

Principles and Applications of Piezoresponse Force Microscopy

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Outline

- ◆ **Introduction**

Ferroelectrics and scanning force microscopy

- ◆ **Piezoresponse Force Microscopy**

Principles, elementary theory

- ◆ **Technical aspects of PFM**

Electromechanic vs electrostatic effect

Vertical vs lateral imaging

Local vs global excitation

- ◆ **PFM and Extrinsic effects**

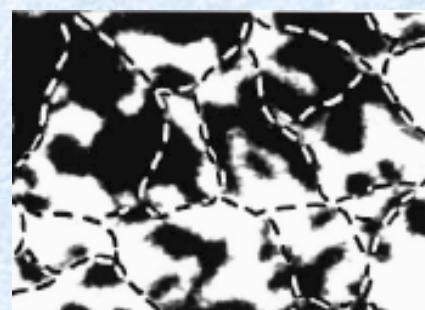
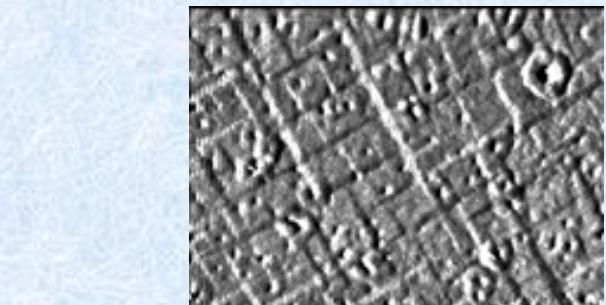
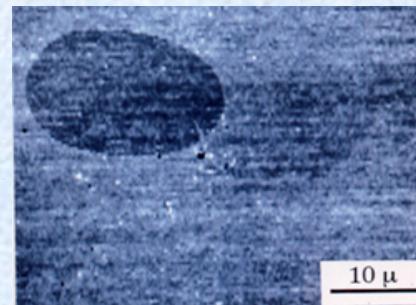
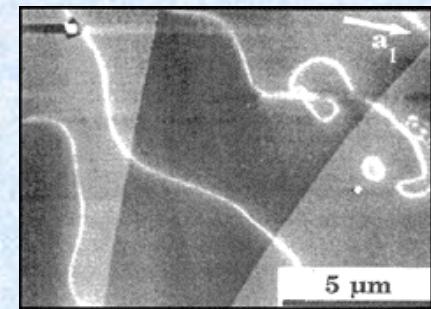
Materials properties and data interpretation

Surface contamination, cross-talk, tip artifacts

- ◆ **Summary**

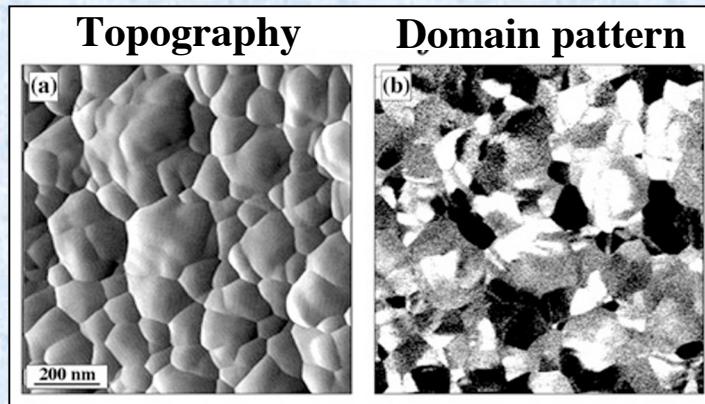
Historical Remarks

- 1986 Invention of the atomic force microscope (Binnig, Quate and Gerber)
- 1989 Quate suggested the use of SFM for imaging of ferroelectric domains
- 1990 First observation of 180° domain walls in GZO crystal by noncontact SFM (Saurenbach and Terris). Resolution is 5 μm
- 1992 Imaging of poled regions in PVDF films (Guethner and Dransfeld)
- 1993 First *nanoscale* observation of 180° domain walls in a GASH crystal by noncontact SFM (Luthi)
- 1994 First *nanoscale* observation of as-grown domains in PZT thin films (Gruverman)
- 1998 PFM switching in nanoscale ferroelectric structures (Alexe)
- 2002 Delineation of optimum imaging in PFM (Kalinin)

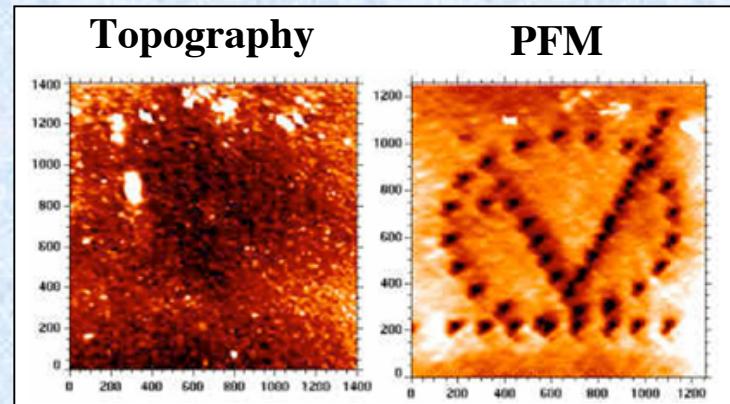


Examples of PFM Capabilities

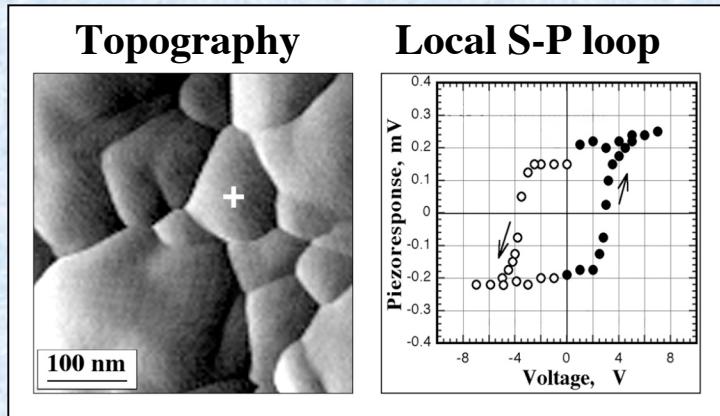
Polarization mapping



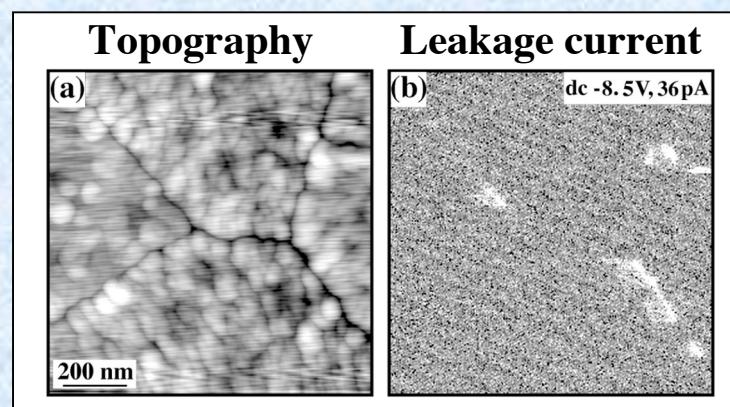
Domain patterning



Local hysteresis loop



Leakage current mapping



Comparison of SPM Methods for Domain Imaging

SPM Method	Advantages	Materials Studied	Drawbacks
EFM, SSPM	<ul style="list-style-type: none"> • Charge • Surface potential • Universal 	Crystals: TGS, GASH, GMO, BaTiO ₃ , PbTiO ₃ , LiNbO ₃	<ul style="list-style-type: none"> • Low-resolution • Surface sensitive
AFM, LFM	<ul style="list-style-type: none"> • High-resolution 	Crystals: TGS, GASH, BaTiO ₃ , PbTiO ₃	<ul style="list-style-type: none"> • Limited applicability • Surface sensitive
SNDM	<ul style="list-style-type: none"> • High-resolution • Dielectric studies • Universal 	<p>Crystals: LiTaO₃, LiNbO₃, SBN</p> <p>Thin films: PZT</p>	<ul style="list-style-type: none"> • Surface sensitive
PFM	<ul style="list-style-type: none"> • High-resolution • Domain control • Capacitors testing • Universal 	<p>Crystals: TGS, BaTiO₃, KTP, PbTiO₃, SBN, LiTaO₃, LiNbO₃</p> <p>Thin films: PZT, SBT, BaTiO₃, PbTiO₃</p>	TBD

Electromechanical Coupling: Motivation to Study

Electromechanical coupling is an essential characteristic of a wide range of inorganic and organic materials alike

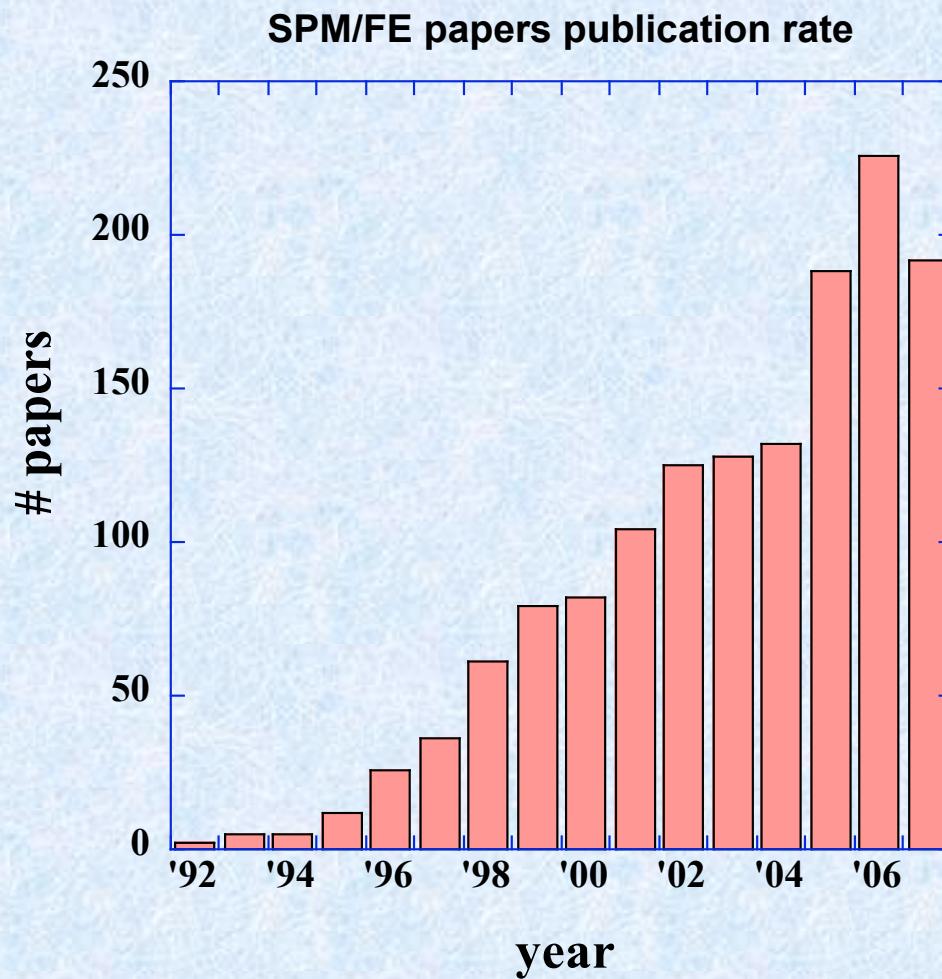
Materials:

- Ferroelectrics: BaTiO₃, Pb(Zr,Ti)O₃, PMN
- Piezoelectrics: ZnO, quartz
- Polymers: PVDF
- III-nitrides: GaN, AlN
- Biological materials: bones, wood, proteins, DNA

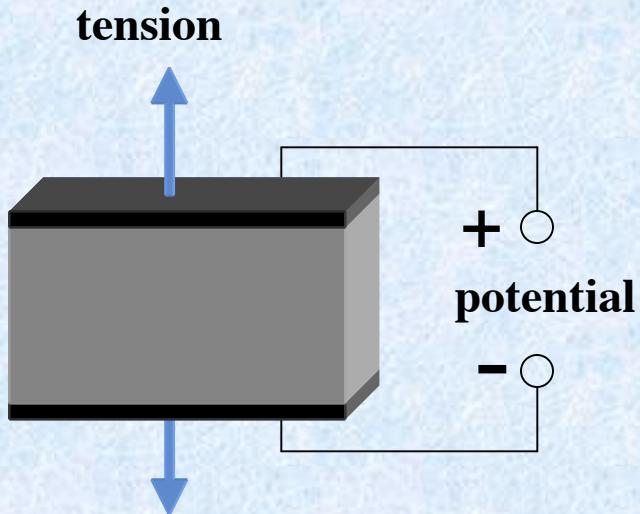
Studies:

- Characterization of electromechanical properties of materials
- Testing of micro- and nanoelectromechanical devices
- Explore relationship between polarity and materials properties
- Nanoscale structural characterization in biomaterials

SPM related publications



Piezoelectric Effect



Direct Piezoelectric Effect

$$D_j = d_{ij}^{dir} S_i$$

Converse Piezoelectric Effect

$$S_j = d_{ij}^{conv} E_i$$

E_m - electric field

S_{ij} - strain

d_{ij} - piezoelectric constant

Piezoelectricity/electrostriction:

- transducers, actuators, MEMS

In an ideal piezoelectric crystal, polarization P is related to mechanical stress s as

$$P_i = d_{ijk} \sigma_{jk}$$

where d_{ijk} - piezoelectric tensor

Piezoelectric tensor

Tetragonal material (4mm):

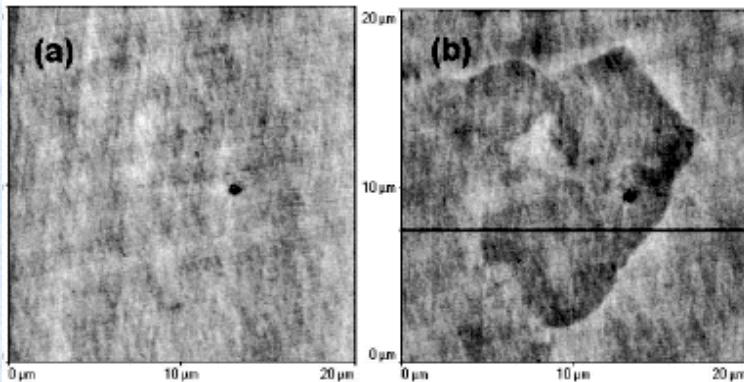
$$\begin{pmatrix} 0 & 0 & 0 & 0 & d_{15} & 0 \\ 0 & 0 & 0 & d_{15} & 0 & 0 \\ d_{31} & d_{31} & d_{33} & 0 & 0 & 0 \end{pmatrix}$$

Non-zero elements are determined by symmetry

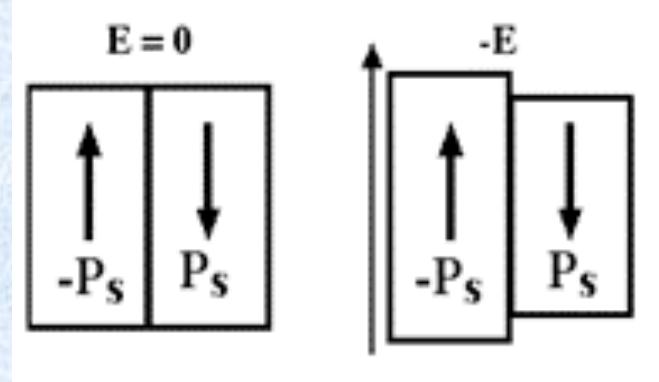
Domain Imaging via Static Piezoresponse

Polarization and piezocoefficients are linked via: $d_{ij} = \epsilon_{im} Q_{jm} P_{sk}$

Pinned domain in SBN crystal (topography); Imaging voltage 200 V, height difference 2 nm



Y.-G. Wang et al, PR B 61 (2000)



In piezoresponse: $\Delta L = \pm d_{33} V$

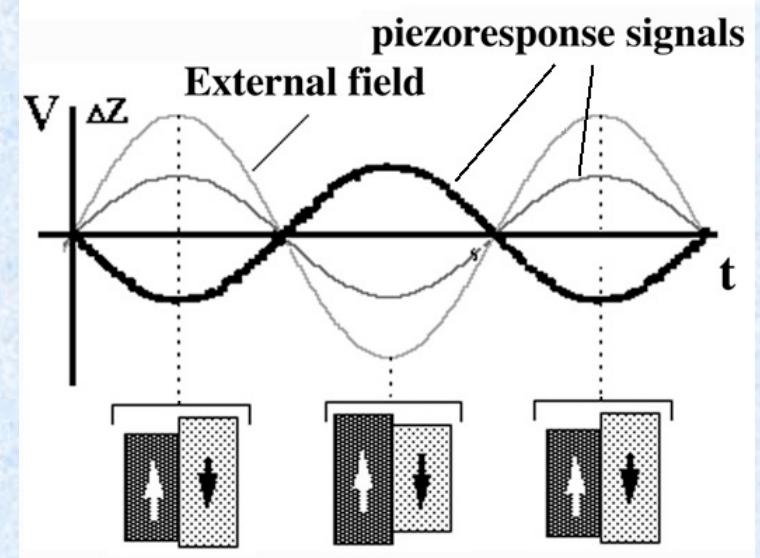
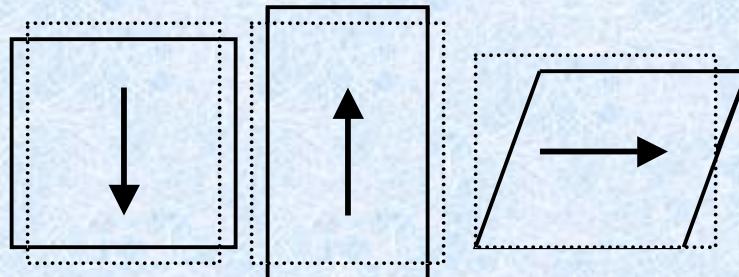
Imaging trade-off:

- The higher V, the better domain resolution
- Non-destructive imaging requires that $V < V_c$

Dynamic Piezoresponse
increases sensitivity
by 3 orders of magnitude

Domain Imaging via Dynamic Piezoresponse

Field is on



$$\text{Field induced strain: } S_j = d_{ij} E_i$$

$$\text{Polarization and piezocoefficients are linked via: } d_{ij} = \epsilon_{im} Q_{jmk} P_{sk}$$

$$\text{Sample deformation: } \Delta L = \pm d_{33} V$$

$$\text{Under modulation voltage } V = V_0 \cos(\omega t), \text{ surface vibrates as } \Delta L = \Delta L_0 \cos(\omega t + \varphi)$$

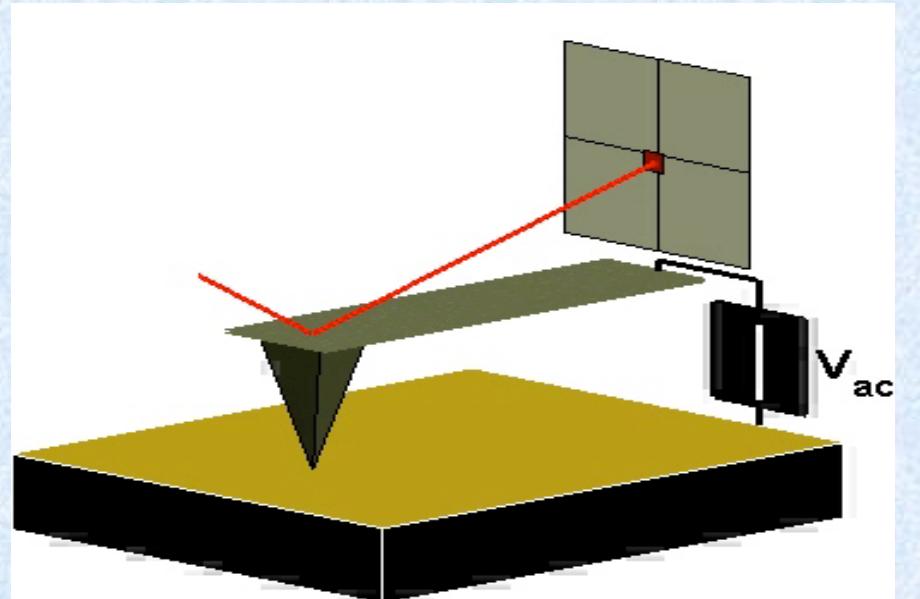
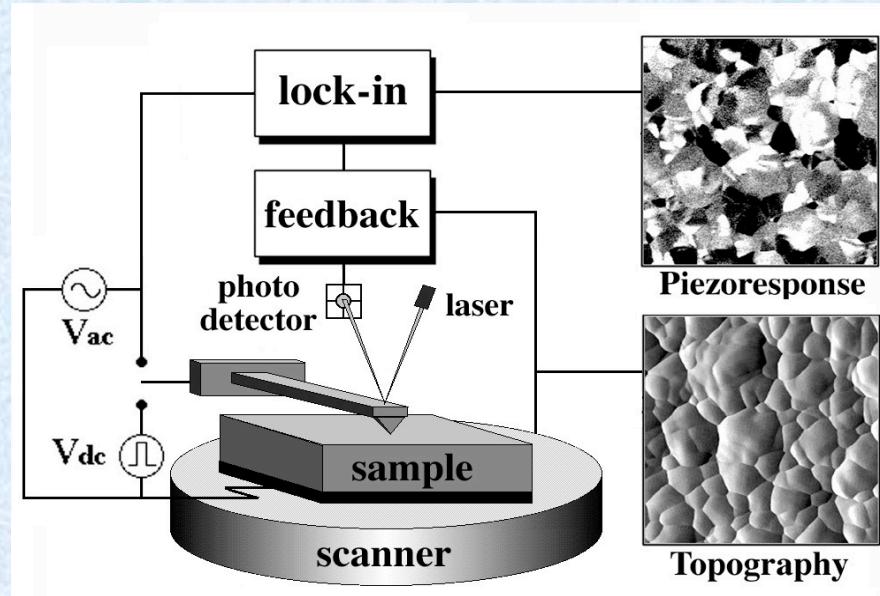
For P^+ (↓), $\varphi=0^\circ$

For P^- (↑), $\varphi=180^\circ$

$$\text{Vibration amplitude: } \Delta L_0 = d_{33} V_0$$

Principle of Piezoresponse Force Microscopy

PFM is based on the field-induced mechanical response (converse piezoeffect)



PZT thin film

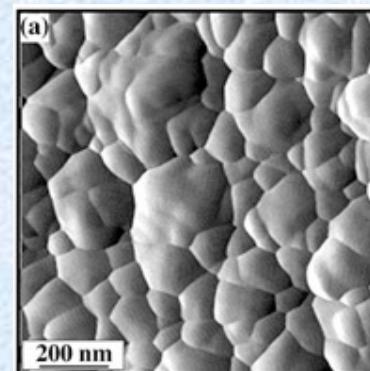
$$\text{AC voltage } V = V_0 \cos(\omega t)$$

$$\text{Surface displacement } \Delta z = d_{33}V_0 \cos(\omega t + \varphi)$$

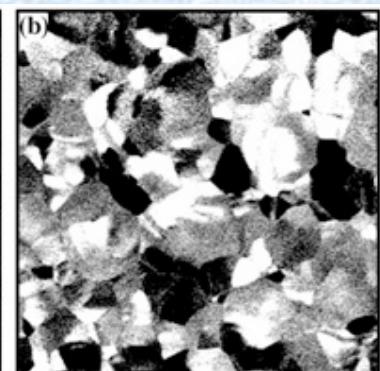
Phase: domain polarity

Magnitude: local piezocoefficient

DC bias: hysteresis loop and local switching



Topography

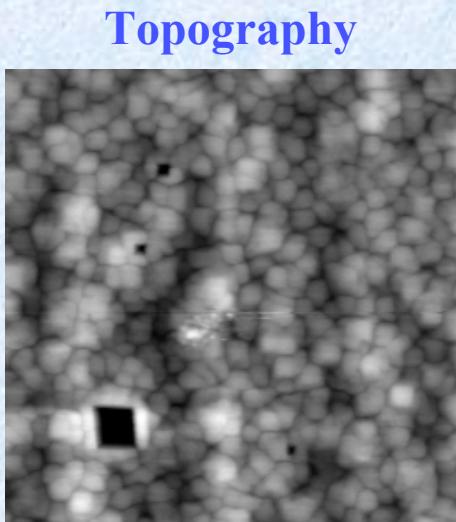


Piezoresponse

• Animation courtesy S. Jesse, ORNL

Phase and Amplitude Imaging in PFM

PFM phase and amplitude signals provide information on different properties

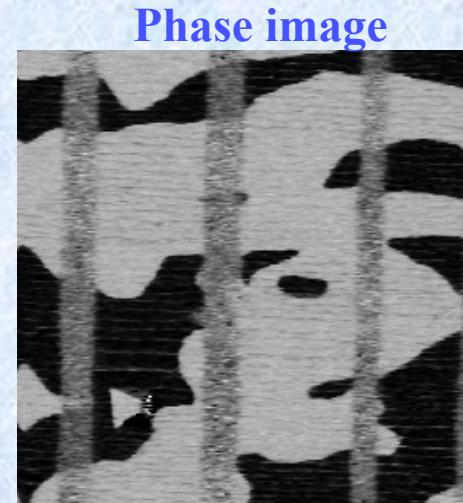


Amplitude recording:
piezoefficient



$$\Delta d = d_{33} E$$

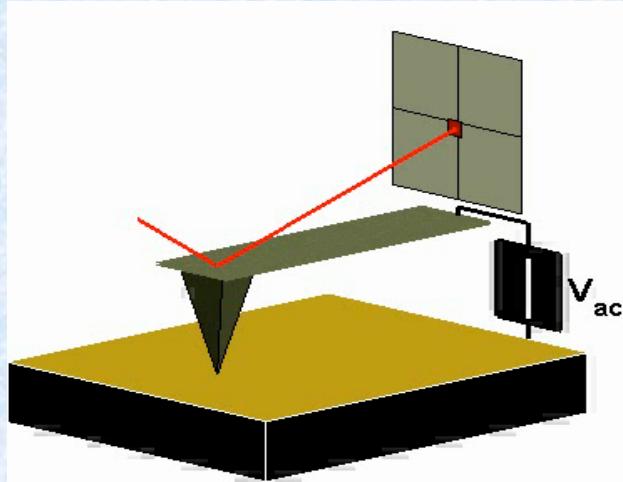
Phase recording:
polarization direction



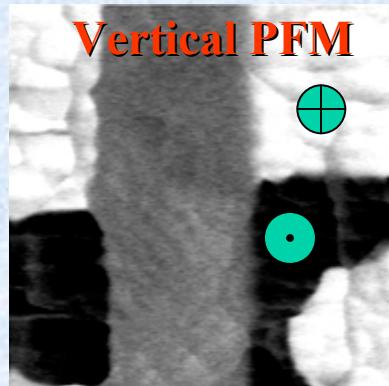
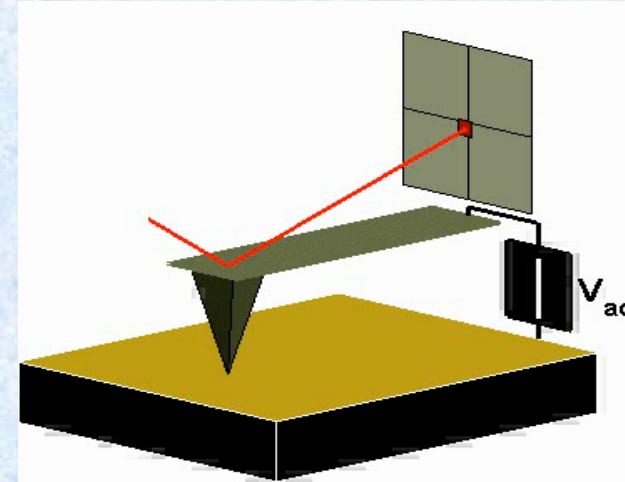
For P⁺, φ=0°; For P⁻, φ=180°

Vertical and Lateral PFM detection

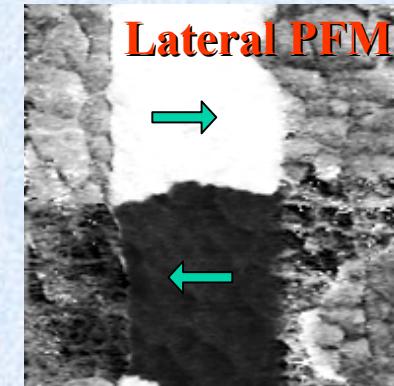
Vertical PFM



Lateral PFM



$$\Delta Z = \pm d_{33} V \cos(wt + \varphi)$$

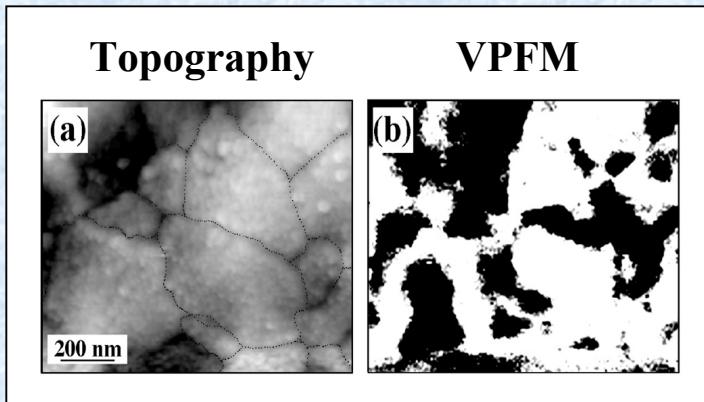


$$\Delta L = \pm d_{15} V \cos(wt + \varphi)$$

• Animation courtesy S. Jesse, ORNL

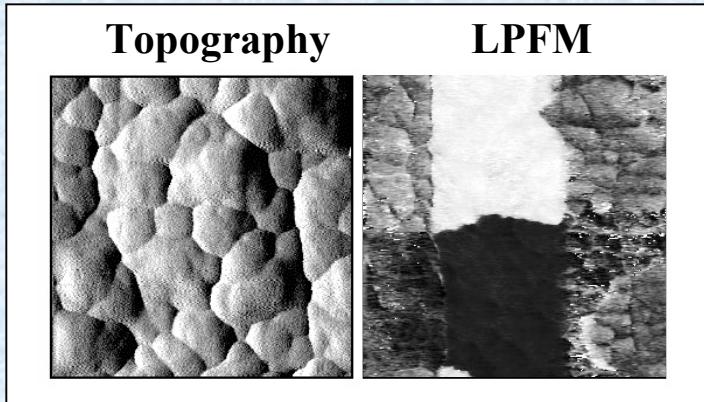
PFM: Out-of-Plane vs In-Plane Polarization

PZT (001) film



$$\Delta L = \pm d_{33} V \rightarrow d_{33} \propto P_s$$

PbTiO₃ (100) film



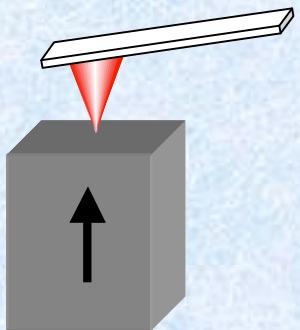
Tetragonal perovskite

$$\begin{pmatrix} 0 & 0 & 0 & 0 & d_{15} & 0 \\ 0 & 0 & 0 & d_{15} & 0 & 0 \\ d_{31} & d_{31} & d_{33} & 0 & 0 & 0 \end{pmatrix}$$

Vertical PFM

Lateral PFM (x)

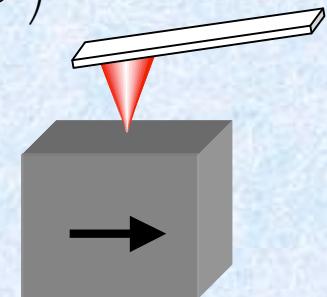
Lateral PFM (y)



Rotated by 90°

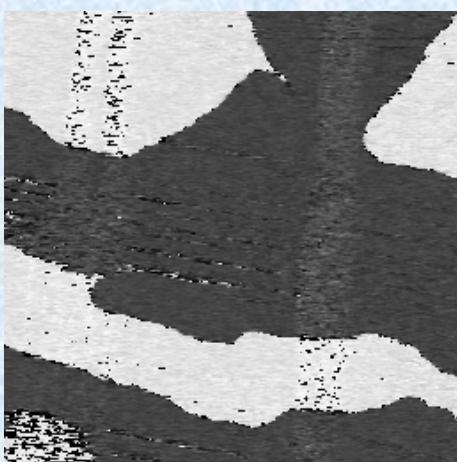
$$\begin{pmatrix} 0 & 0 & 0 & 0 & 0 & d_{15} \\ d_{31} & d_{33} & d_{31} & 0 & 0 & 0 \\ 0 & 0 & 0 & d_{15} & 0 & 0 \end{pmatrix}$$

Lateral PFM (x)

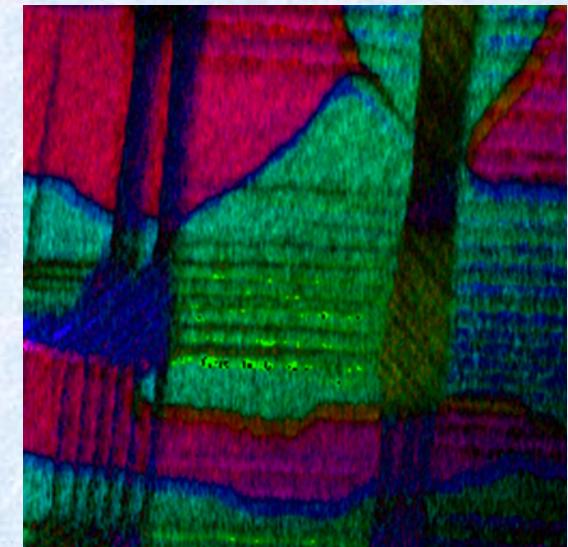
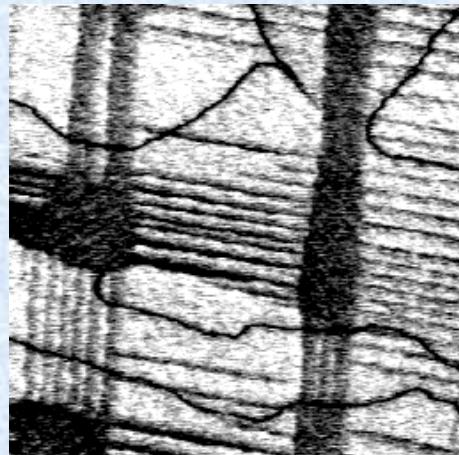


Color Representation of 2D PFM Data

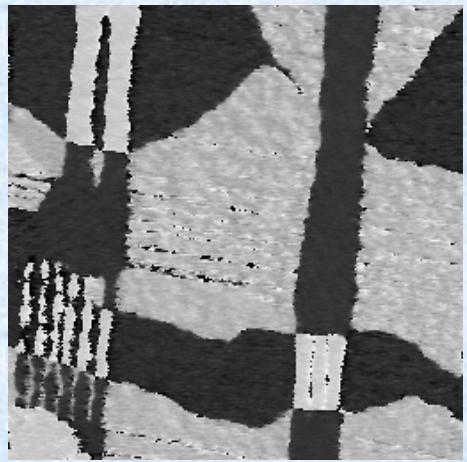
VPFM



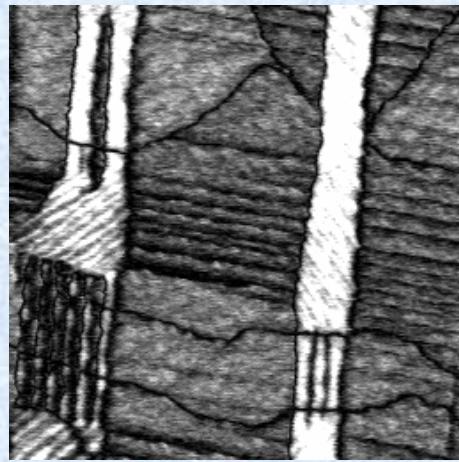
VPFM amplitude



LPFM



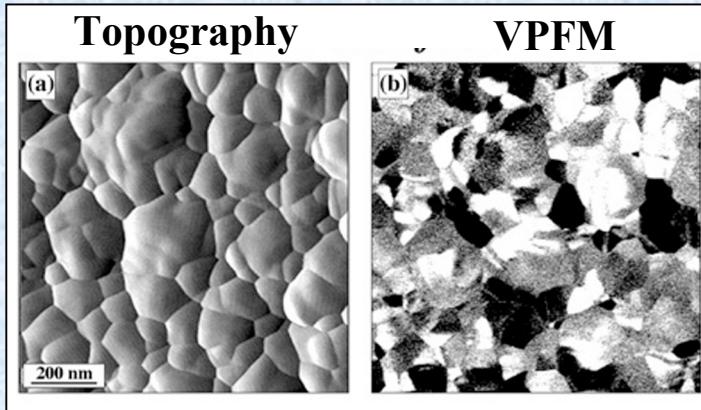
LPFM amplitude



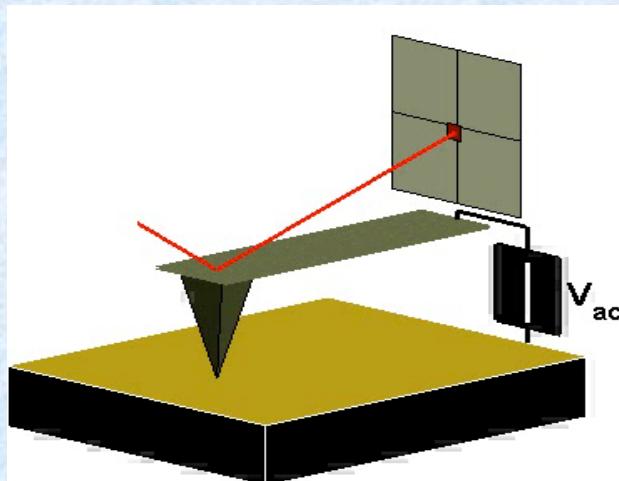
• Sample courtesy H. Funakubo

PFM of Polycrystalline Ferroelectrics

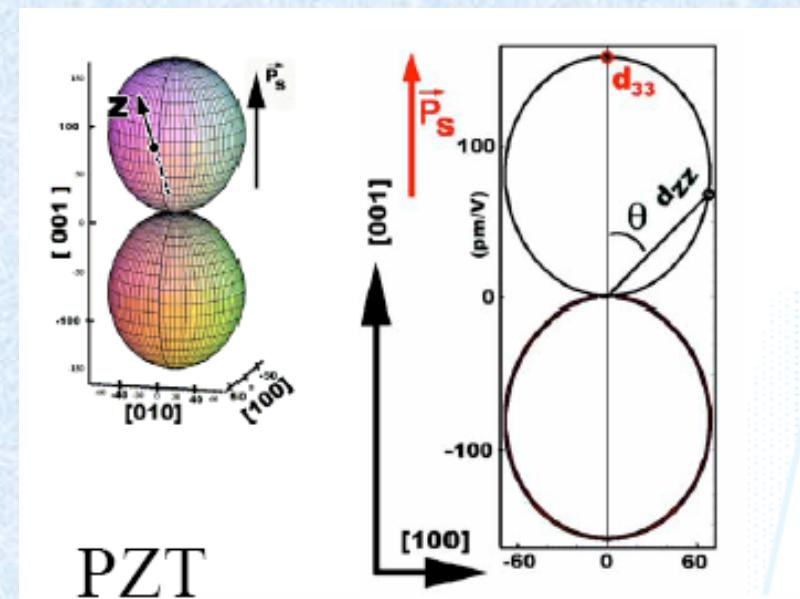
Randomly oriented grains



- P_s is not proportional to d_{33}
- Signal depends on d_{33} , d_{31} , d_{15}



VPFM surface for tetragonal $\text{Pb}(\text{Zr},\text{Ti})\text{O}_3$



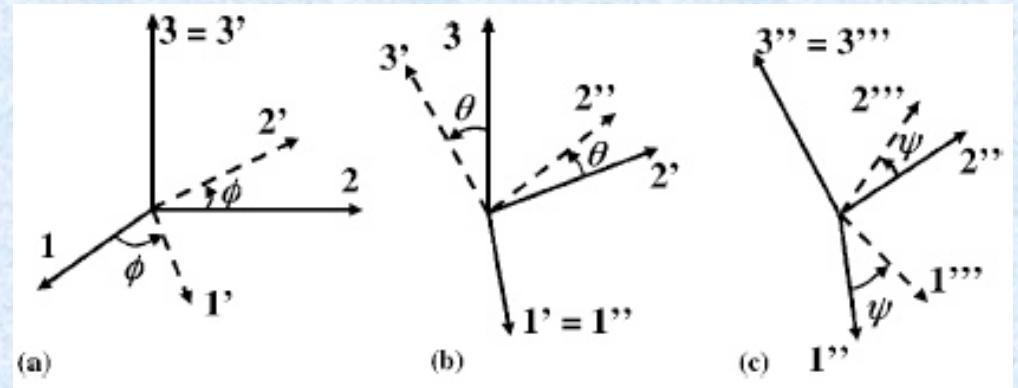
$$d_{zz}(\theta) = (d_{31} + d_{15}) \sin^2 \theta \cos \theta + d_{33} \cos^3 \theta$$

Harnagea et al, Integrated Ferroelectrics 38, 23 (2001)

• Animation courtesy S. Jesse, ORNL

Crystal Orientation Effect on PFM

PE tensor in the laboratory system of coordinates $d_{ij} = A_{ik}d_{kl}^0 N_{lj}$



In general case:

VPFM:

$$d_{zz} = (d_{31} + d_{15})\sin^2 \theta \cos \theta + d_{33} \cos^3 \theta$$

LPFM:

$$d_{zx} = -(d_{31} - d_{33} + (d_{15} + d_{31} - d_{33})\cos 2\theta)\cos \psi \sin \theta$$

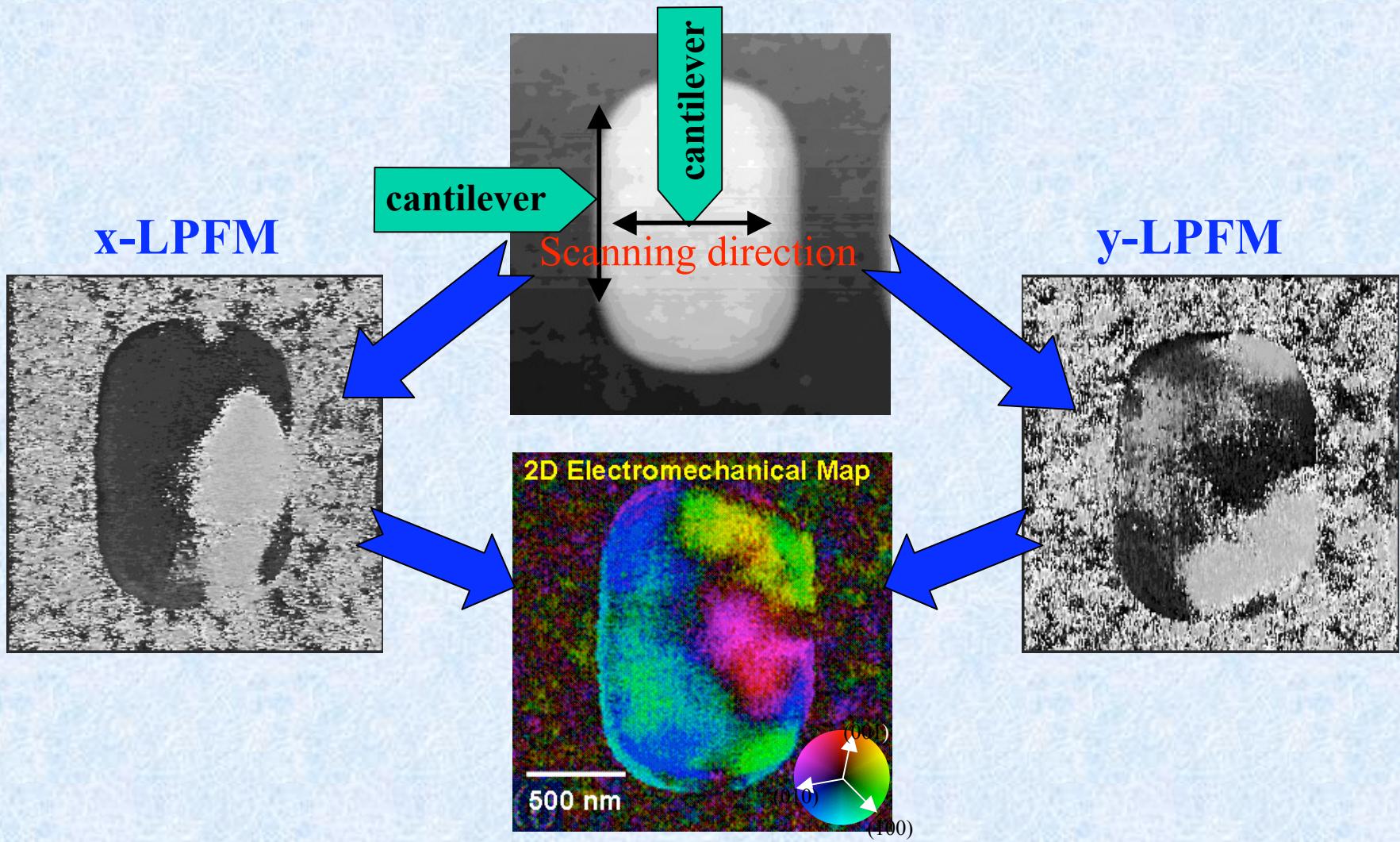
$$d_{zy} = -(d_{31} - d_{33} + (d_{31} + d_{31} - d_{31})\cos 2\theta)\sin \psi \sin \theta$$

Transformations for transition from crystal to laboratory coordinate system

- From 3D PFM data either the piezoelectric constants d_{ij} or local orientation map (θ , ϕ , ψ) can be obtained
- For materials with known constraints on possible crystallographic orientation polarization reconstruction can be performed

2D PFM imaging in (111) PZT capacitor

In-plane polarization mapping in poled capacitor



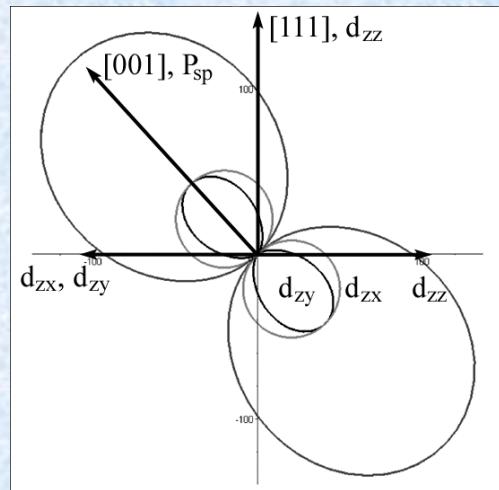
3D Reconstruction of Polarization in a PZT Capacitor

Simple case where possible directions are known: PZT (111)

VPFM: $d_{zz}(\theta) = (d_{31} + d_{15})\sin^2 \theta \cos \theta + d_{33} \cos^3 \theta$

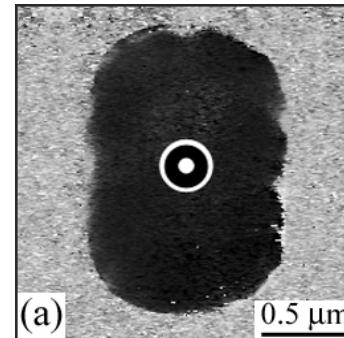
x-LPFM: $d_{zx}(\theta) = d_{31} \cos \theta$

y-LPFM: $d_{zy}(\theta) = (d_{33} - d_{15})\sin^2 \theta \cos \theta + d_{31} \cos^3 \theta$

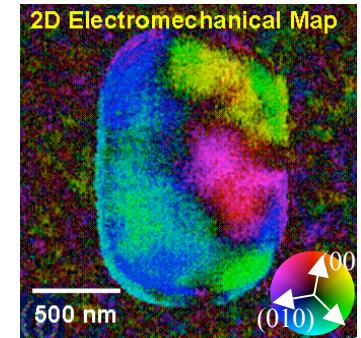


- Poled capacitors, which appear uniformly polarized in VPFM, are in fact in a polydomain state

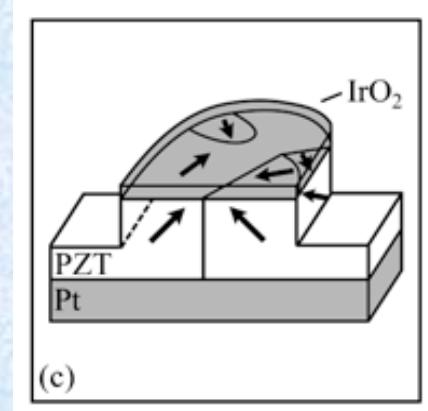
Out-of-plane polarization



2D in-plane map



3D reconstruction



Rodriguez et al, Appl. Phys. (2005)

Elementary Theory of PFM

Total response of the cantilever in contact with a ferroelectric:

$$\mathbf{A} = \mathbf{A}_{em} + \mathbf{A}_{cap} + \mathbf{A}_{nl}$$

Useful reference:

S. Kalinin and D. Bonnell, PRB (2001)

where

\mathbf{A}_{em} - electromechanical response

$$A_{em} = d_{33}V_{ac} + 2\frac{M_{333}}{t}V_{ac}^2$$

\mathbf{A}_{cap} - capacitive/electrostatic response $F_{cap} + F_{Coul} = \frac{1}{2}V^2 \frac{dC}{dz} + \frac{\sigma CV}{2\varepsilon_0}$

\mathbf{A}_{nl} - non-local (cantilever) response

Can be neglected for most practical cases

For tetragonal phase of
 BaTiO_3 (E parallel to P_s)

$$d_{33} = 2\chi_{33}Q_{33}P_{s3} \quad \text{Expansion/contraction}$$

$$d_{35} = 2\chi_{33}Q_{55}P_{s1}$$

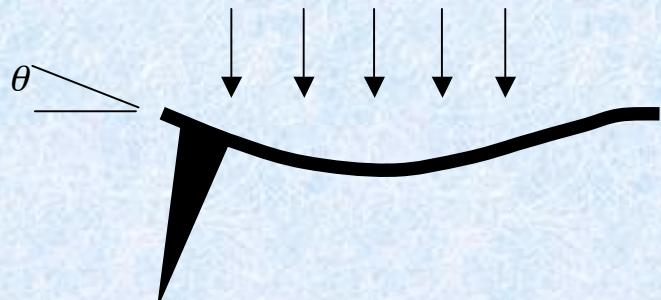
$$d_{34} = 2\chi_{33}Q_{44}P_{s2}$$

Shear

Shear

Cancelled out

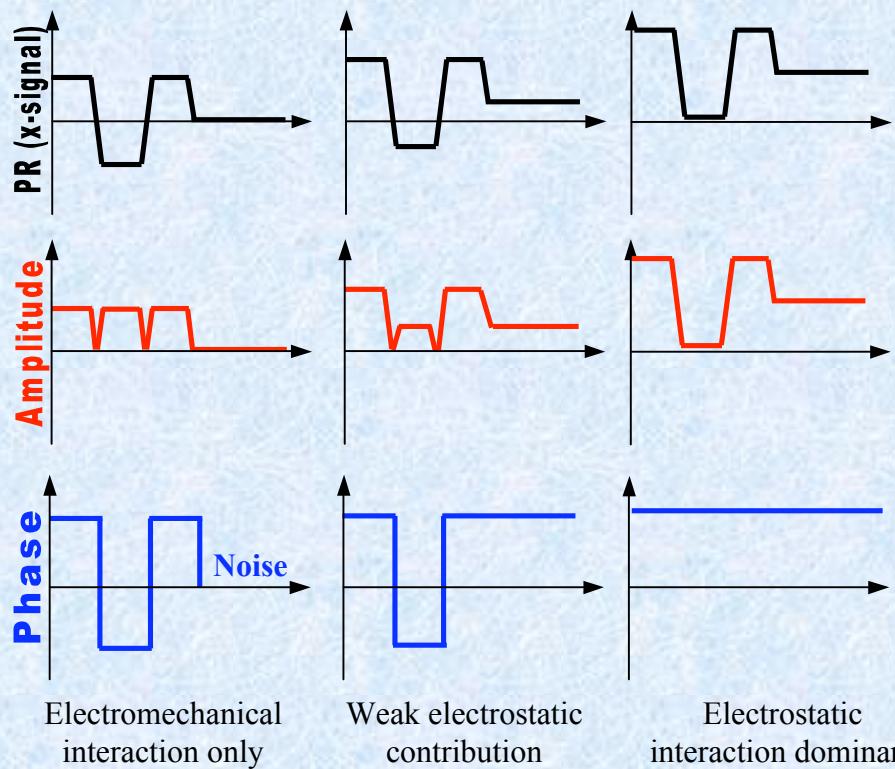
Electrostatic Contribution to PFM



Why quantifying PFM contrast is difficult:

- Tip is in contact - both electrostatic and electromechanical interactions contribute
- Total response contains both local and non-local contributions

Qualitative Aspects of Electrostatic Signal



PFM signal over positive domain

$$PR_+ = d_{33} + F_{nl}(V_{tip} - V_{av})$$

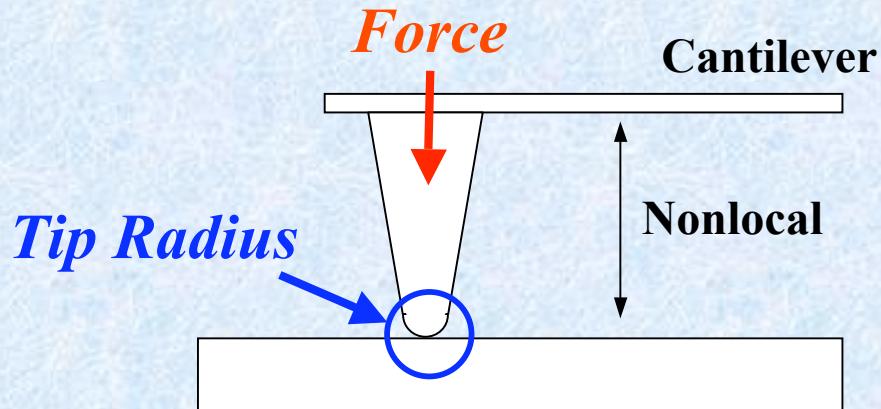
PFM signal over negative domain

$$PR_- = -d_{33} + F_{nl}(V_{tip} - V_{av})$$

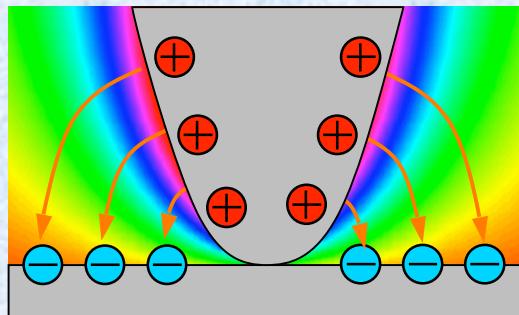
Stiffness criterion:

$$PR = d_{eff} + \frac{Lw\epsilon_0\Delta V}{48kH^2}$$

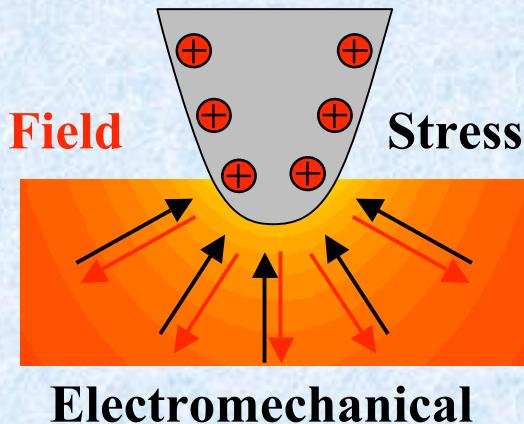
Various Imaging Regimes in PFM



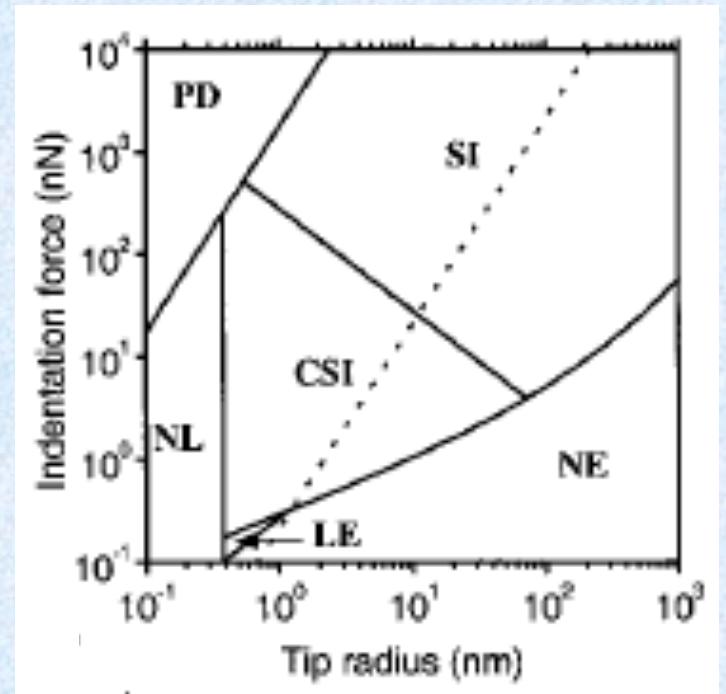
Local Piezoresponse Contrast



Electrostatic



Electromechanical



E - Electrostatic

NL - Non-local interactions

PD - Plastic Deformation

SI - Strong Indentation

CWI - Weak indentation

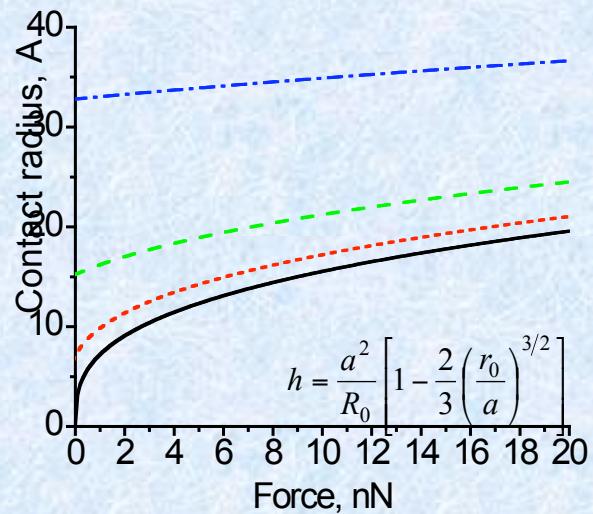
Kalinin and Bonnell, PR B (2002)

PFM Resolution Limits

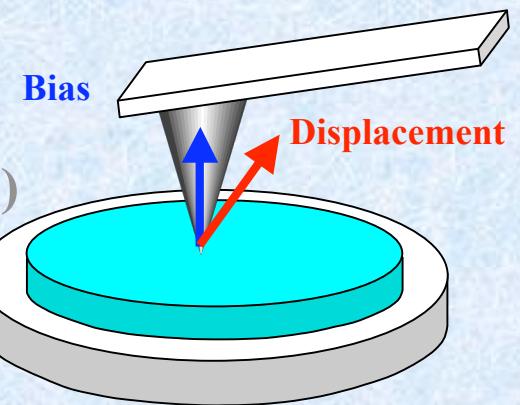
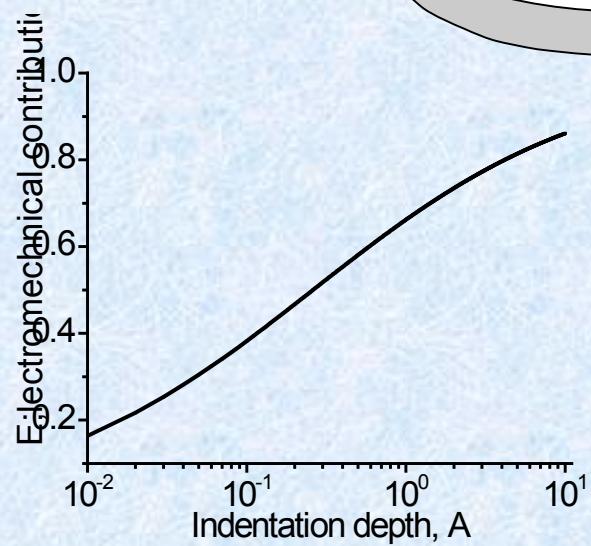
Ideally, we want to probe electromechanical behavior with $\sim 1 \text{ pm/V}$ sensitivity at $\sim 0.1\text{-}1 \text{ V}$ excitation bias on molecular (biosystems) and unit cell (ferroelectrics) level.

PFM limitations: contact mode technique

- electrostatic tip-surface interactions
- formation of liquid necks at the tip-surface junction
- large contact force – large contact area (low resolution)
- difficult to use resonant enhancement
- probing dynamic processes



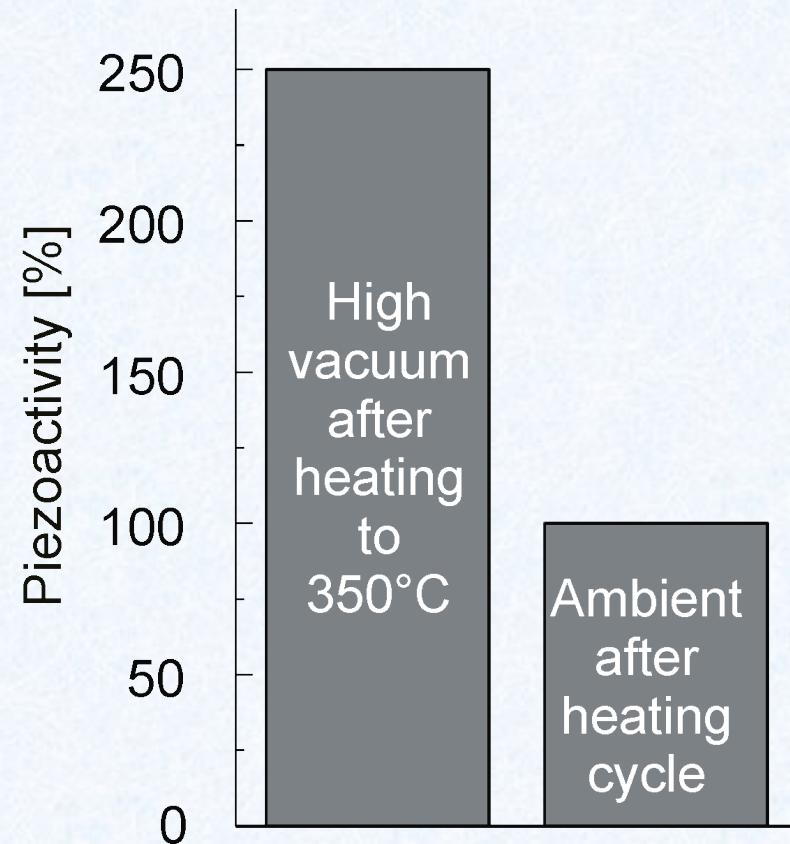
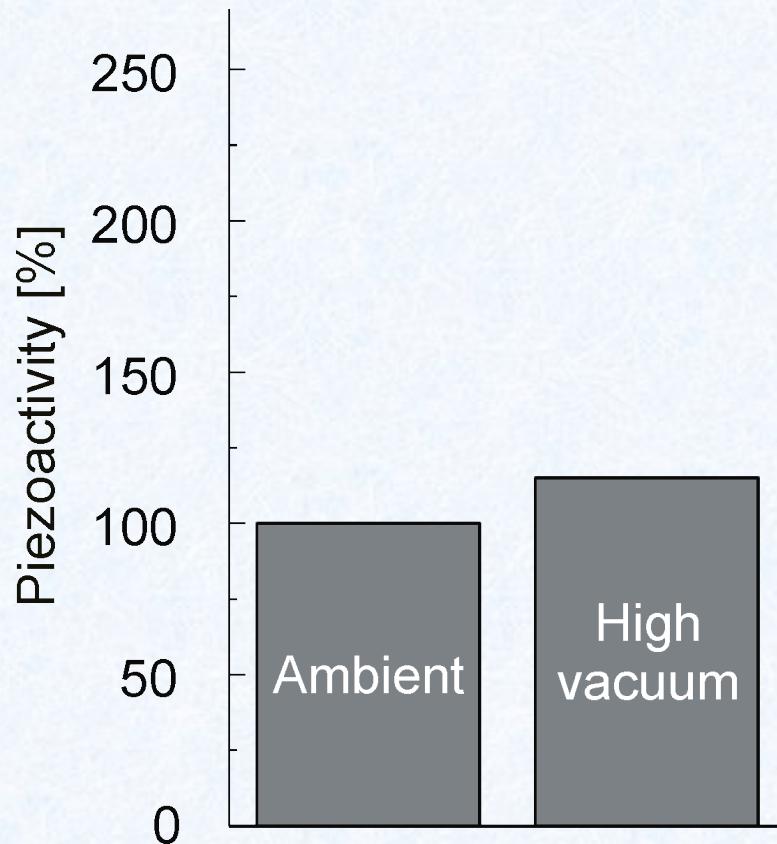
$$a^3 = \frac{R_0}{E^*} \left\{ P + 3\sigma\pi R_0 + \sqrt{6\sigma\pi R_0 P + (3\sigma\pi R_0)^2} \right\}$$



$$PR = \alpha_a(h) d_3 \frac{k_1}{k_1 + k} + \frac{C'_s}{k_1 + k} (V_{dc} - V_s)$$

Surface Contamination Effect in PFM

PFM measurements of a BaTiO_3 single crystal

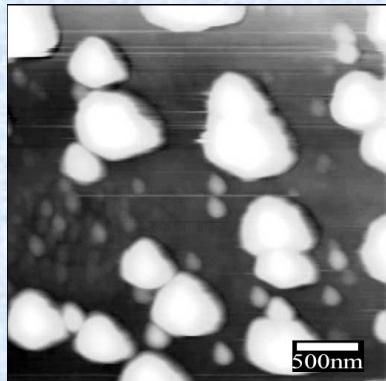


Peter, Ruediger, Waser, RSI (2006)

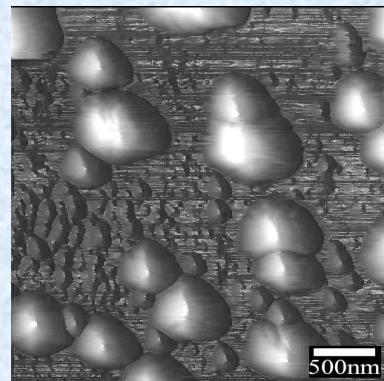
Topographic Cross-talk in PFM

(001) PZT grains

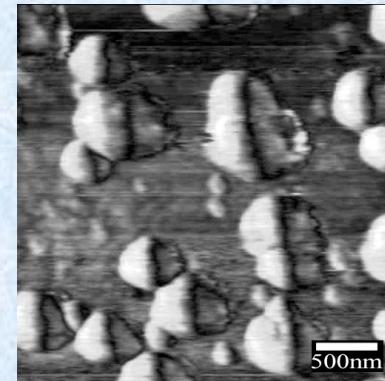
Topography



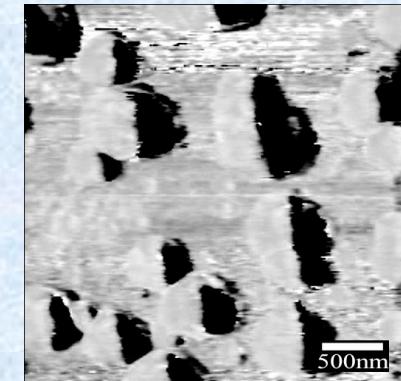
Derivative



VPFM amplitude



VPFM phase



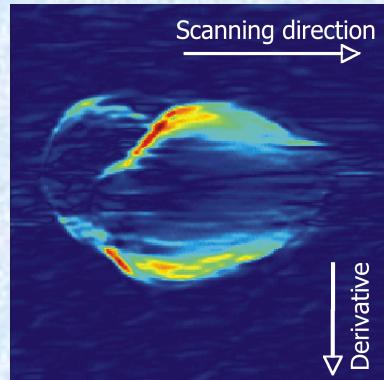
Data courtesy S.Kalinin

(001) BaTiO₃ grain

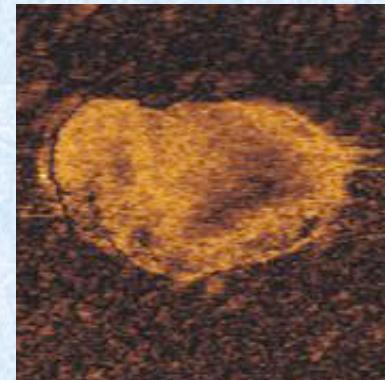
Topography



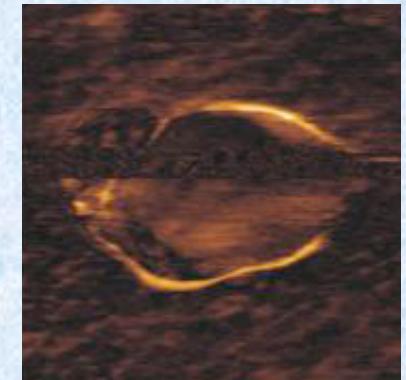
Derivative



VPFM



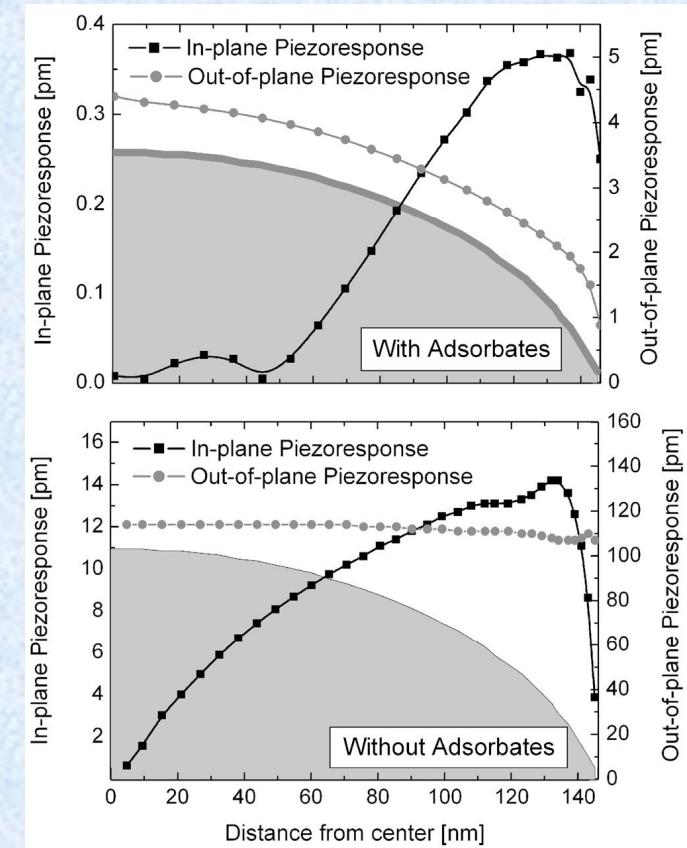
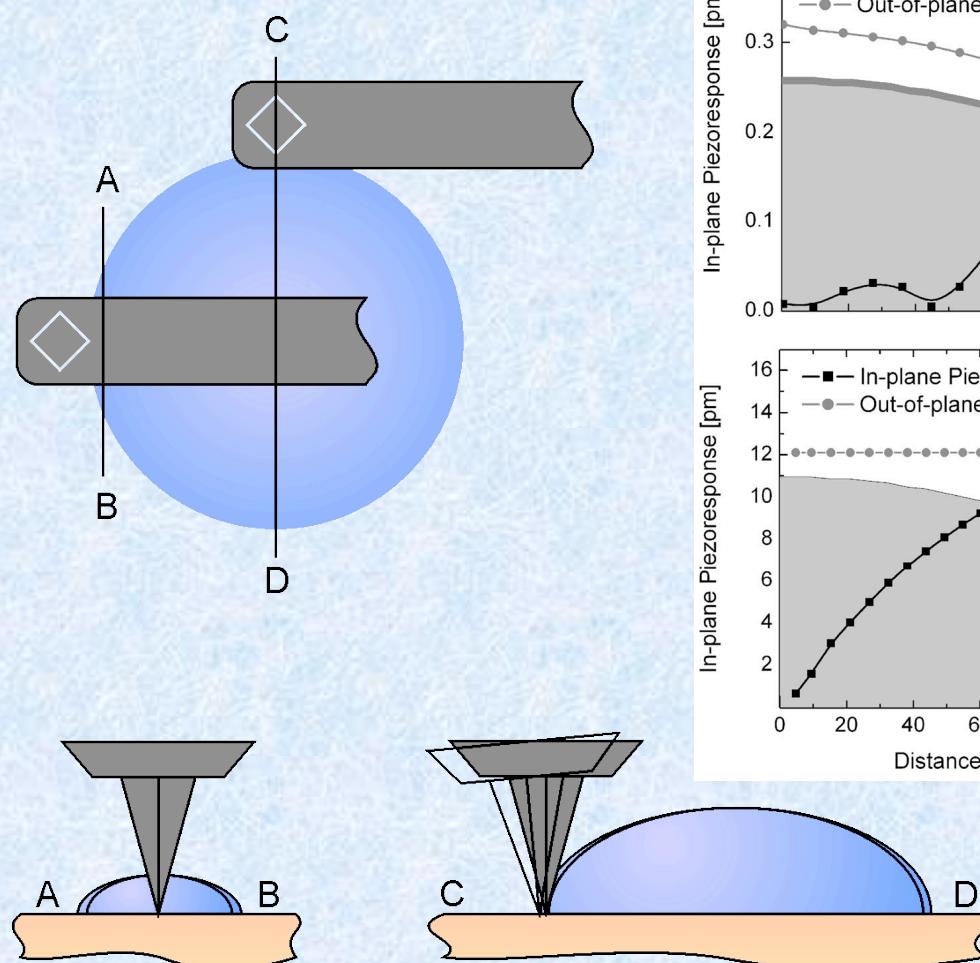
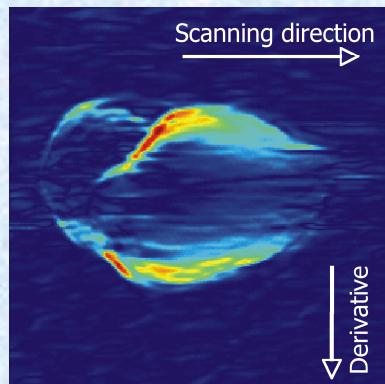
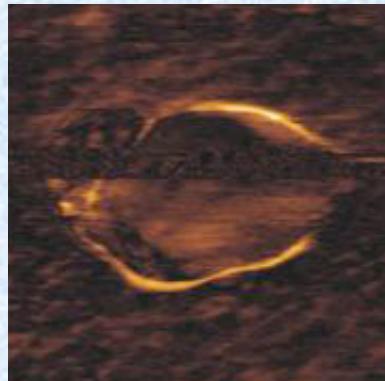
LPFM



Peter, Ruediger, Waser, RSI (2006)

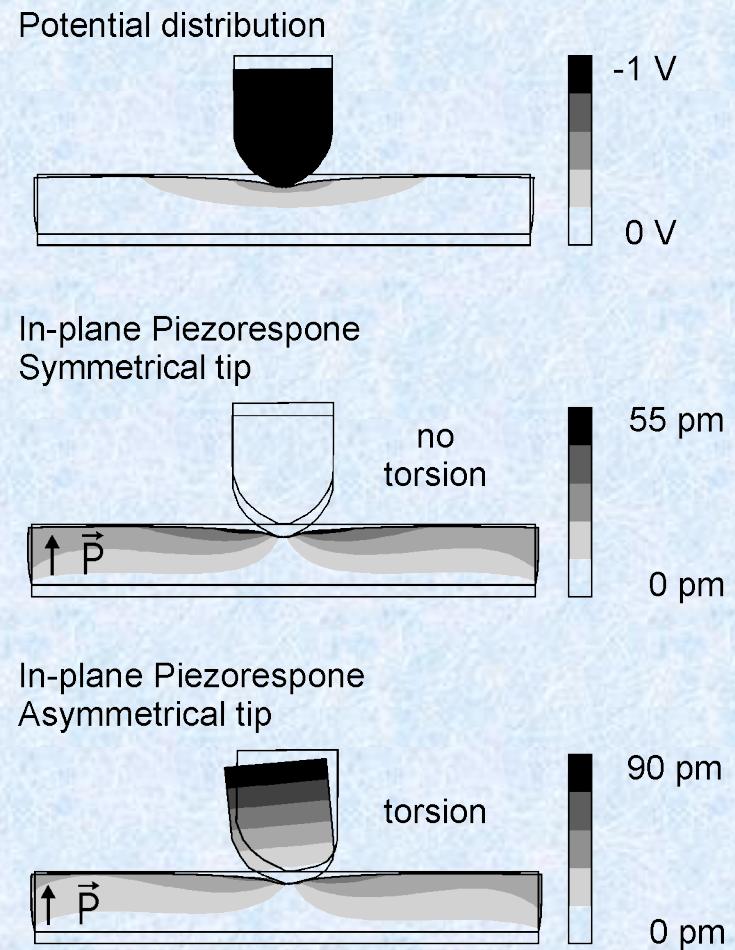
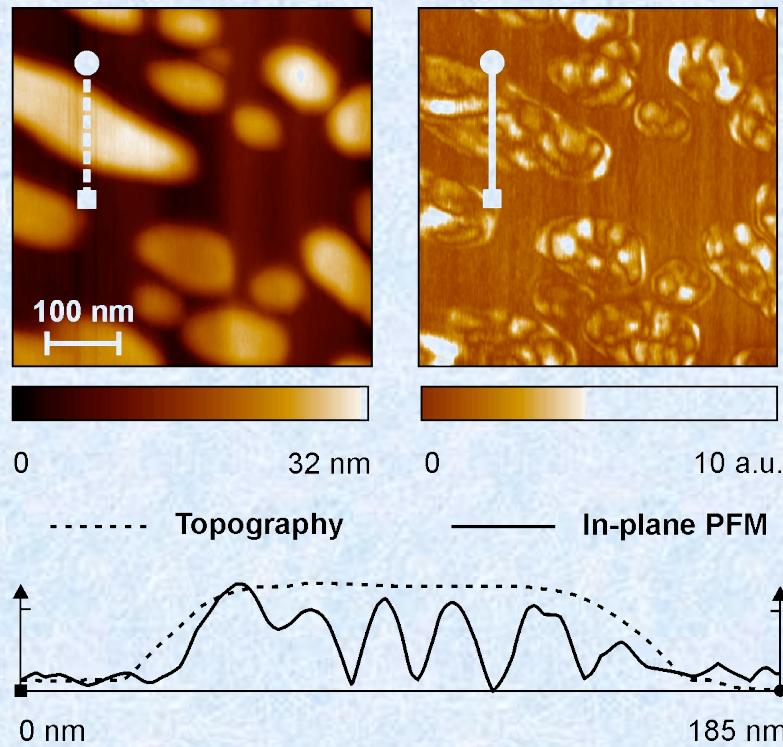
Topographic Cross-talk in PFM

(001) BaTiO₃ grain



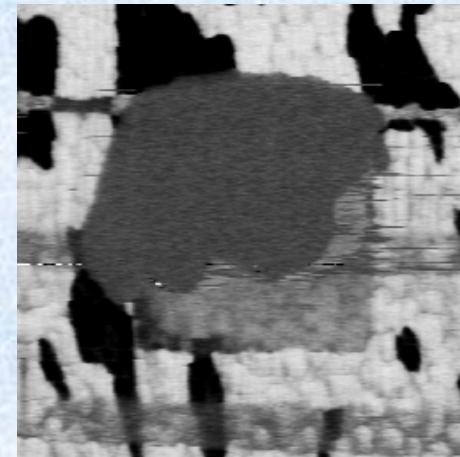
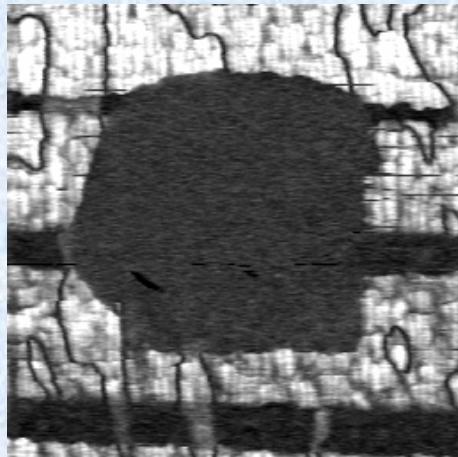
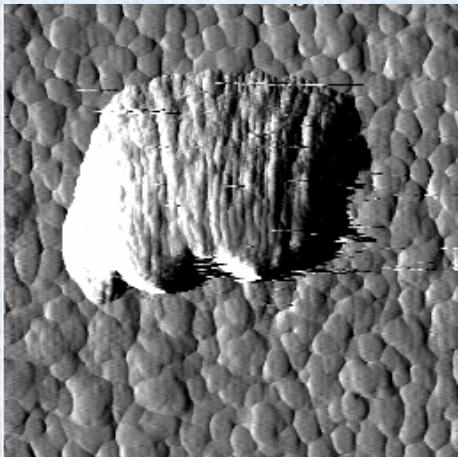
Slide courtesy A.Ruediger, RWTH

Tip Shape Effect in PFM



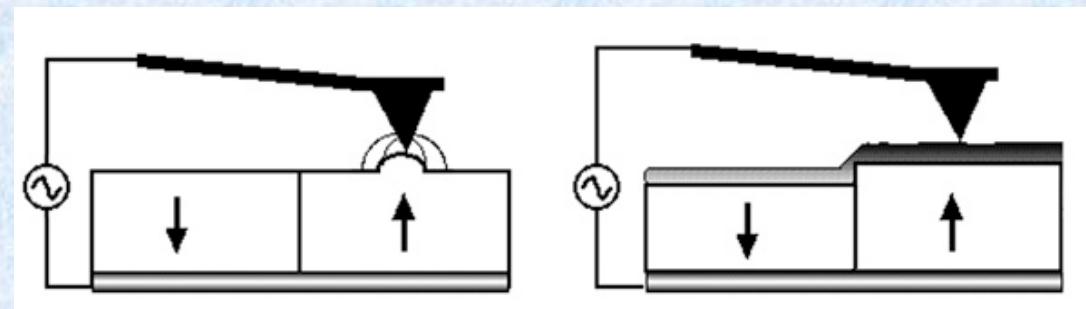
Slide courtesy A.Ruediger, RWTH

Surface Modification Effect in PFM



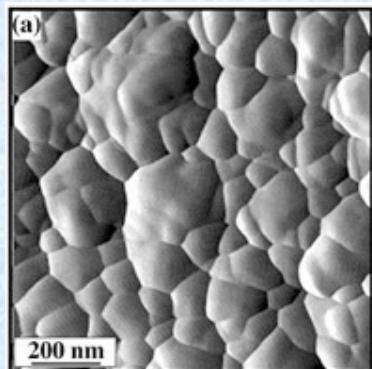
Built-up of foreign substance (tip material transfer, adsorbates) during long bias application results in surface modification and a change in PFM signal.

Local vs Integral Excitation (Thin Films vs Capacitors)

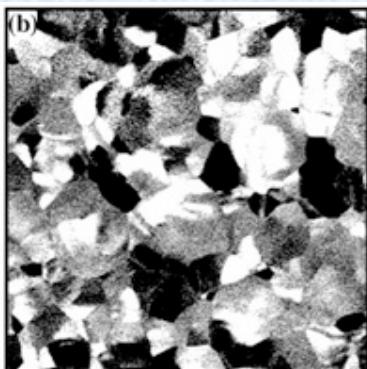


PZT thin film

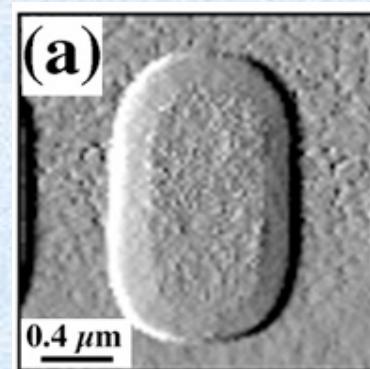
PZT capacitor



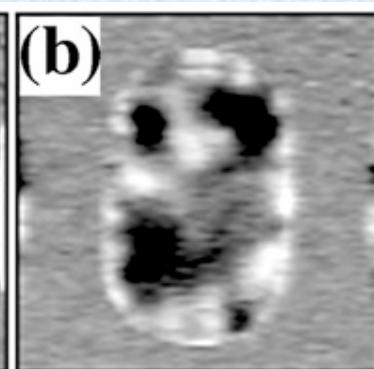
Topography



Piezoresponse



Topography



Piezoresponse

Note: your ac power supply should be able to supply enough energy to generate piezoelectric oscillation in the capacitor.

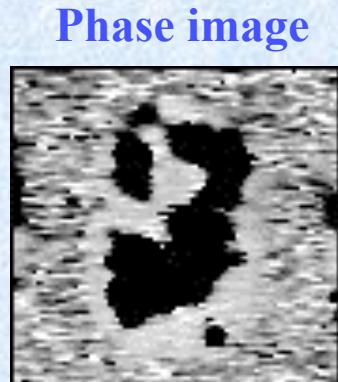
Separate Recording of Phase and Amplitude in PFM

PFM provides information on local switching behavior within a capacitor
Measures absolute value of piezoelectric constant

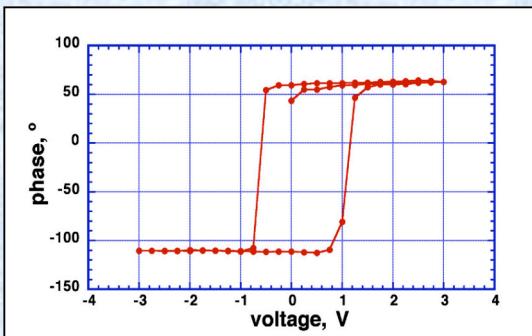
Phase recording:

polarization direction

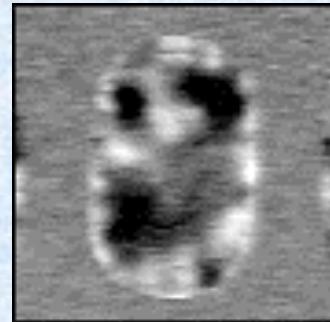
For P^+ , $\varphi=0^\circ$; For P^- , $\varphi=180^\circ$



Phase loop



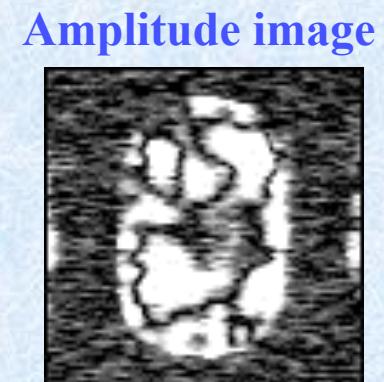
Mixed PFM image



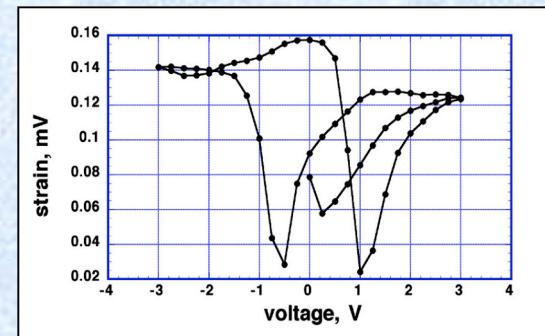
Amplitude recording:

switchable volume

$$\Delta d = ad_{33} \int E(z) dz$$



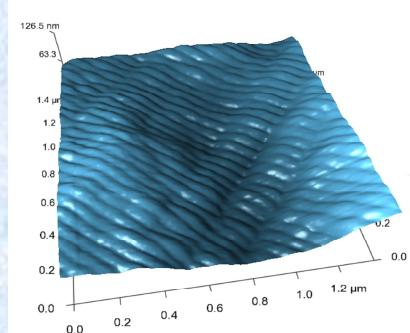
Amplitude loop



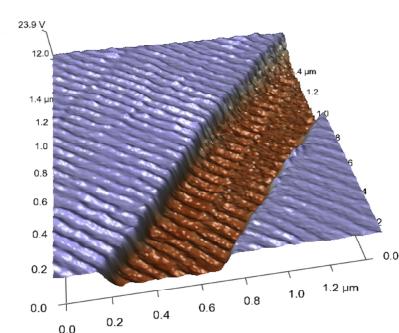
PFM Imaging of Piezoelectric Materials

Collagen fibers

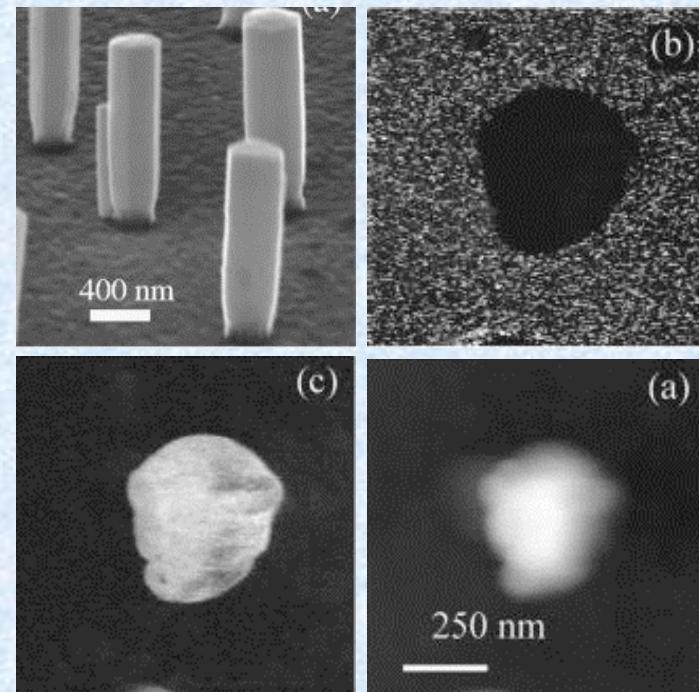
Topography



PFM phase



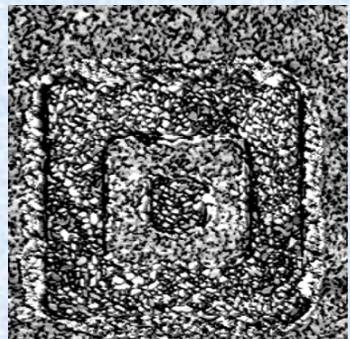
ZnO nanorods



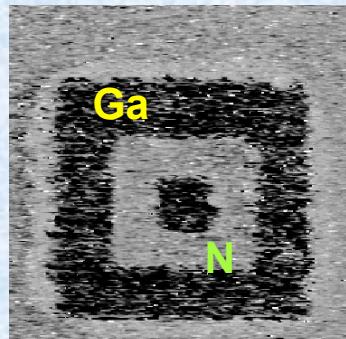
- Structural imaging in biomaterials

GaN films

Topography



PFM



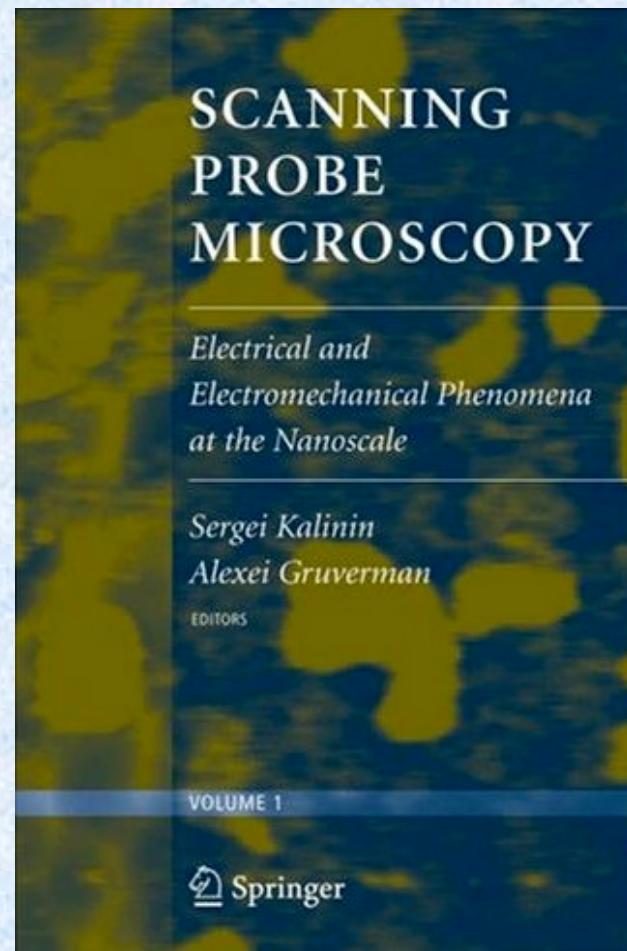
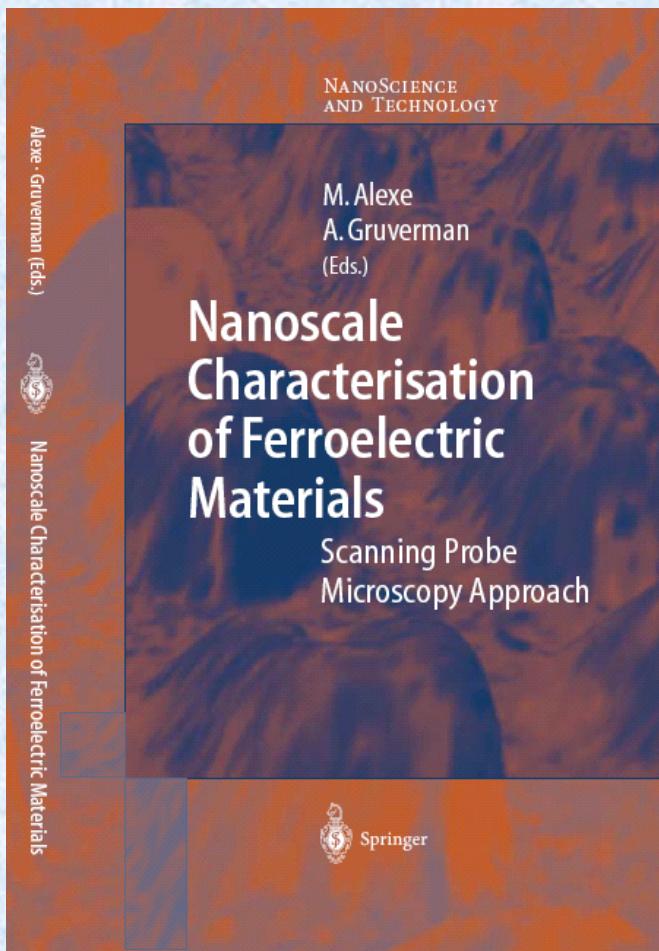
- Detection of inverse domains in III-N semiconductors

Scrymgeour et al, JAP (2007)

- Evaluation of piezoelectric properties in nanostructures

Books on PFM of Ferroelectrics

...presents recent advances in the field of nanoscale characterization of ferroelectric materials using SPM. ...addresses various imaging mechanisms of ferroelectric domains in SPM, quantitative analysis of the SPM signals, as well as nanoscale switching, scaling effects, and transport behavior.



Conclusion

- PFM has become a standard tool for investigation of nanoscale properties of ferroelectric materials
- PFM in combination with various SPM methods provides complementary information for quantitative analysis of surface and bulk properties of ferroelectrics
- PFM allows characterization of electromechanical and structural properties of a wide range of piezoelectrically active materials leading to a better understanding of material functionality down to the nanoscale level.