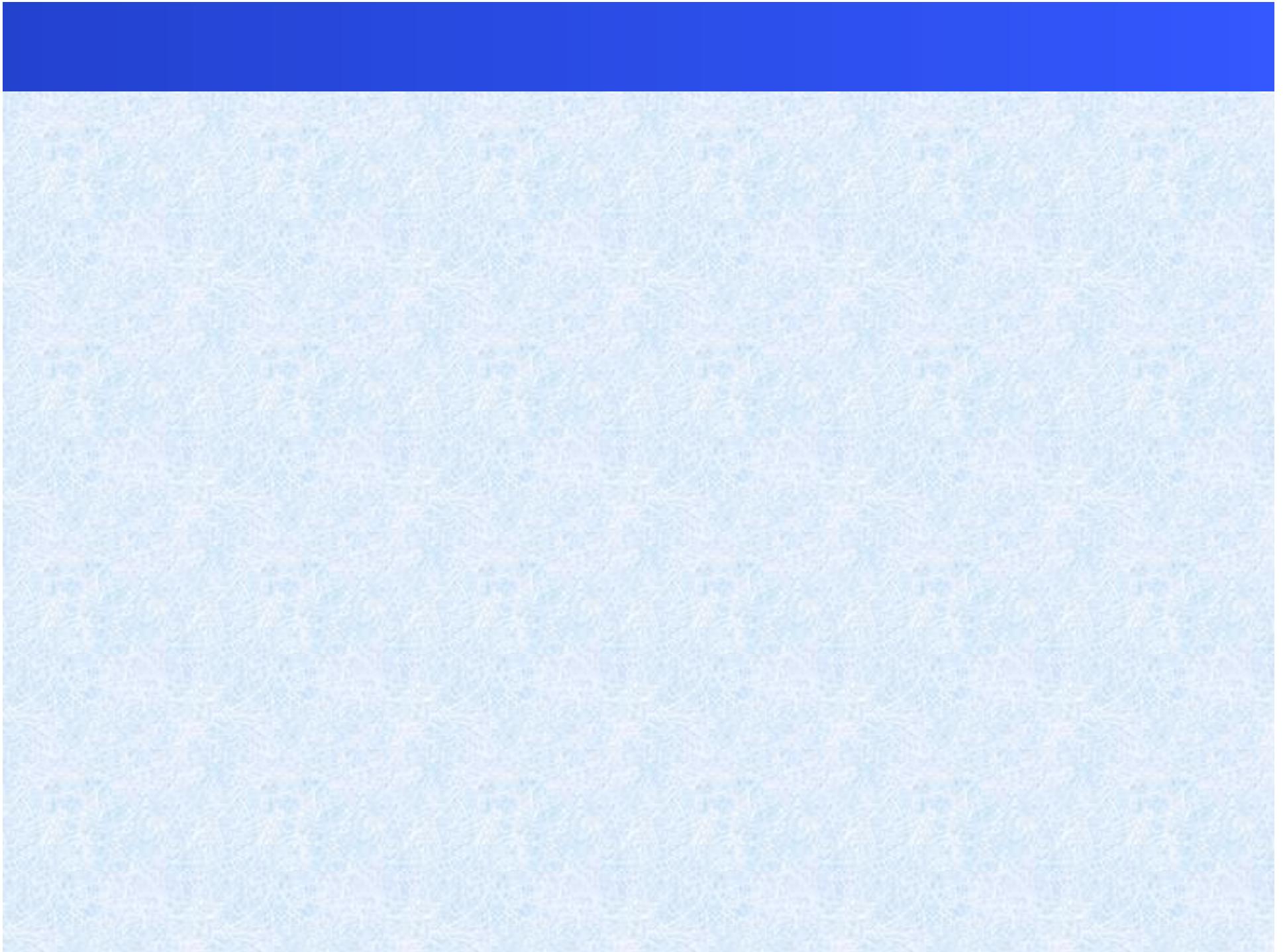
Direction of fast wall motion coincides with the orientation of morphological ridges which may be a reason for anisotropy of wall energy density and anisotropic domain growth in **low fields**.

No anisotropy of domain growth has been observed in PFM tip-induced switching: **in high fields** any directional variations of  $\Delta U$  become negligibly small:

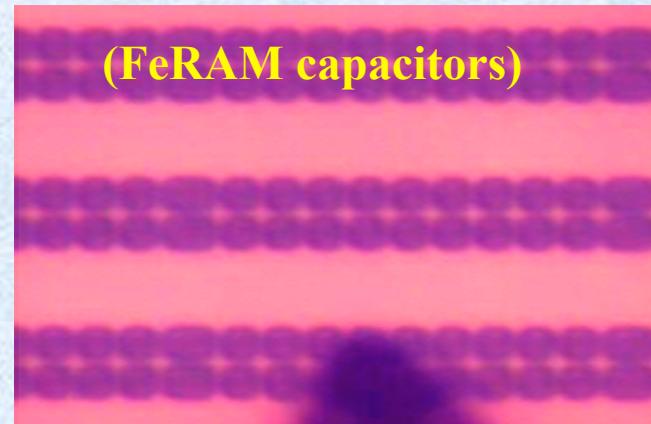
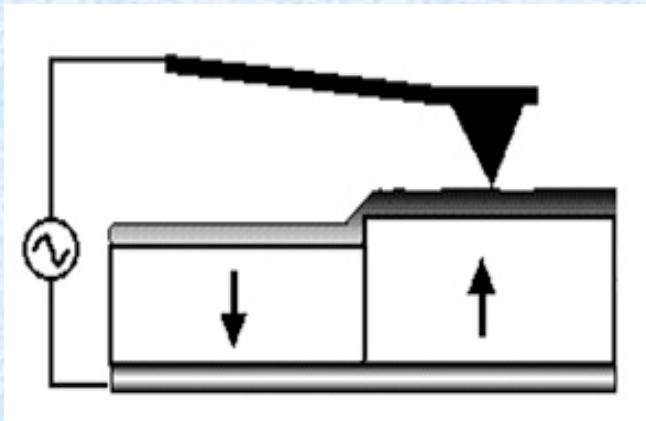
$$\Delta U = \frac{8b}{3\sqrt{3}} \frac{\sigma_p^{1/2} \sigma_w^{3/2}}{P_s E}$$

# Conclusion

- Inhomogeneous nucleation results in cycle-to-cycle reproducibility of switching kinetics which allows application of stroboscopic PFM and direct measurements of domain nucleation rate and wall velocity.
- It has been shown directly that the rate-limiting mechanism depends upon both the capacitor size and field range.
- In small capacitors ( $\sim 1\mu\text{m}^2$ ) switching is dominated by the wall motion (nucleation limited). As a result, in high fields, small capacitors switch faster than large capacitors ( $>> 1\mu\text{m}^2$ ) where nucleation, rate-limiting mechanism, plays significant role. In low fields, wall velocity as a rate-limiting mechanism causes slower switching of small capacitors.
- Capacitor microstructure plays a major role in switching kinetics. In polycrystalline capacitors, broad variation of local switching times leads to NLS-type switching kinetics. In epitaxial capacitors (of even microscale dimensions), KAI model provides adequate description of switching.

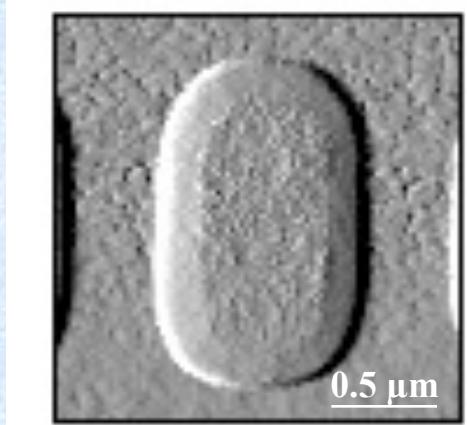


# PFM for Testing Ferroelectric Capacitors

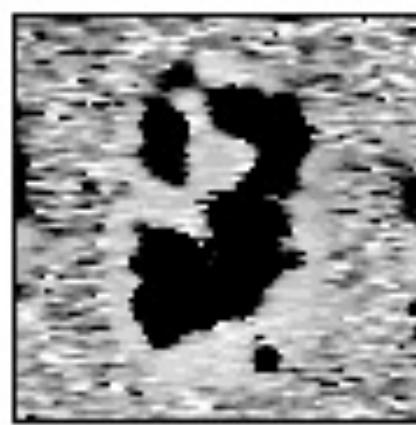


PFM allows delineation of domain patterns in FE capacitors as a function of time and voltage and correlate this information with integral switching parameters (switching charge, coercive voltage, time of switching)

PZT capacitor



PFM phase



PFM amplitude

